

Xisa: Extensible Inductive Shape Analysis

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The promise of program analysis: Eliminate entire classes of bugs

For example,

- Reading from a closed file: `read();` 
- Reacquiring a locked lock: `acquire();` 

How?

- Systematically examine the program
- Simulate running program on “all inputs”
- “Automated code review”

Program analysis by example: Checking for double acquires

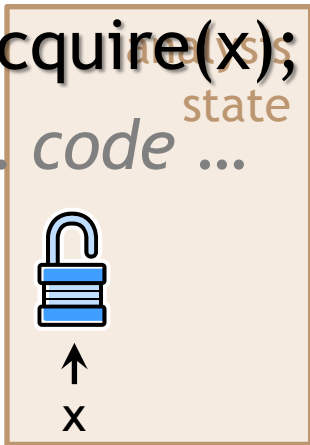
Simulate running program on “all inputs”

...code ...

// x now points to an unlocked lock

acquire(x);

... code ...



Program analysis by example: Checking for double acquires

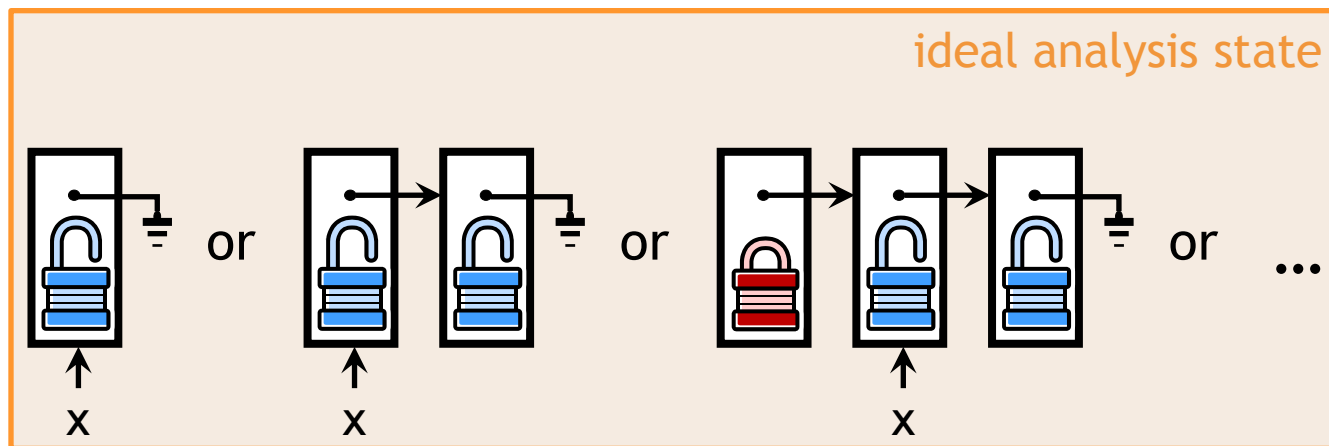
Simulate running program on “all inputs”



undecidability

...code ...

// x now points to an unlocked lock in a linked list



`acquire(x);`

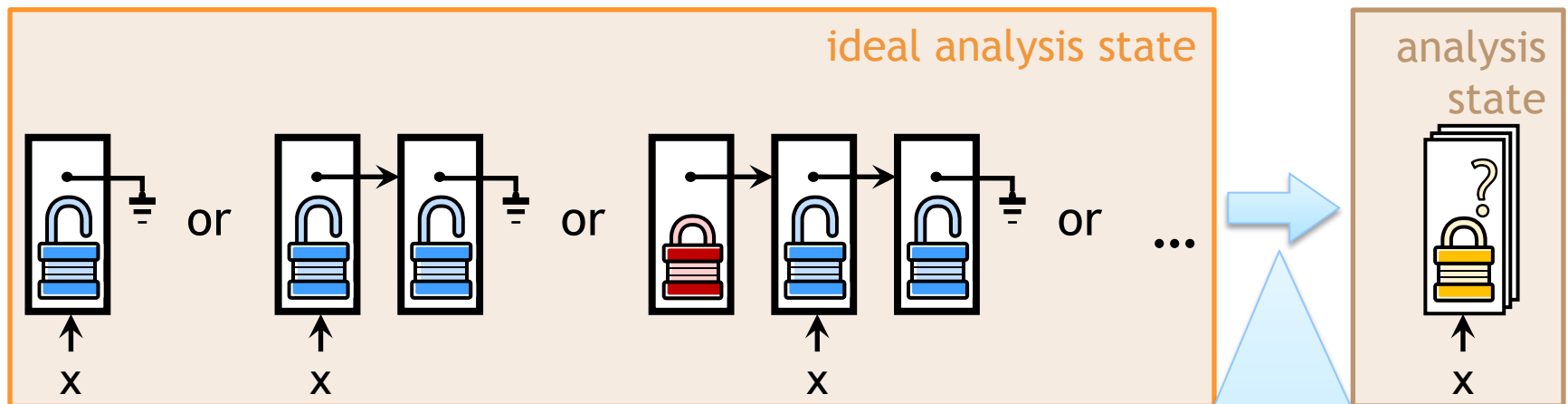
... code ...

Must abstract

Abstraction too coarse or **not precise** enough
(e.g., lost x is always unlocked)

...code ...

// x now points to an unlocked lock in a linked list



`acquire(x);` **✗**

... code ...

mislabeled good code
as buggy

For decidability, must **abstract**—“model all inputs” (e.g., merge objects)

To address the precision challenge

Traditional program analysis mentality:

“Why can’t developers write more **specifications for our analysis**? Then, we could verify so much more.”

“Since developers won’t write specifications, we will use **default abstractions** (perhaps coarse) that work hopefully most of the time.”

Cooperative approach:

“Can we design program analyses around the user? Developers write testing code. Can we **adapt the analysis** to use those as specifications?”

Summary of overview

Challenge in analysis: Finding a good abstraction
precise enough but not more than necessary

Powerful, generic abstractions
expensive, hard to use and understand

Built-in, default abstractions
often not precise enough (e.g., data structures)

Cooperative approach:

Must involve the user in abstraction
without expecting the user to be a program analysis
expert

Overview of contributions

Extensible Inductive Shape Analysis (Xisa)

Precise inference of data structure properties

Able to check, for instance, the locking example

Targeted to software developers

Uses data structure checking code for guidance

- Turns testing code into a specification for static analysis

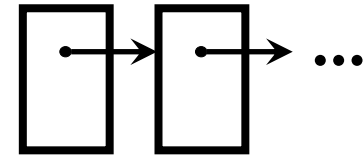
Efficient

- Builds abstraction out of developer-supplied checking code

End-user approach

Extensible Inductive Shape Analysis

Precise inference of
data structure properties

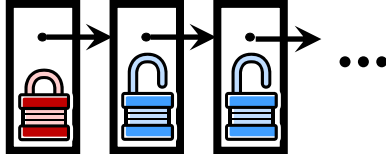


Shape analysis is a fundamental analysis

Precise heap abstraction needed to analyze

- Traditional languages (C, Java)
- Web scripting languages

Improves verifiers that try to

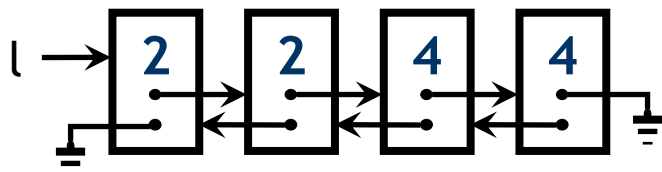
- Eliminate resource usage bugs (locks, file handles) 
- Eliminate memory errors (leaks, dangling pointers)
- Eliminate concurrency errors (data races)
- Validate developer assertions

Enables program transformations

- Compile-time garbage collection
- Data structure refactorings

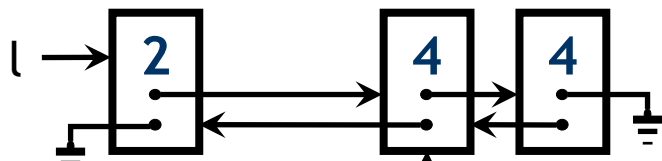
Shape analysis by example: Removing duplicates

Example/Testing

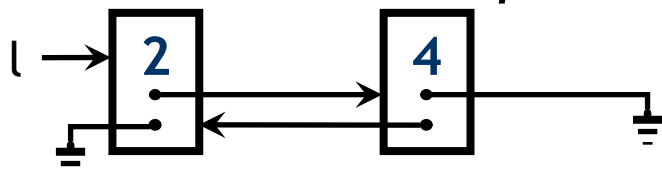


// *l* is a sorted doubly-linked list

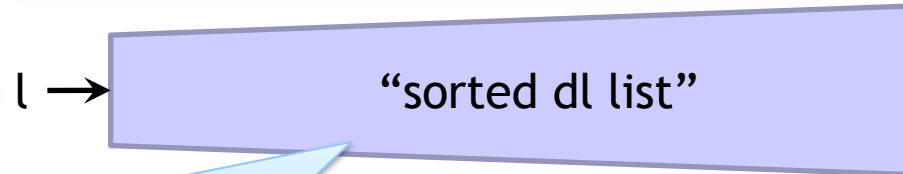
for each node **cur** in list *l* {
 remove **cur** if duplicate;



}
assert *l* is sorted, doubly-linked
with no duplicates;

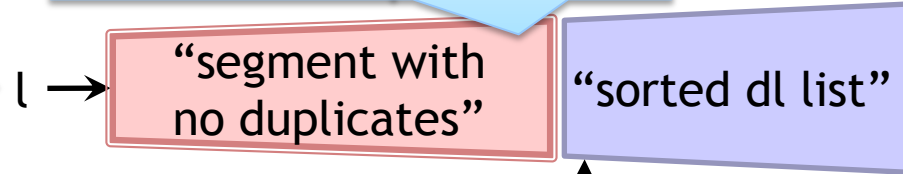


Code Review/Static Analysis



program-specific

intermediate state
more complicated



"segment with
no duplicates"

"sorted dl list"

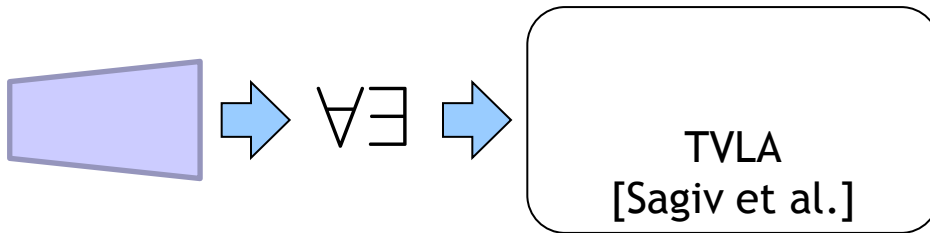


"no duplicates"

Shape analysis is not yet practical

Choosing the heap abstraction difficult for precision

Some representative approaches:



Parametric in low-level,
analyzer-oriented predicates

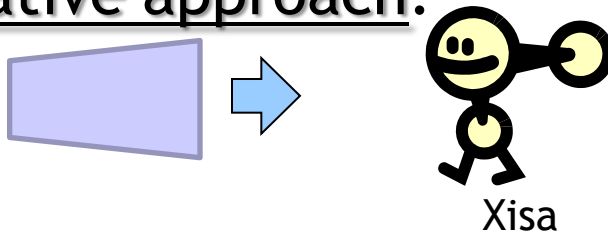
- + Very general and expressive
- Harder for non-expert



Built-in high-level predicates

- Harder to extend
- + No additional user effort (if precise enough)

Cooperative approach:



Parametric in high-level,
developer-oriented predicates

- + Extensible
- + Targeted at developers

Our approach: Executable specifications

Utilize “run-time **checking code**” as specification for static analysis.

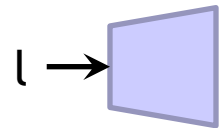
```
h.dll(p) :=  
  h = null  $\wedge$  emp  
 $\vee \exists n. h \neq \text{null} \wedge$   
  h.prev  $\mapsto$  p *  
  h.next  $\mapsto$  n *  
  n.dll(h)
```

checker

- p specifies where prev should point

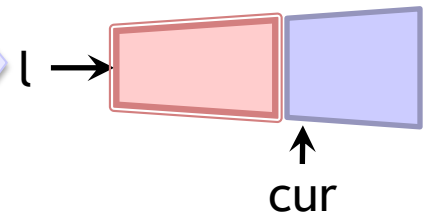
Contribution:

Build the abstraction for analysis out of developer-specified checking code



Contribution:

Generalize checkers for complicated intermediate states



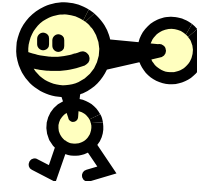
assert(l.sorted_dll_nodup(...)); l \rightarrow

Xisa is ...

An automated **shape analysis** with a precise memory abstraction based around **invariant checkers**.

```
h.dll(p) =  
  if (h = null) then  
    true  
  else  
    h→prev = prev and  
    h→next.dll(h)
```

checkers

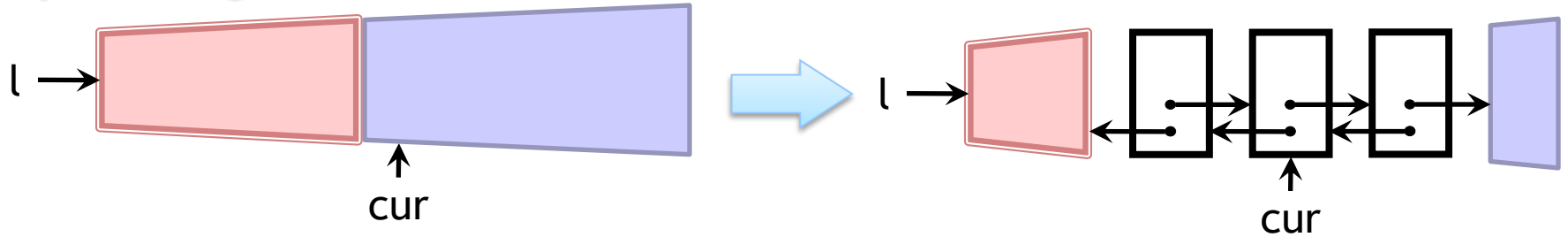


Xisa

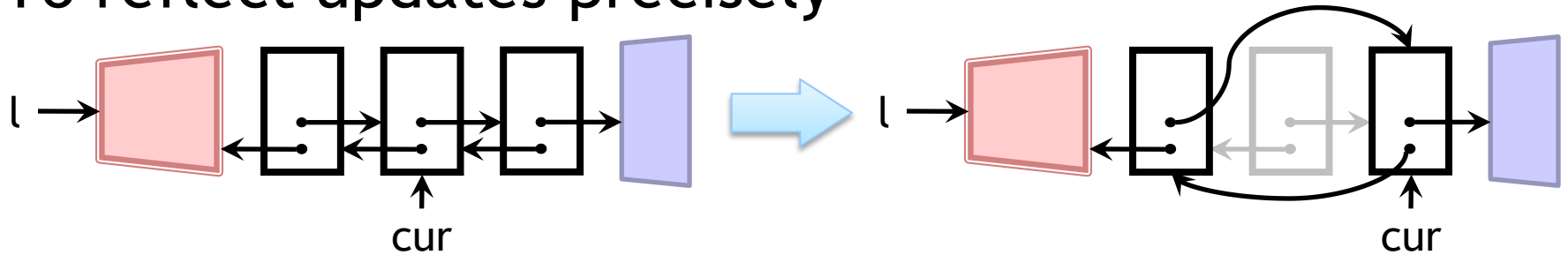
- Extensible and targeted for developers
 - Parametric in developer-supplied checkers—viewed as inductive definitions in separation logic
- Precise yet compact abstraction for efficiency
 - Data structure-specific based on properties of interest to the developer

Shape analysis is an abstract interpretation on abstract memory descriptions with ...

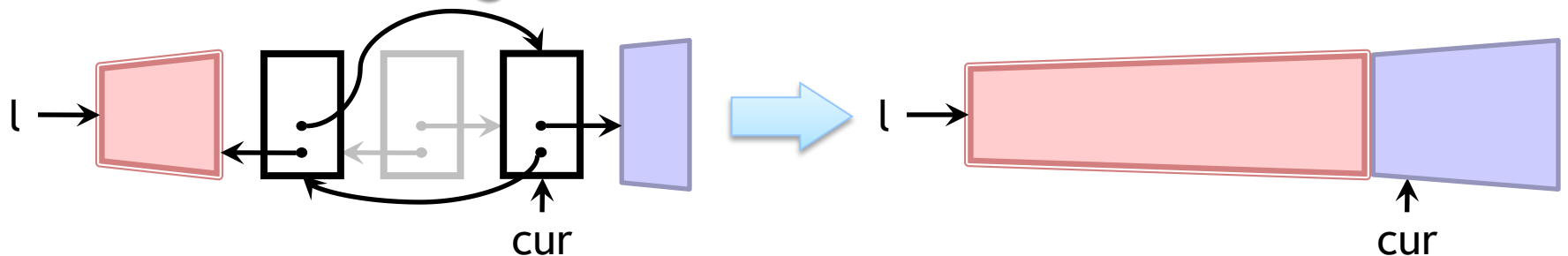
Splitting of summaries (*materialization*)



To reflect updates precisely



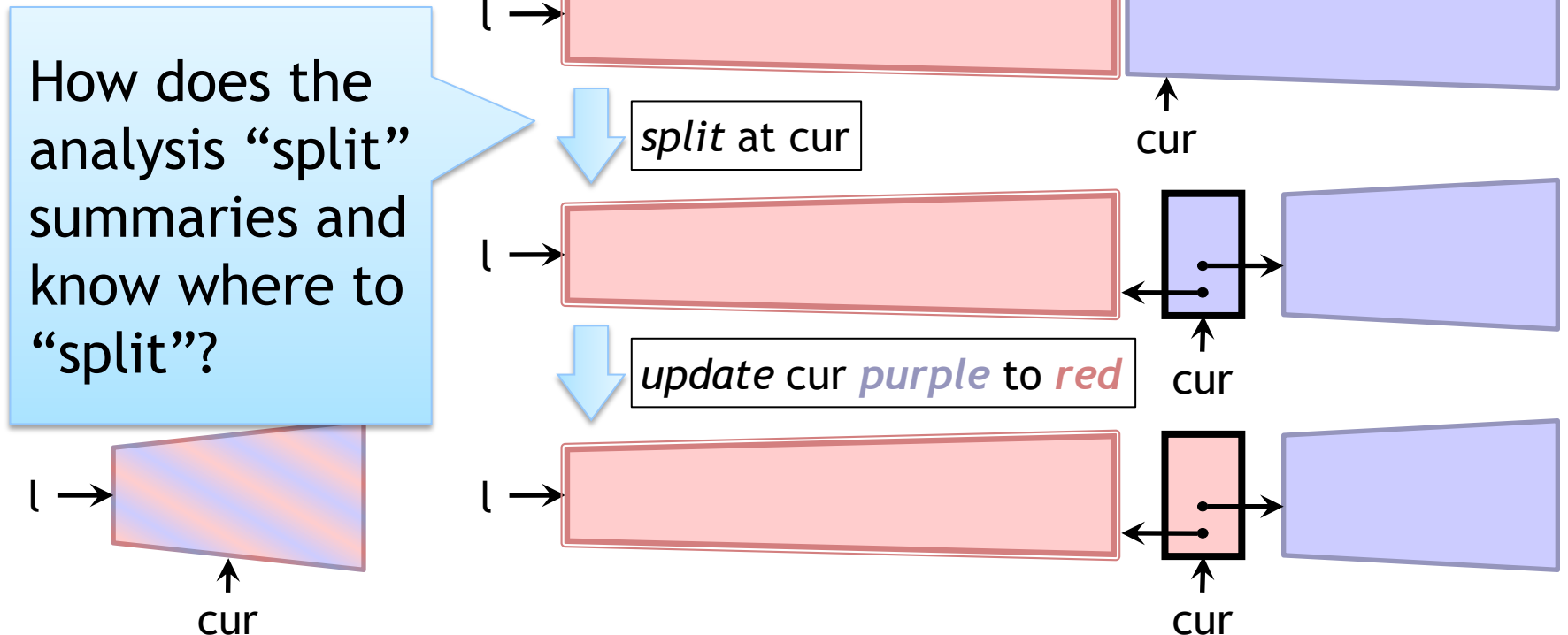
And **summarizing** for termination (*widening*)



Must materialize summaries to interpret updates precisely

Want abstract update to be “exact”, that is, to update one “concrete memory cell”.

The example at a high-level: iterate using **cur** changing the doubly-linked list from *purple* to *red*.



Roadmap: Components of Xisa

checker analysis

program analysis

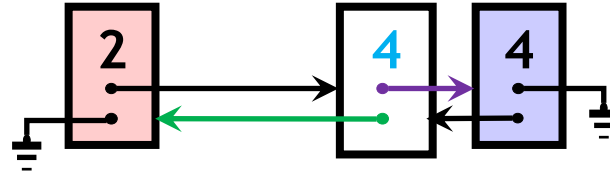
Defining a program analysis:

1. The abstraction (e.g., separation logic formulas with inductive definitions) and operations on the abstraction (e.g., unfolding, update)
2. How to effectively apply the operations (harder!)

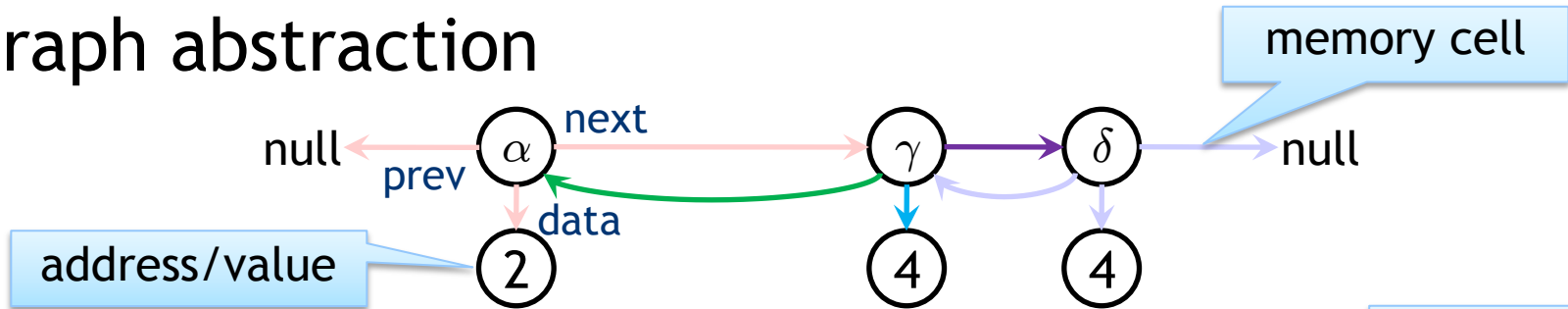
Challenge: Checkers are incomplete specs

Memory abstraction as separating shape graphs

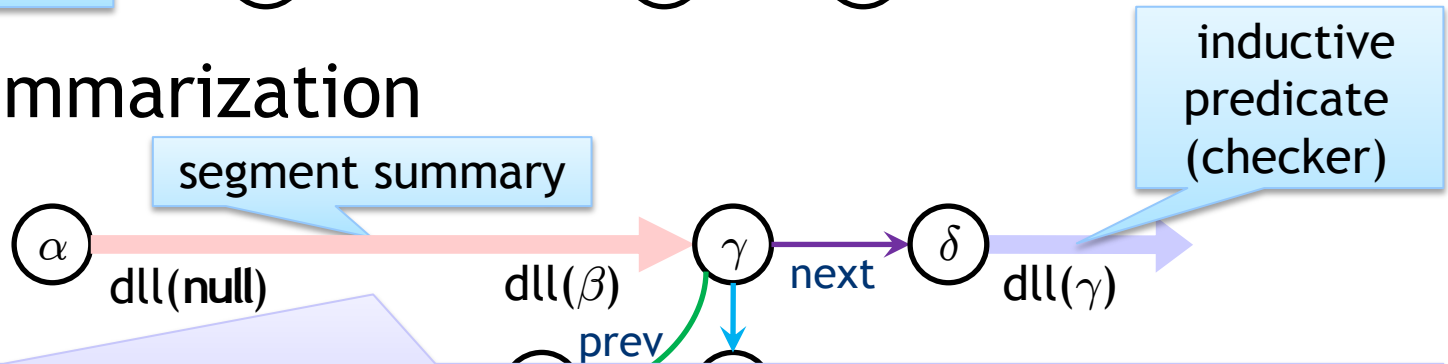
Memory partitioned into regions



Graph abstraction



Region summarization

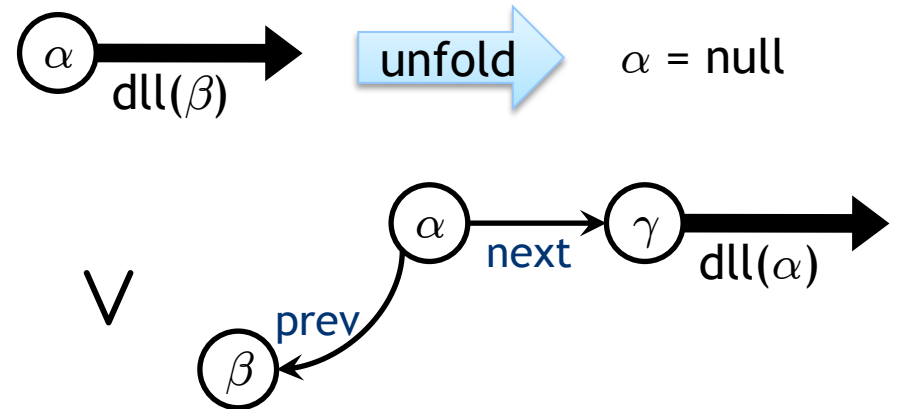


Segment generalization of a checker ($\alpha.dll(\text{null})$ up to $\gamma.dll(\beta)$)

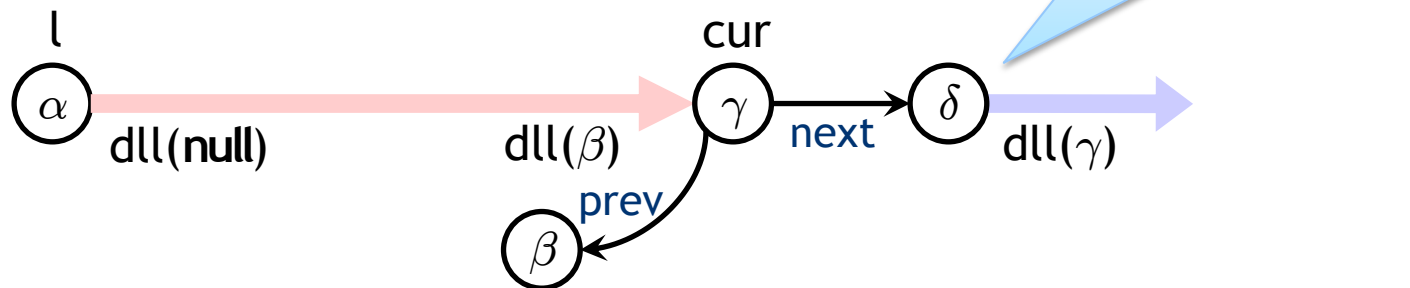
Unfold inductive definitions to split summaries

Definition yields graph unfolding rules

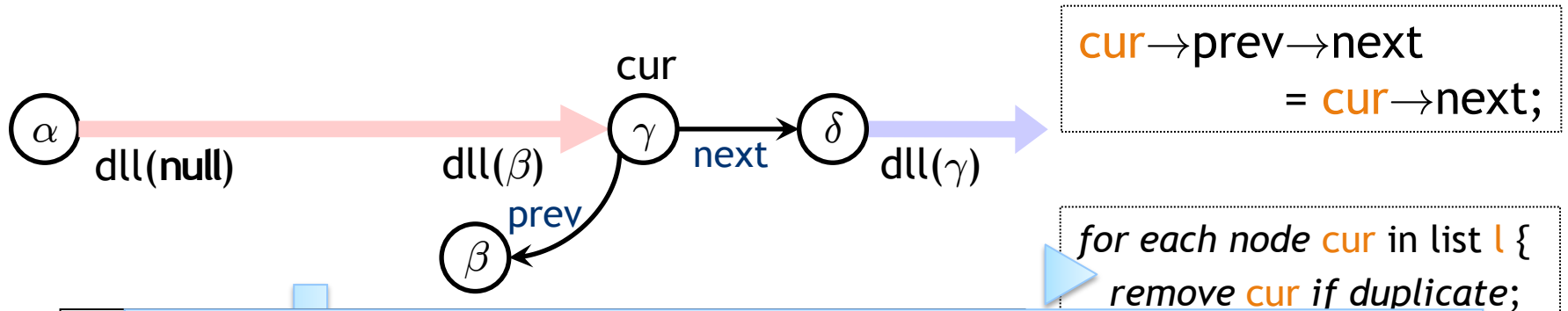
$h.dll(p) :=$
 $h = \text{null} \wedge \text{emp}$
 $\vee \exists n. h \neq \text{null} \wedge$
 $h.\text{prev} \mapsto p *$
 $h.\text{next} \mapsto n *$
 $n.dll(h)$



To *materialize* $cur \rightarrow next \rightarrow next \dots$



Also need a “backwards” unfolding



“b” Technical Details:

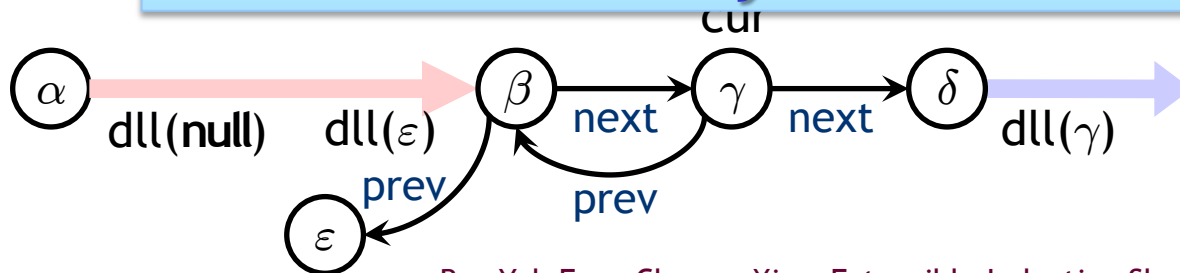
How does the analysis do this unfolding?

Why is this unfolding allowed?

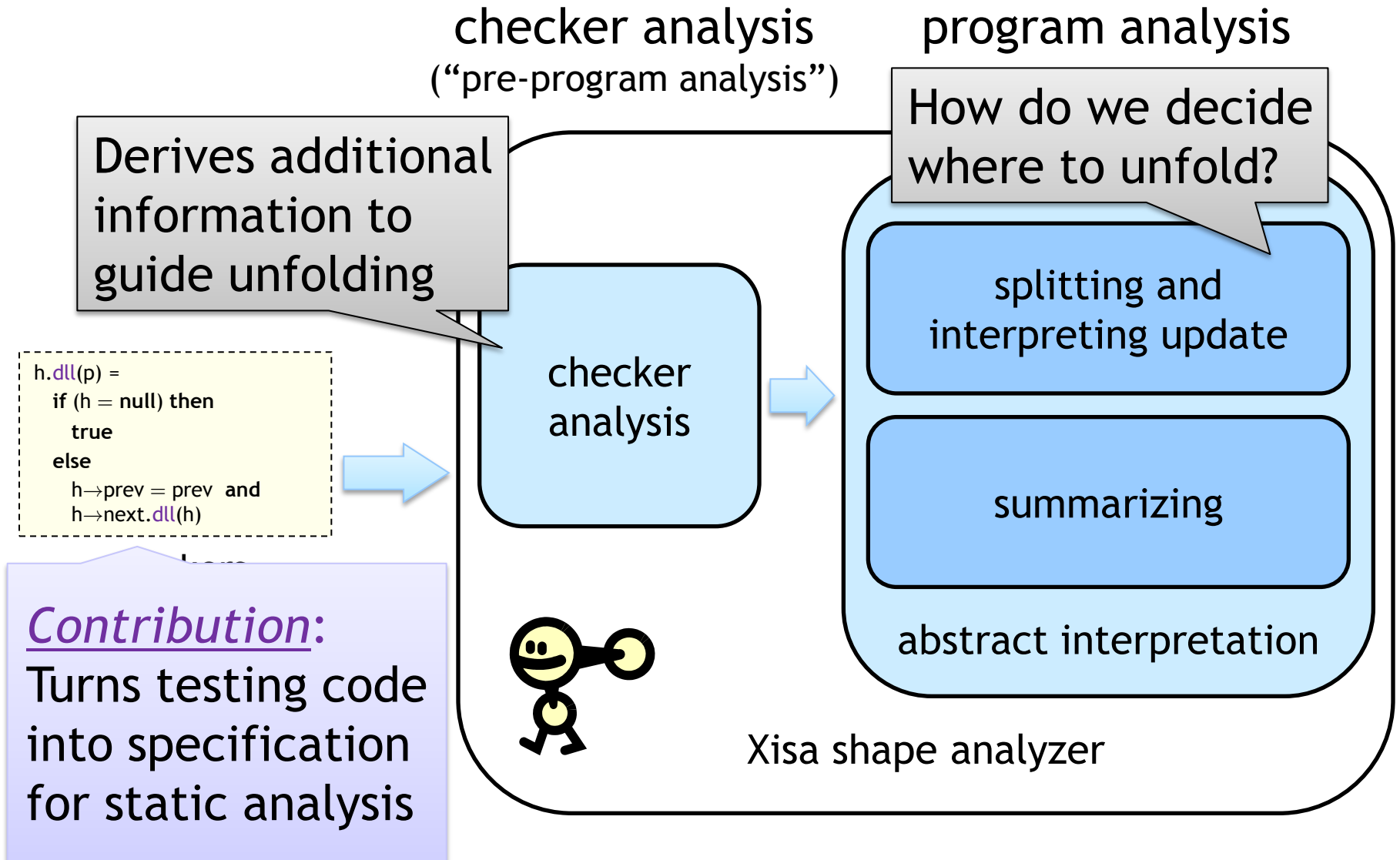
(Key: Segments are also inductively defined)

[POPL'08]

How does the analysis know to do this unfolding?

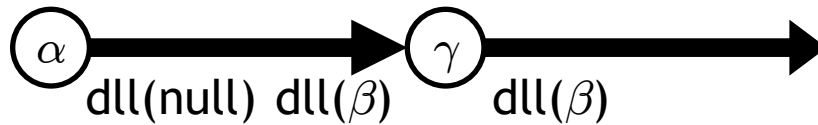


Roadmap: Components of Xisa



Level types for deciding where to unfold

Summary

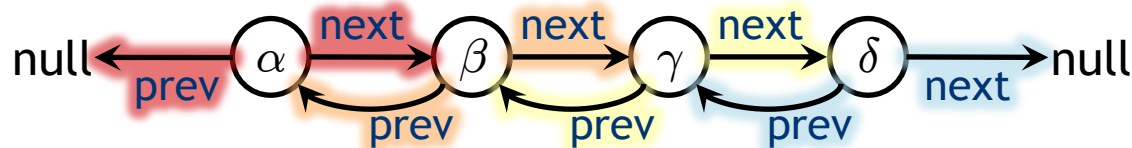


If it exists, where is:

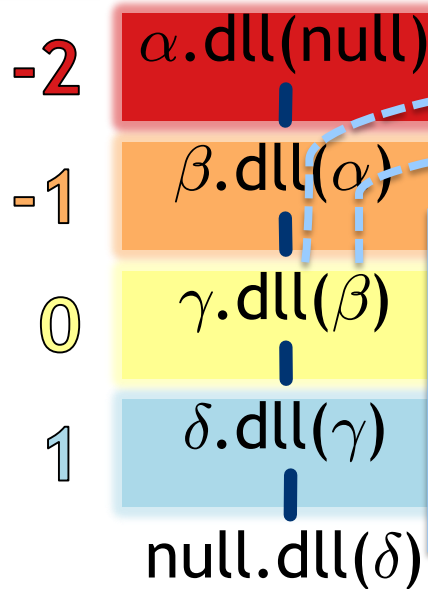
$\gamma \rightarrow \text{next}$? 0

$\beta \rightarrow \text{next}$? -1

Instance



Checker "Run" (call tree/derivation)



Says:

For $h \rightarrow \text{next}/h \rightarrow \text{prev}$,
unfold **from** h

For $p \rightarrow \text{next}/p \rightarrow \text{prev}$,
unfold **before** h

Checker Definition

$h : \{\text{next}\langle 0 \rangle, \text{prev}\langle 0 \rangle\}$
 $p : \{\text{next}\langle -1 \rangle, \text{prev}\langle -1 \rangle\}$

$h.dll(p) =$

if $(h = \text{null})$ then
true

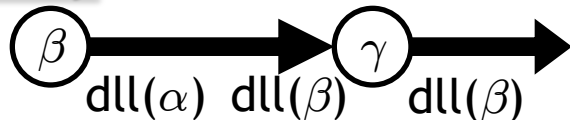
else

$h \rightarrow \text{prev} = p$ and
 $h \rightarrow \text{next}.dll(h)$

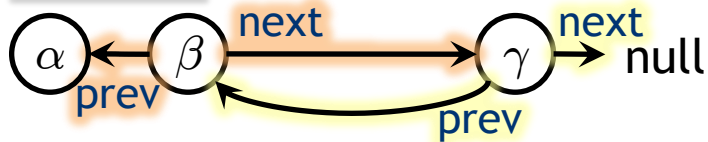
Level types make the analysis robust with respect to how checkers are written

Doubly-linked list checker (as before)

Summary



Instance

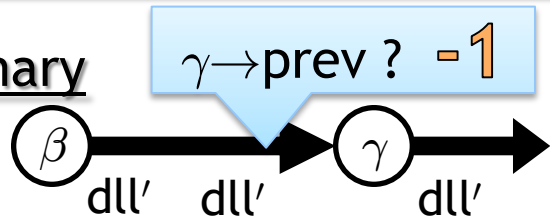


```

h: {next<0>, prev<0>}
p: {next<-1>, prev<-1>}
h.dll(p) =
  if (h = null) then
    true
  else
    h->prev = p and
    h->next.dll(h)
    
```

Alternative doubly-linked list checker

Summary



Instance



Different types for different unfolding

```

h: {next<0>, prev<-1>}
h.dll'() =
  if (h->next = null) then
    true
  else
    h->next->prev = h
    and h->next.dll'()
    
```

Summary of checker parameter types

Tell **where** to unfold for **which** fields

Make analysis **robust** with respect to how checkers are written

Learn where in summaries unfolding won't help

Can be **inferred automatically** with a fixed-point computation on the checker definitions

Summary of interpreting updates

Splitting of summaries needed for precision

Unfolding checkers is a natural way to do splitting

When checker traversal matches code traversal

Checker parameter type analysis

Useful for guiding unfolding in difficult cases, for example, “back pointer” traversals

Roadmap: Components of Xisa

checker analysis
("pre-program analysis")

program analysis

```
h.dll(p) =  
  if (h = null) then  
    true  
  else  
    h→prev = prev and  
    h→next.dll(h)
```

checkers



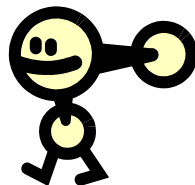
checker
analysis



splitting and
interpreting update

summarizing

abstract interpretation



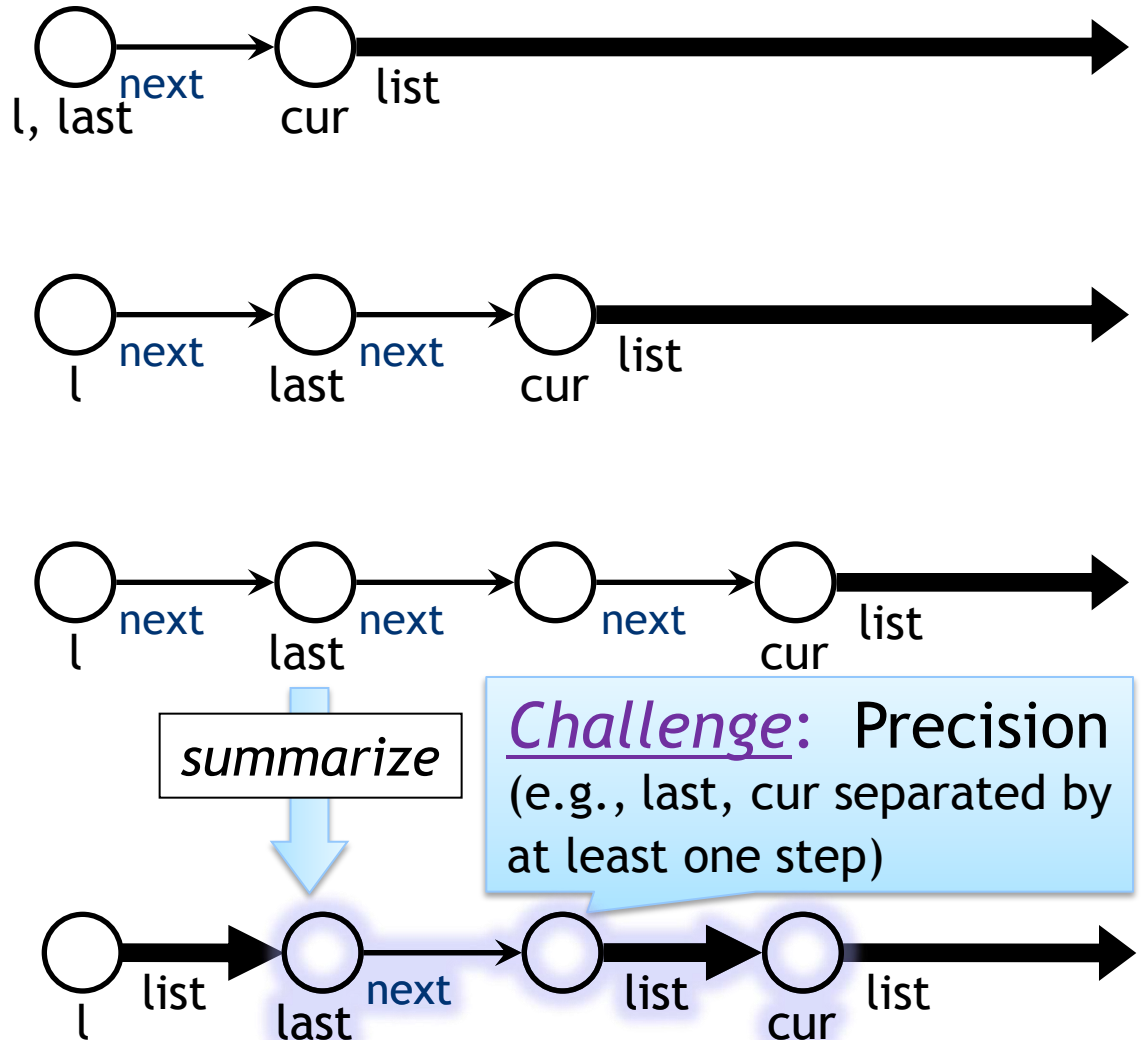
Xisa shape analyzer

Summarize by folding into inductive predicates

```
last = l;  
cur = l → next;  
while (cur != null) {  
  // ... cur, last ...  
  if (...) last = cur;  
  cur = cur → next;  
}
```

Previous approaches
guess where to fold
for each graph.

Contribution:
Determine where by
comparing graphs
across history



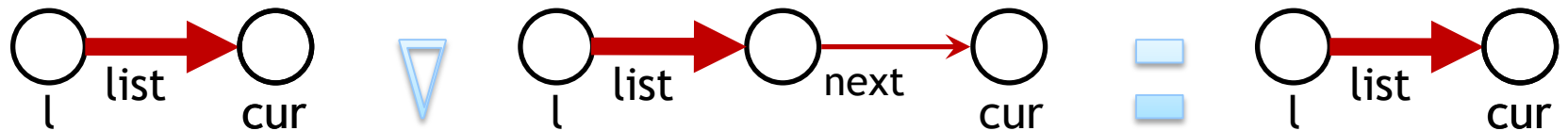
Challenge: Precision
(e.g., last, cur separated by
at least one step)

Use iteration history with a widening operator

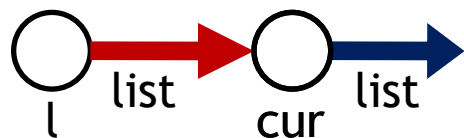
Match regions



Apply local **weakening** rules on each region



Widened result



Given checkers, everything is automatic

checker analysis
("pre-program analysis")

program analysis

```
h.dll(p) =  
if (h = null) then  
  true  
else  
  h→prev = prev and  
  h→next.dll(h)
```

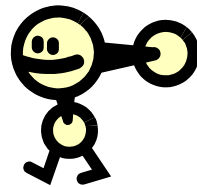
checkers

checker
analysis

splitting and
interpreting update

summarizing

abstract interpretation



Xisa shape analyzer

Results: Performance

Times negligible for data structure operations (often in sec or $1/_{10}$ sec)

Expressiveness:
Different data structures

Benchmark	Max. Num. Graphs at a Program Pt	Analysis Time (ms)
singly-linked list reverse	1	TVLA: 290 ms → 1.0
doubly-linked list reverse	<div style="border: 1px solid black; padding: 5px; text-align: center;"> <i>Space Invader</i> only analyzes lists (built-in) </div>	1.5
doubly-linked list copy		5.4
doubly-linked list remove		17.9
doubly-linked list remove and back		18.1
search tree with parent insert		TVLA: 850 ms → 16.6
search tree with parent insert and back	5	64.7
two-level skip list rebalance	1	11.7
Linux <code>scull</code> driver (894 loc) (char arrays ignored, functions inlined)	4	3969.6

Verified shape invariant as given by the checker is preserved across the operation.

Demo: Doubly-linked list reversal

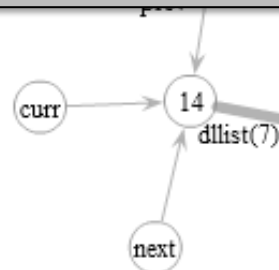
← → ↻ × 🏠 <http://xisa.cs.berkeley.edu/demo/examples/dll.reverse.inv/dll.reverse.html>

memory state

```
prev = curr->prev;  
next = curr->next;
```

Body of loop over the elements:

Ongoing Undergraduate Project:
Better memory visualization
+ Eclipse integration
+ User study



Not yet reversed list

<http://xisa.cs.colorado.edu/>

Summary of Xisa: Extensible Inductive Shape Analysis

Key Insight: Checkers as specifications

Developer View: Global, Expressed in a familiar style

Analysis View: Capture developer intent,
Not arbitrary inductive definitions

Constructing the program analysis

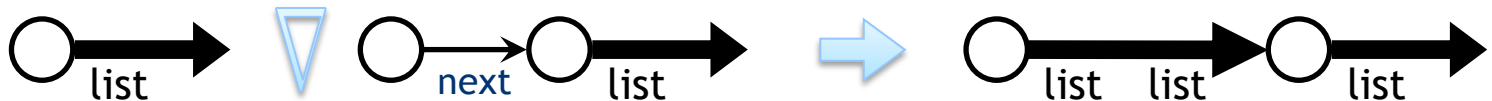
Intermediate states: **Generalized segment** predicates



Splitting: Checker parameter **types with levels**

$h : \{\text{next}\langle 0 \rangle, \text{prev}\langle 0 \rangle\}$ $p : \{\text{next}\langle -1 \rangle, \text{prev}\langle -1 \rangle\}$

Summarizing: **History-guided** approach with widening op



Subsequent Work

- C-Level Memory Abstraction [ESOP'10]
 - Separating shape graphs support **mixing high-level** (e.g., record fields) and **low-level** (e.g., union fields) memory abstractions
- “Very Context-Sensitive” Interprocedural Analysis [POPL'11]
 - Whole program, state-based interprocedural analysis using Xisa
 - Make **call stack** explicit and **summarize using shape** invariants

Future work:

Exploiting common specification framework

Scenario: Code instrumented with lots of checker calls
(perhaps automatically with object invariants)

```
assert( mychecker(x) );  
// ... operation on x ...  
assert( mychecker(x) );
```

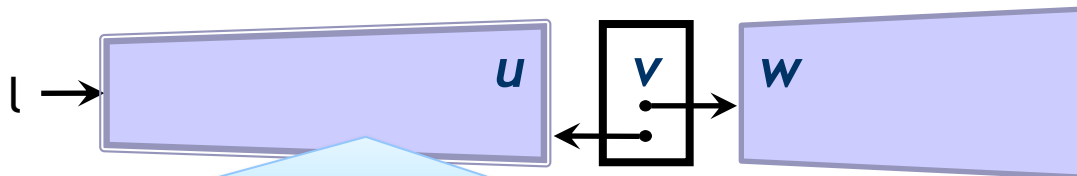
- Very slow to execute
- Hard to prove statically (in general)

Can we prove **parts** statically?

Static Analysis View: Hybrid checking

Testing View: Incrementalize invariant checking

Example: Insert in a sorted list



Preservation of sortedness shown statically

Emit run-time check for new element: $u \leq v \leq w$

Conclusion

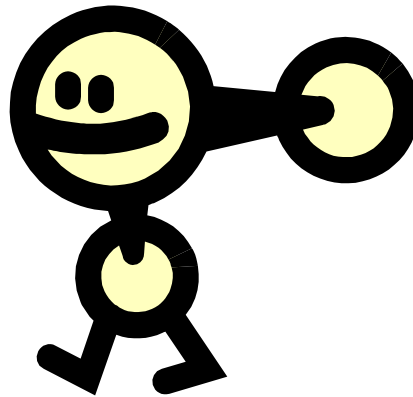
Extensible Inductive Shape Analysis

precision demanding program analysis
improved by novel user interaction

Developer: Gets results corresponding to intuition

Analysis: Focused on what's important to the developer

Practical precise tools for better software
with a cooperative approach!



*What can inductive
shape analysis do for you?*

<http://xisa.cs.colorado.edu>