

form of a heuristic function that estimates how far a given state is from the goal, or if we precompute partial solutions involving patterns or landmarks.

- Before an agent can start searching, a well-defined **problem** must be formulated.
- A problem consists of five parts: the **initial state**, a set of **actions**, a **transition model** describing the results of those actions, a set of **goal states**, and an **action cost function**.
- The environment of the problem is represented by a **state space graph**. A **path** through the state space (a sequence of actions) from the initial state to a goal state is a **solution**.
- Search algorithms generally treat states and actions as **atomic**, without any internal structure (although we introduced features of states when it came time to do learning).
- Search algorithms are judged on the basis of **completeness**, **cost optimality**, **time complexity**, and **space complexity**.
- **Uninformed search** methods have access only to the problem definition. Algorithms build a search tree in an attempt to find a solution. Algorithms differ based on which node they expand first:
  - **Best-first search** selects nodes for expansion using an **evaluation function**.
  - **Breadth-first search** expands the shallowest nodes first; it is complete, optimal for unit action costs, but has exponential space complexity.
  - **Uniform-cost search** expands the node with lowest path cost,  $g(n)$ , and is optimal for general action costs.
  - **Depth-first search** expands the deepest unexpanded node first. It is neither complete nor optimal, but has linear space complexity. **Depth-limited search** adds a depth bound.
  - **Iterative deepening search** calls depth-first search with increasing depth limits until a goal is found. It is complete when full cycle checking is done, optimal for unit action costs, has time complexity comparable to breadth-first search, and has linear space complexity.
  - **Bidirectional search** expands two frontiers, one around the initial state and one around the goal, stopping when the two frontiers meet.
- **Informed search** methods have access to a **heuristic** function  $h(n)$  that estimates the cost of a solution from  $n$ . They may have access to additional information such as pattern databases with solution costs.
  - **Greedy best-first search** expands nodes with minimal  $h(n)$ . It is not optimal but is often efficient.
  - **A\* search** expands nodes with minimal  $f(n) = g(n) + h(n)$ . A\* is complete and optimal, provided that  $h(n)$  is admissible. The space complexity of A\* is still an issue for many problems.
  - **Bidirectional A\* search** is sometimes more efficient than A\* itself.
  - **IDA\*** (iterative deepening A\* search) is an iterative deepening version of A\*, and thus addresses the space complexity issue.
  - **RBFS** (recursive best-first search) and **SMA\*** (simplified memory-bounded A\*) are robust, optimal search algorithms that use limited amounts of memory; given enough time, they can solve problems for which A\* runs out of memory.