# EECS 225A Spring 2005

## **Common themes**

Complex variables

Real functions of a complex variable contains  $z^*$ , not analytic Stationary points  $\frac{\partial}{\partial z^*} = 0$ Gradient  $\frac{\partial}{\partial z^*} = 0$ 

Linear time-invariant systems

Complex exponentials Impulse response, transfer function

Rational transfer functions of a complex variable z

Poles and zeros Minimum-phase Real-valued unit-sample response Real-valued on unit circle Spectral factorization: non-negative on unit circle Allpass: unit magnitude on unit circle Structures Direct form Lattice

#### Matrices

Hermitian Real-valued eigenvalues Orthonormal eigenvectors Spectral theorem Toeplitz Circulant Eigenvalues = FFT Eigenvectors = complex exponential Linear equations Result from quadratic criteria No solutions, many solutions, unique solution

### Time and ensemble averages

Wiener filters Non-causal vs causal FIR (matrix) vs IIR (transfer function) Predictor Joint process estimator Estimation Linear vs. non-linear Orthogonality principle applies to both Quadratic criteria, linear estimates

#### Model vs. non-parametric

Signals (sample functions) vs statistics MA, AR, ARMA Polynomial coefficients Polynomial roots Reflection coefficients Harmonic: sum of sinusoids

Non-stationary signals

Steepest descent, LMS Recursive LS Block processing Time-frequency representations Time resolution vs frequency resolution Bandpass filters vs transforms