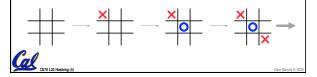


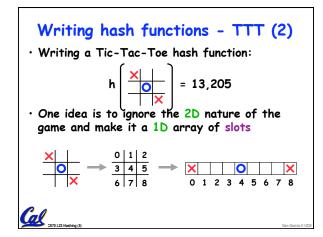
## **Hash Function**

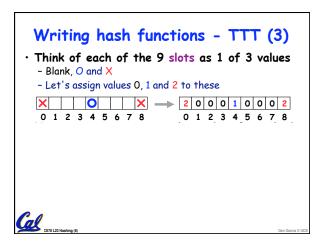
- If what we want to memoize isn't a simple number, how do we convert it to a number to easily store it into a table?
- We need something that can help us map this data into an integer, to serve as an index into an array (used to store the table).
- This mapping function is called a hash function
- http://en.wikipedia.org/wiki/Hash\_function

## Writing hash functions - TTT (1)

- Let's consider Tic-Tac-Toe:
  - One player chooses X, the other chooses O
  - They take turns placing their piece on the board
  - Assume X goes first
  - Once a piece is placed, it isn't moved
  - The player who first gets 3-in-a-row wins
  - If the board gets filled up and nobody wins, it's a tie







## Writing hash functions - TTT (4)

- Analysis of ternary polynomial hashcode:
  - What's the smallest #?

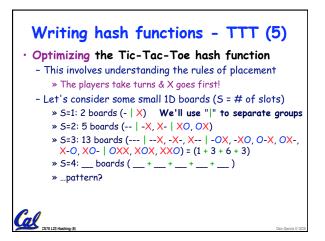
Cal

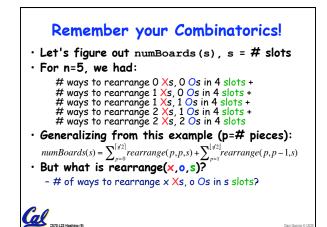
- What's the biggest #?
- Is this as optimal (I.e., tightly-packed) as possible? No!

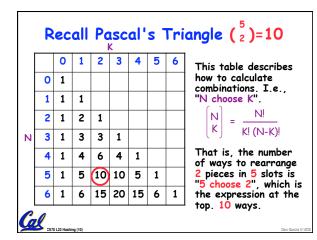
0

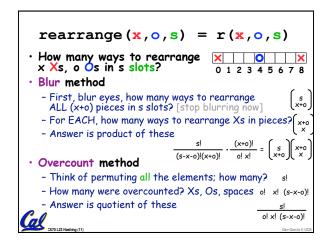
3<sup>9</sup>-1

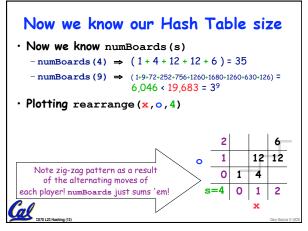
- Any suggestions for making this more optimal?

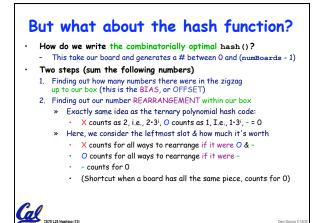


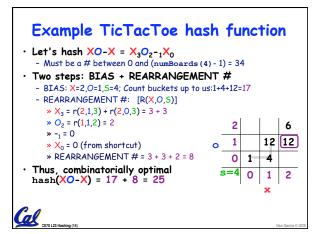












## Summary

- We showed how to calculate combinatorially optimal hash functions for a game - In real-world applications, we often find this useful
- If it's too expensive, we usu. settle for sub-optimal
- A good hash function spreads out values evenly • Sometimes hard to write good hash function
- In 8 real applications, 2 had written poor hash funs • Java has a great hash function for Strings
- Strings are commonly used as the keys (the things you hash upon for a data structure)

Cal