

# C280, Computer Vision

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Lecture 15: Part-based models

# Last Lecture: Discriminative Kernels

- SVM-BOW
- Pyramid and Spatial-Pyramid match
- Fast Intersection Kernels
- Latent-part SVM models

# Recognition Lectures Summary

- Tues. 10/13: Introduction to Recognition
  - Scanning window paradigm
  - GIST
  - HOG
  - Boosted Face Detection
  - Local-feature Alignment; from Roberts to Lowe...
  - BOW Indexing
- Thurs. 10/15: Topic models for Recognition
  - Topic models for category discovery [Sivic05]
  - Category discovery from web [Fergus05]
  - Bootstrapping a category model [Li07]
  - Using text in addition to image [Berg06]
  - Learning objects from a dictionary [Saenko08]
- Tues. 10/20: Discriminative Kernels
  - SVM-BOW
  - Pyramid and Spatial-Pyramid match
  - Fast Intersection Kernels
  - Latent-part SVM models
- Thurs. 10/22: Voting and Part Based Models
  - Naïve-Bayes Nearest Neighbor [Irani]
  - Implicit Shape Model (ISM)
  - Constellation Models
  - Transformed LDA Models [Sudderth]
  - 3-D view models [Saravese]

# Today

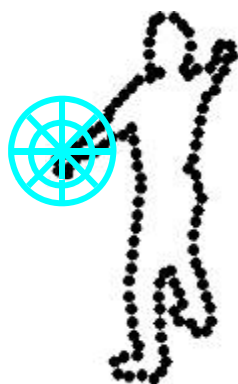
- Naïve-Bayes Nearest Neighbor (Irani)
- ISM (Liebe)
- Constellation Models (Fergus)
- Transformed LDA Models (Sudderth)
- 3-D view models (Saravese)

# Multiple Features...

Wide variety of proposed local feature representations:



SIFT [Lowe]



Shape context  
[Belongie et al.]



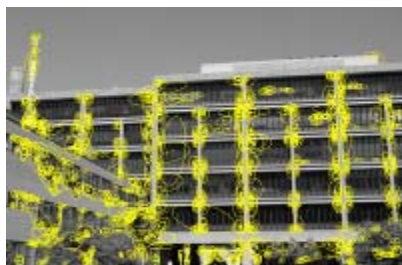
Superpixels [Ren  
et al.]



Maximally Stable Extremal  
Regions [Matas et al.]



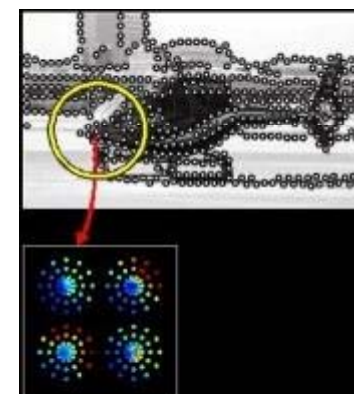
Salient regions  
[Kadir et al.]



Harris-Affine  
[Schmid et al.]



Spin images  
[Johnson and  
Hebert]



Geometric Blur  
[Berg et al.]

# Discriminative Paradigm: Learning the Kernel

---

- Learn the kernel parameters
  - Improve accuracy and generalisation
  - Perform feature component selection
  - Perform dimensionality reduction
- Learn a linear combination of base kernels
  - $K(\mathbf{x}_i, \mathbf{x}_j) = \sum_k d_k K_k(\mathbf{x}_i, \mathbf{x}_j)$
  - Combine heterogeneous sources of data
  - Perform feature selection

# Gaussian Processes for Object Categorization

Ashish Kapoor · Kristen Grauman · Raquel Urtasun · Trevor Darrell

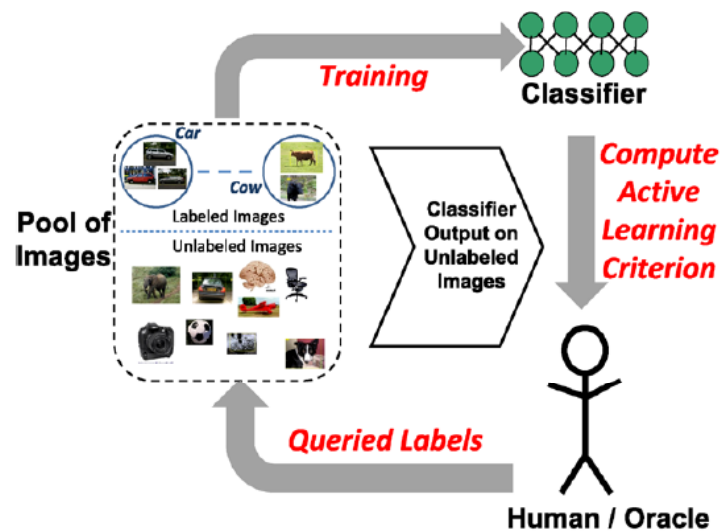


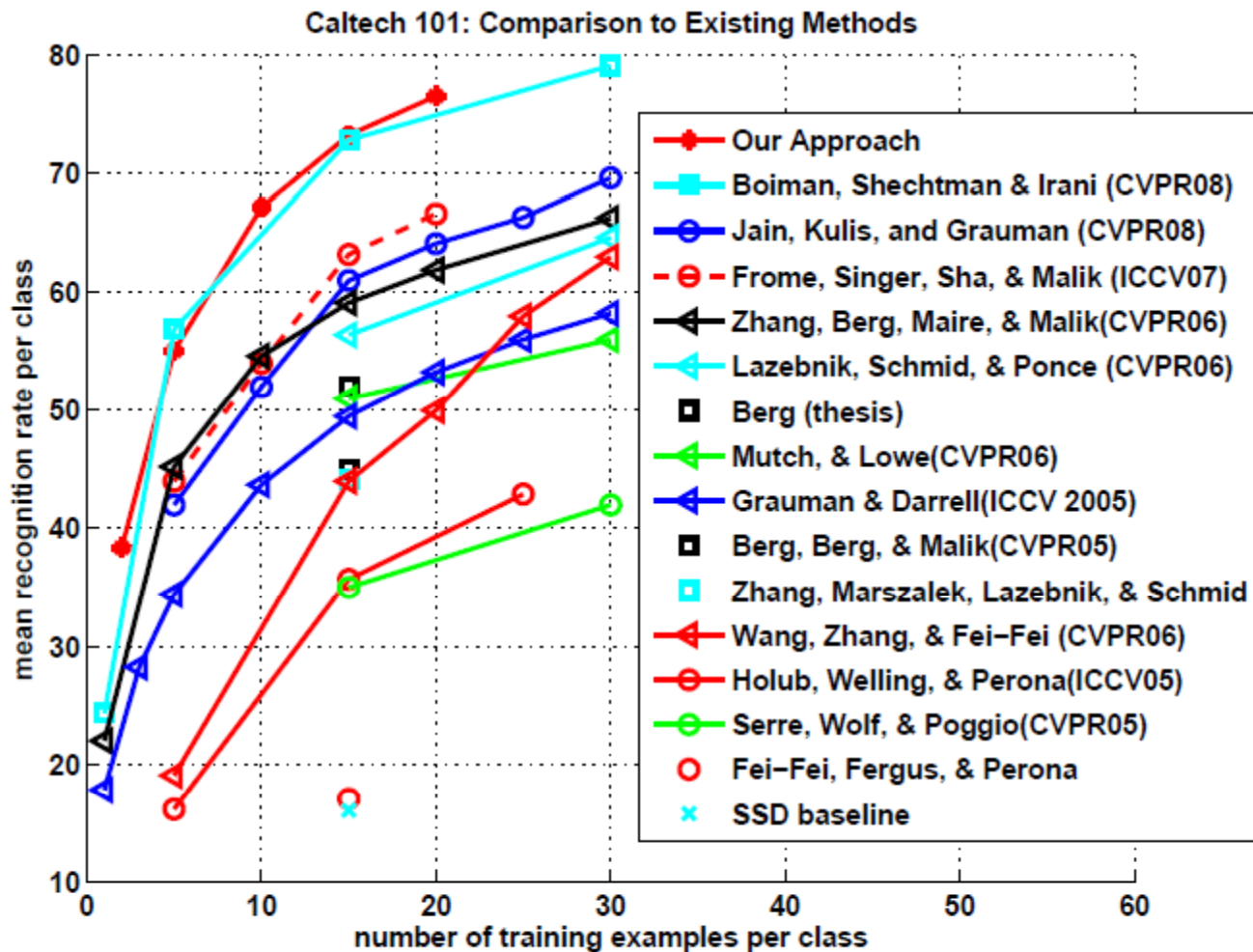
Fig. 1 The active learning framework. The goal of the system is to query labels for images that are most useful in training

$$\mathbf{K} = \sum_{i=1}^k \alpha_i \mathbf{K}^{(i)},$$

2. Kernel weights and kernel hyperparameters can be efficiently learned in a 1-vs-all setting (vs. SVM MKL)

1. GP uncertainty model facilitates active learning

# The power of discriminative kernels?





# In Defense of Nearest-Neighbor Based Image Classification

Oren Boiman

The Weizmann Institute of Science  
Rehovot, ISRAEL

Eli Shechtman

Adobe Systems Inc. &  
University of Washington

Michal Irani

The Weizmann Institute of Science  
Rehovot, ISRAEL

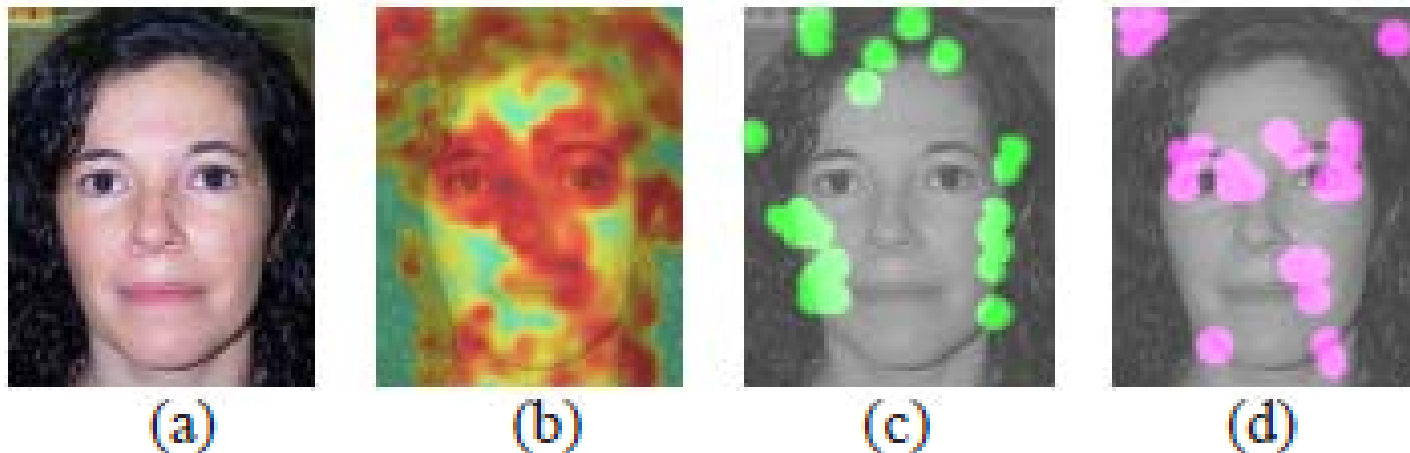
## Abstract

*State-of-the-art image classification methods require an intensive learning/training stage (using SVM, Boosting, etc.) In contrast, non-parametric Nearest-Neighbor (NN) based image classifiers require no training time and have other favorable properties. However, the large performance gap between these two families of approaches rendered NN-based image classifiers useless.*

*We claim that the effectiveness of non-parametric NN-based image classification has been considerably undervalued. We argue that two practices commonly used in image classification methods, have led to the inferior performance of NN-based image classifiers: (i) Quantization of local image descriptors (used to generate “bags-of-words”, codebooks). (ii) Computation of ‘Image-to-Image’ distance, instead of ‘Image-to-Class’ distance.*

*We propose a trivial NN-based classifier – NBNN, (Naive-Bayes Nearest-Neighbor), which employs NN-distances in the space of the local image descriptors (and not in the space of images). NBNN computes direct ‘Image-to-Class’ distances without descriptor quantization. We further show that under the Naive-Bayes assumption, the theoretically optimal image classifier can be accurately approximated by NBNN.*

*Although NBNN is extremely simple, efficient, and requires no learning/training phase, its performance ranks among the top leading learning-based image classifiers. Empirical comparisons are shown on several challenging databases (Caltech-101, Caltech-256 and Graz-01).*



**Figure 1. Effects of descriptor quantization – Informative descriptors have low database frequency, leading to high quantization error.** (a) *An image from the Face class in Caltech101.* (b) *Quantization error of densely computed image descriptors (SIFT) using a large codebook (size 6,000) of Caltech101 (generated using [14]). Red = high error; Blue = low error. The most informative descriptors (eye, nose, etc.) have the highest quantization error.* (c) *Green marks the 8% of the descriptors in the image that are most frequent in the database (simple edges).* (d) *Magenta marks the 8% of the descriptors in the image that are least frequent in the database (mostly facial features).*

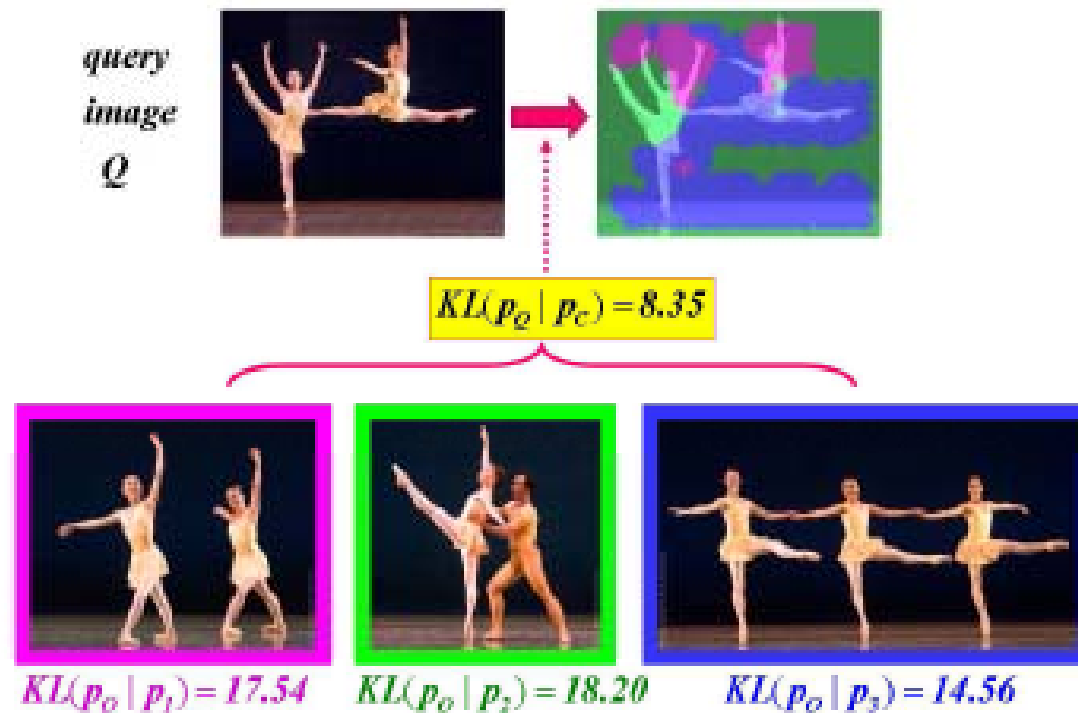
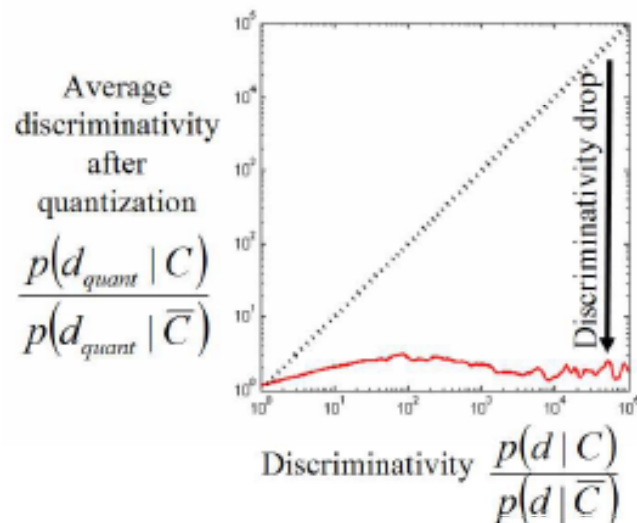
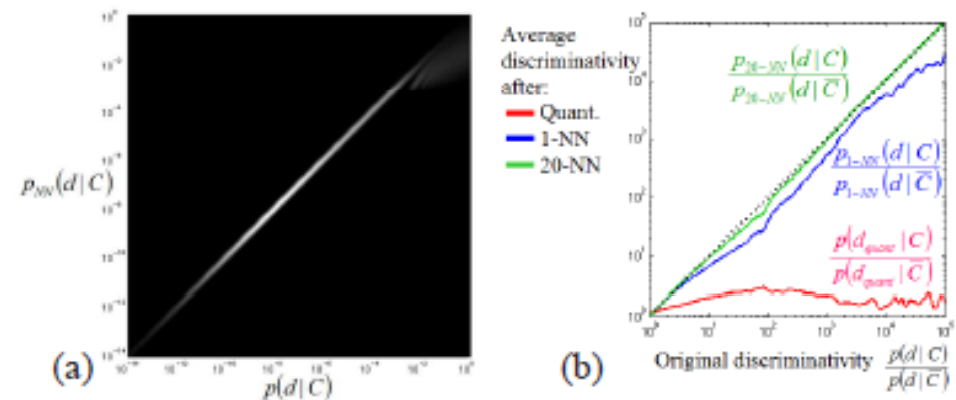


Figure 3. “Image-to-Image” vs. “Image-to-Class” distance. A Ballet class with large variability and small number (three) of ‘labelled’ images (bottom row). Even though the “Query-to-Image” distance is large to each individual ‘labelled’ image, the “Query-to-Class” distance is small. **Top right image:** For each descriptor at each point in  $Q$  we show (in color) the ‘labelled’ image which gave it the highest descriptor likelihood. It is evident that the new query configuration is more likely given the three images, than each individual image separately. (Images taken from [4].)



**Figure 2. Effects of descriptor quantization – Severe drop in descriptor discriminative power.** We generated a scatter plot of descriptor discriminative power before and after quantization (for a very large sample set of SIFT descriptors  $d$  in Caltech-101, each for its respective class  $C$ ). We then averaged this scatter plot along the y-axis. This yields the “Average discriminative power after quantization” (the RED graph). The display is in logarithmic scale in both axes. NOTE: The more informative (discriminative) a descriptor  $d$  is, the larger the drop in its discriminative power.



**Figure 4. NN descriptor estimation preserves descriptor density distribution and discriminativity.** (a) A scatter plot of the 1-NN probability density distribution  $p_{1-NN}(d|C)$  vs. the true distribution  $p(d|C)$ . Brightness corresponds to the concentration of points in the scatter plot. The plot shows that 1-NN distribution provides a very accurate approximation of the true distribution. (b) 20-NN descriptor approximation (Green graph) and 1-NN descriptor approximation (Blue graph) preserve quite well the discriminative power of descriptors. In contrast, descriptor quantization (Red graph) severely reduces discriminative power of descriptors. Displays are in logarithmic scale in all axes.

# NBNN

## The NBNN Algorithm:

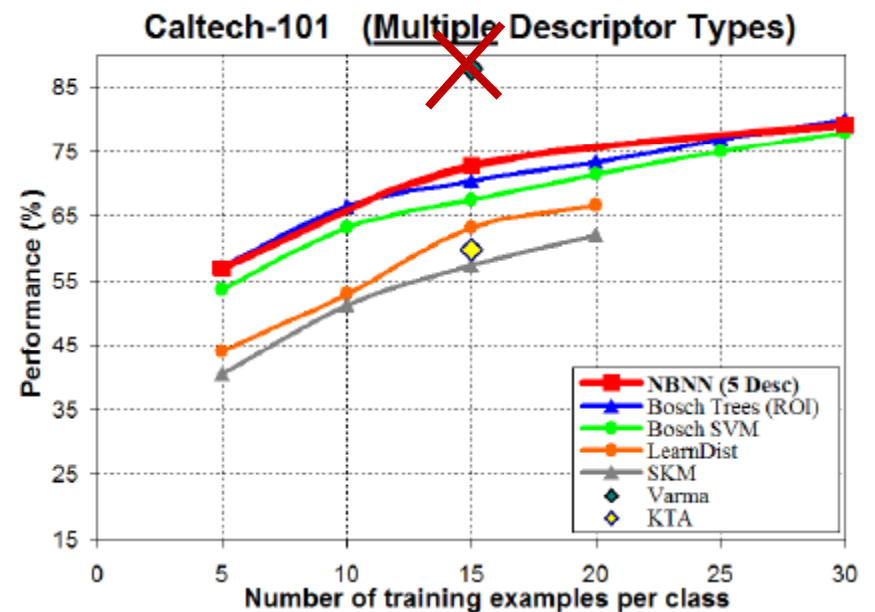
1. Compute descriptors  $d_1, \dots, d_n$  of the query image  $Q$ .
2.  $\forall d_i \forall C$  compute the NN of  $d_i$  in  $C$ :  $\text{NN}_C(d_i)$ .
3.  $\hat{C} = \arg \min_C \sum_{i=1}^n \| d_i - \text{NN}_C(d_i) \|^2$ .

with multiple feature types:

$$\hat{C} = \arg \min_C \sum_{j=1}^t w_j \cdot \sum_{i=1}^n \| d_i^j - \text{NN}_C(d_i^j) \|^2,$$

NN-based method	Performance
SPM NN Image [27]	42.1 ± 0.81%
GBDist NN Image [27]	45.2 ± 0.96%
GB Vote NN [3]	52%
SVM-KNN [30]	59.1 ± 0.56%
<b>NBNN (1 Desc)</b>	<b>65.0 ± 1.14%</b>
<b>NBNN (5 Desc)</b>	<b>72.8 ± 0.39%</b>

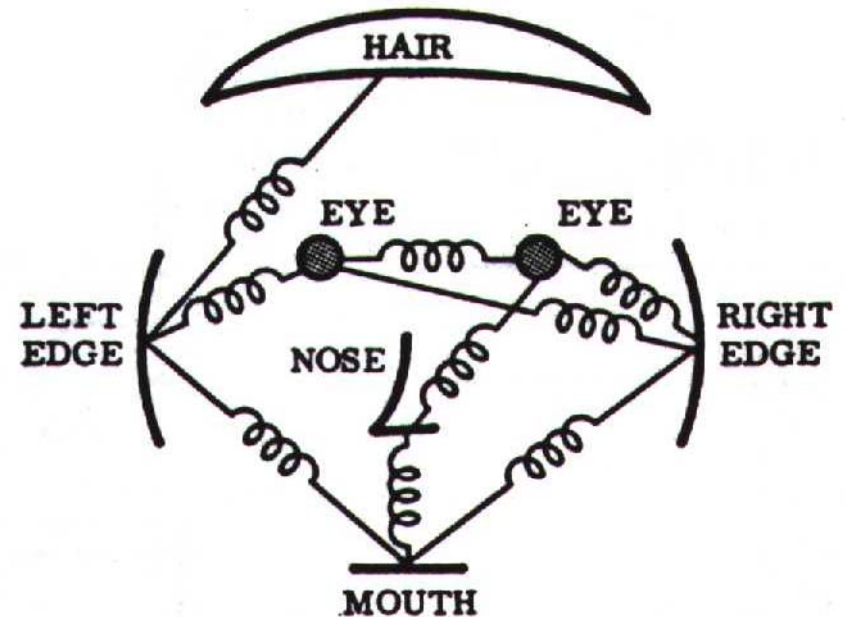
Table 1. Comparing the performance of non-parametric NN-based approaches on the Caltech-101 dataset ( $n_{label} = 15$ ). All the listed methods do not require a learning phase.



Bosch Kernels used in original Varma paper have been withdrawn...

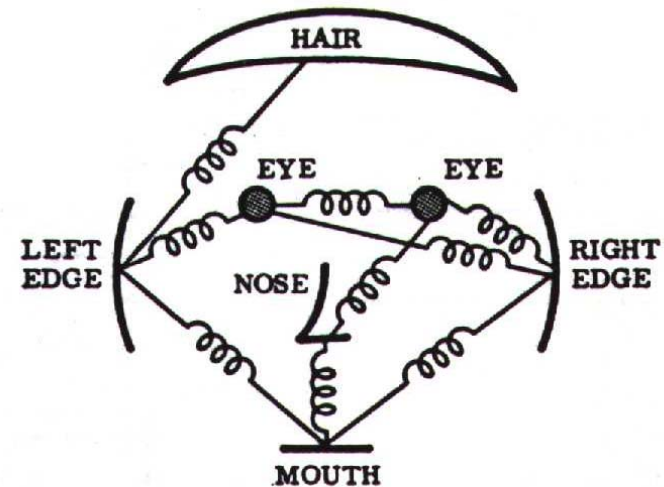
# Back to shape: Parts-based Representation

- ⊙ Object as set of parts
  - ⊙ Generative representation
- ⊙ Model:
  - ⊙ Relative locations between parts
  - ⊙ Appearance of part
- ⊙ Issues:
  - ⊙ How to model location
  - ⊙ How to represent appearance
  - ⊙ Sparse or dense (pixels or regions)
  - ⊙ How to handle occlusion/clutter



# History of Parts and Structure approaches

- Fischler & Elschlager 1973
- Yuille '91
- Brunelli & Poggio '93
- Lades, v.d. Malsburg et al. '93
- Cootes, Lanitis, Taylor et al. '95
- Amit & Geman '95, '99
- Perona et al. '95, '96, '98, '00, '03, '04, '05
- Felzenszwalb & Huttenlocher '00, '04
- Crandall & Huttenlocher '05, '06
- Leibe & Schiele '03, '04
- Many papers since 2000

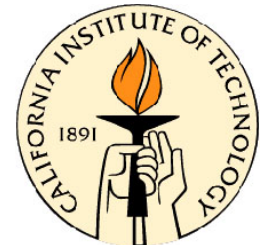




# Object class recognition using unsupervised scale-invariant learning

Rob Fergus  
Pietro Perona  
Andrew Zisserman

Oxford University  
California Institute of Technology



Slide credit: Fergus

# Goal

- Recognition of object categories
- Unassisted learning



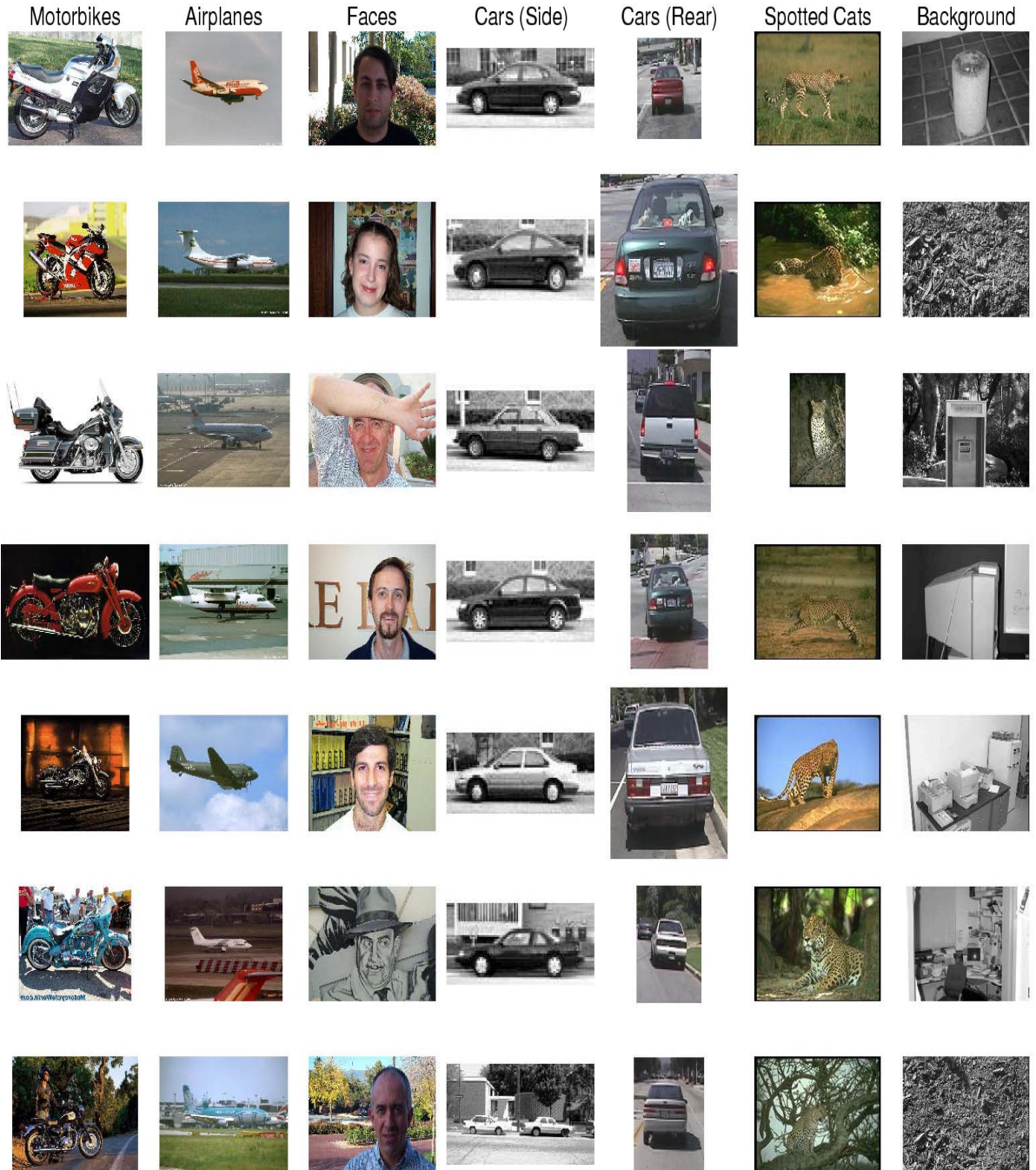
Slide credit: Fergus

# Some object categories

Learn from examples

Difficulties:

- Size variation
- Background clutter
- Occlusion
- Intra-class variation

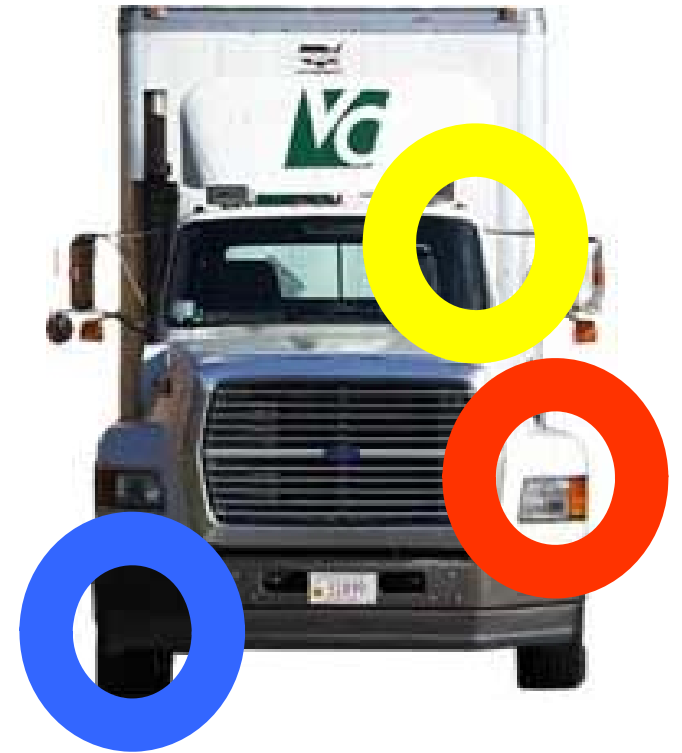


# Main issues

- **Representation**
- Learning
- Recognition

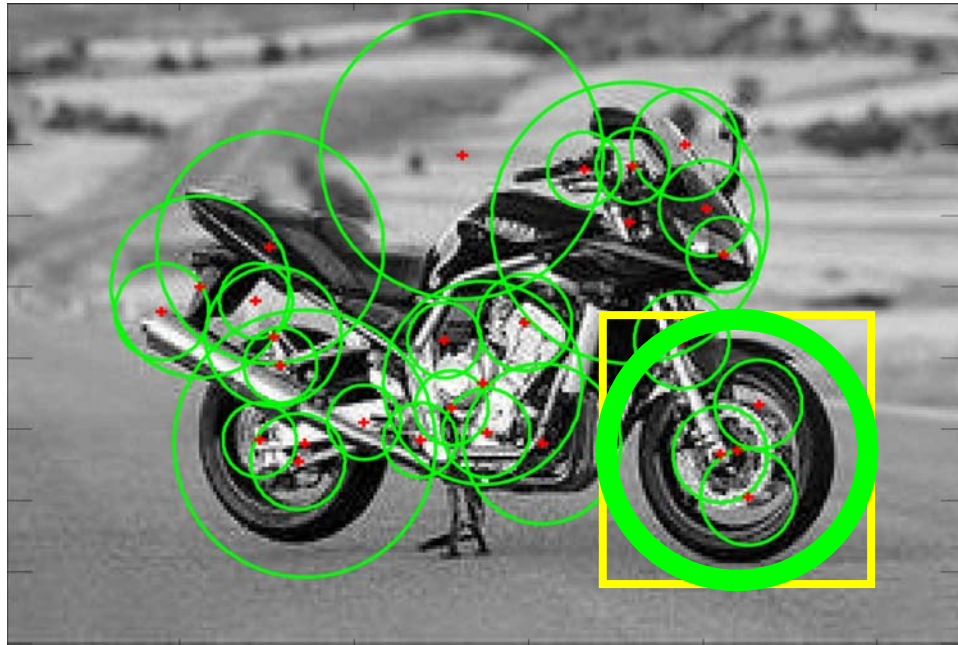
# Sparse representation

- + Computationally tractable ( $10^5$  pixels  $\rightarrow$   $10^1$  --  $10^2$  parts)
- + Generative representation of class
- + Avoid modeling global variability
- + Success in specific object recognition



- Throw away most image information
  - Parts need to be distinctive to separate from other classes
- Slide credit: Fergus

# Detection & Representation of regions



- Find regions within image
- Use Kadir and Brady's salient region operator [IJCV '01]

## Location

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(x,y) coords. of region center

## Scale

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Diameter of region (pixels)

## Appearance

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Gives representation of appearance in low-dimensional vector space

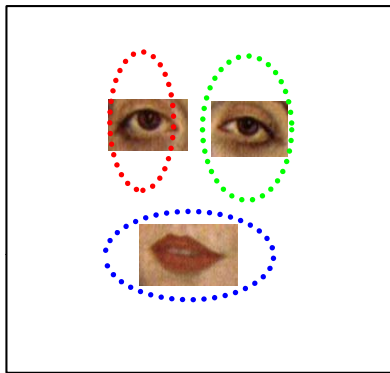
Slide credit: Fergus

# Generative probabilistic model

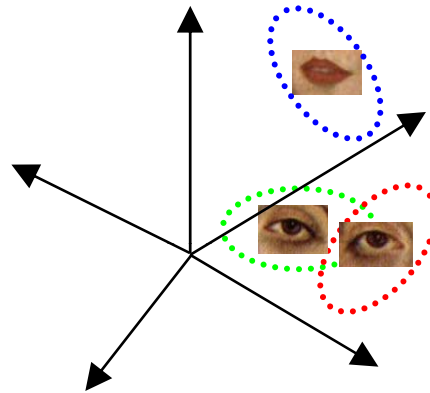
## Foreground model

based on Burl, Weber et al. [ECCV '98, '00]

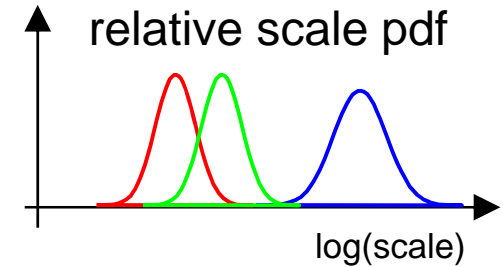
Gaussian shape pdf



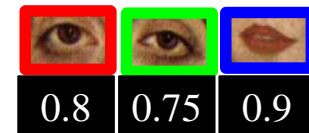
Gaussian part appearance pdf



Gaussian relative scale pdf

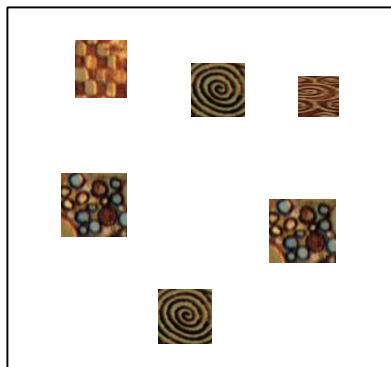


Prob. of detection

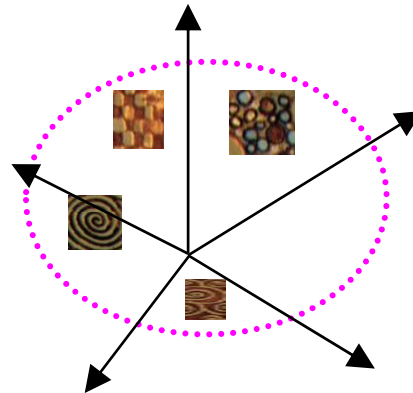


## Clutter model

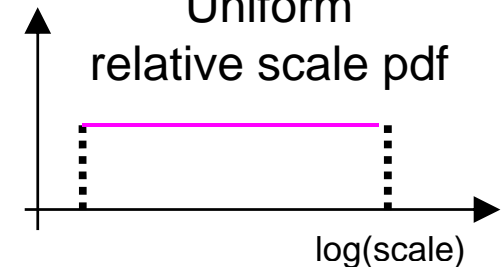
Uniform shape pdf



Gaussian background appearance pdf



Uniform relative scale pdf

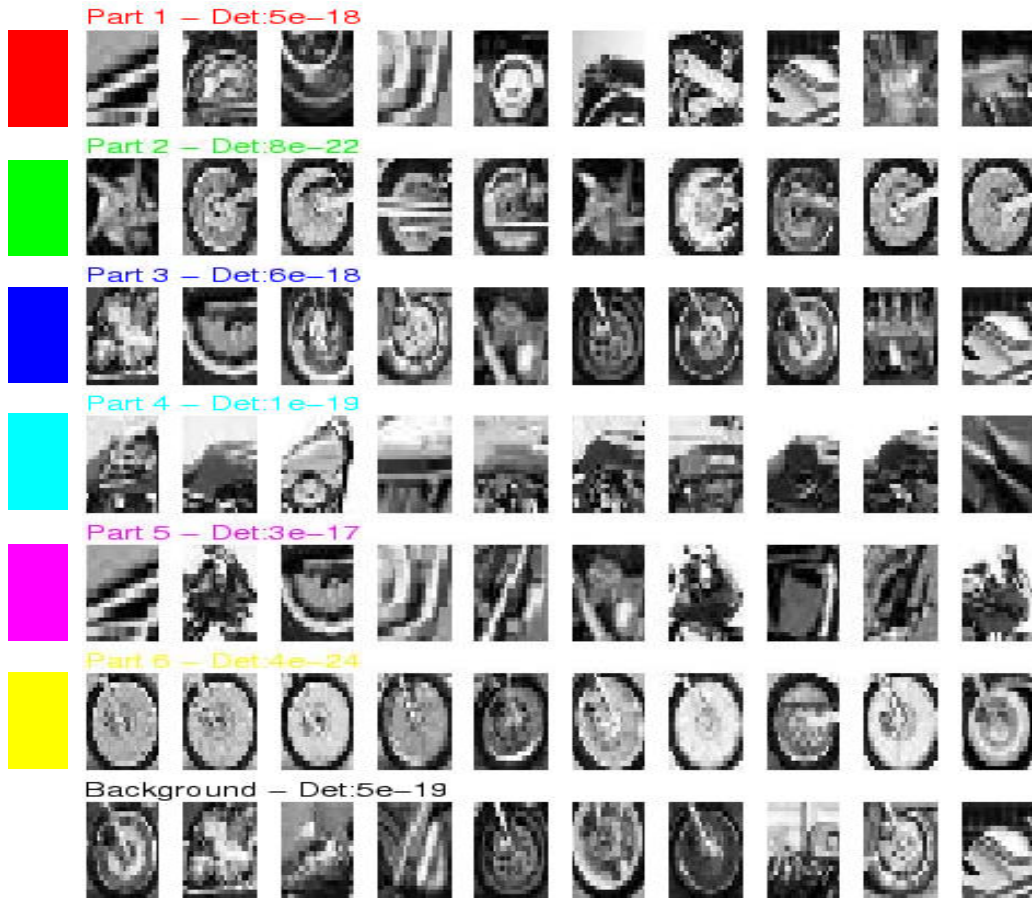


Poisson pdf on # detections

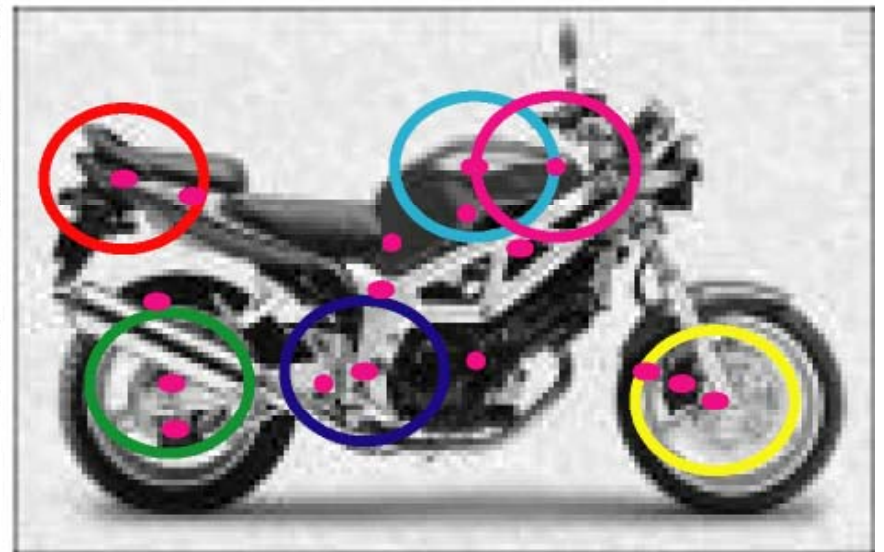
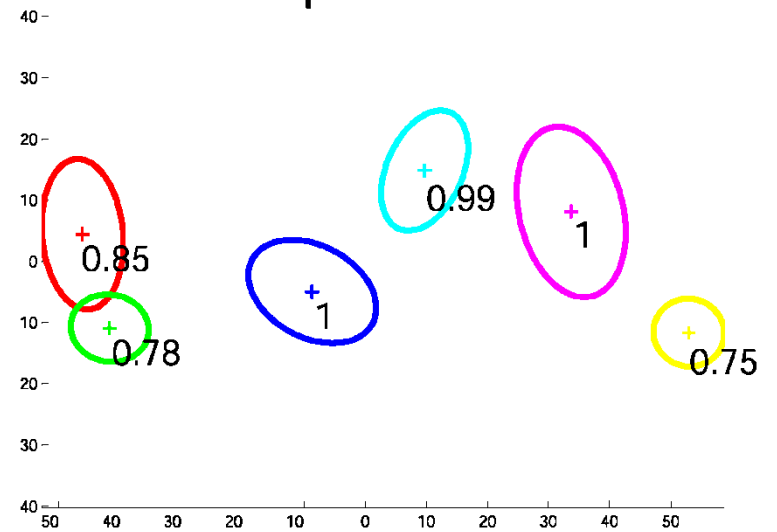
Slide credit: Fergus

# Motorbikes

## Samples from appearance model



## Shape model

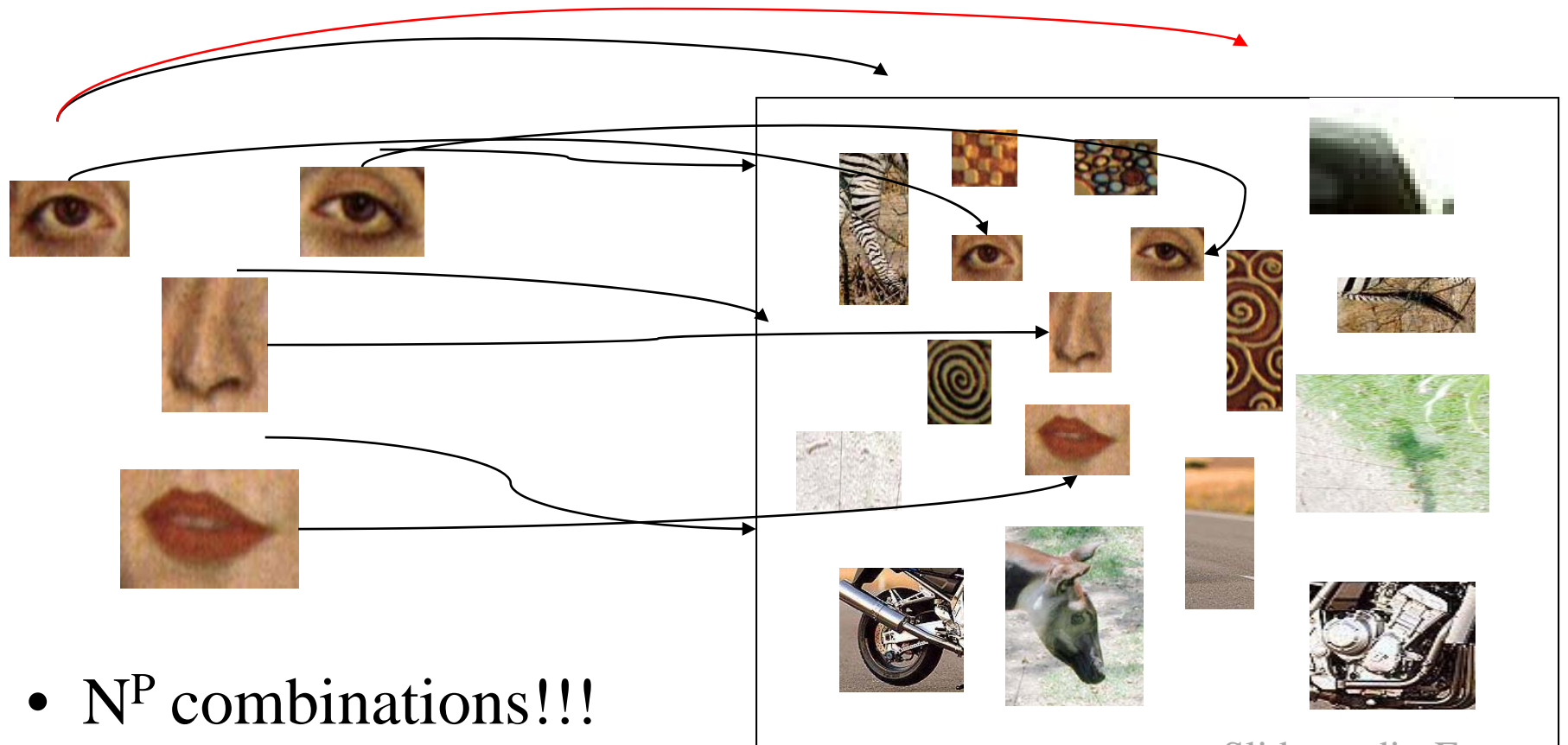


Slide credit: Fergus



# The correspondence problem

- Model with  $P$  parts
- Image with  $N$  possible assignments for each part
- Consider mapping to be 1-1



- $N^P$  combinations!!!

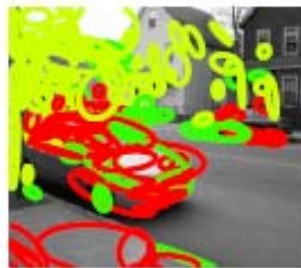
Slide credit: Fergus

# The correspondence problem

- ⊙ 1 – 1 mapping
  - ⊙ Each part assigned to unique feature

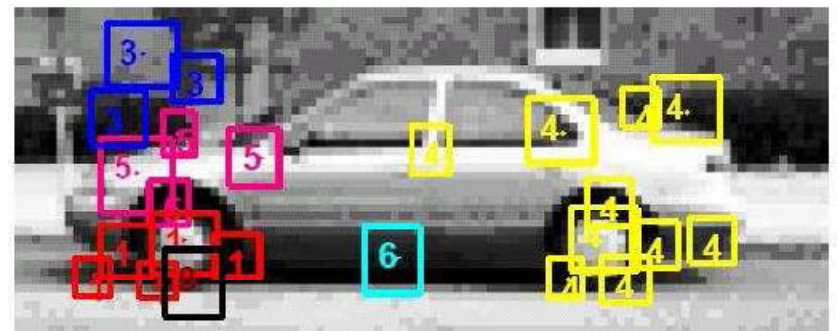
As opposed to:

- ⊙ 1 – Many
  - ⊙ Bag of words approaches
  - ⊙ Sudderth, Torralba, Freeman '05
  - ⊙ Loeff, Sorokin, Arora and Forsyth '05



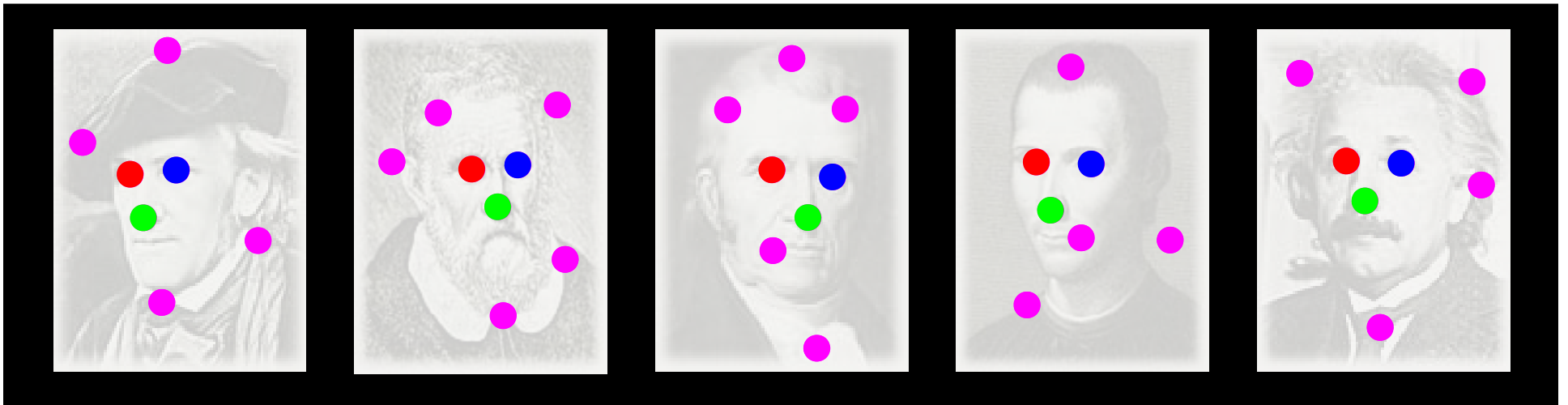
- Many – 1

- Quattoni, Collins  
and Darrell, 04



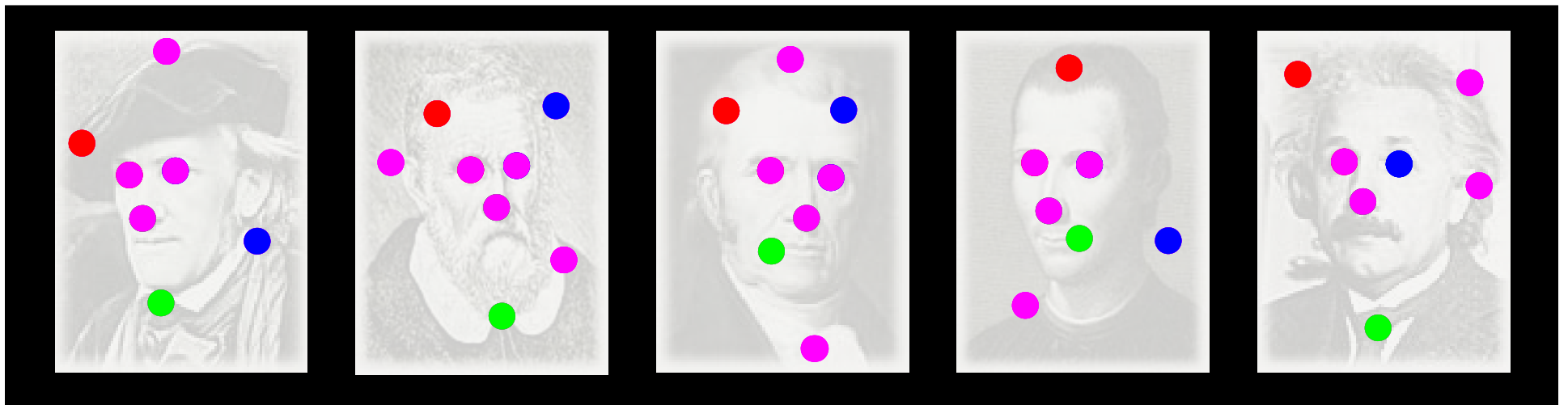
# Learning

- Task: Estimation of model parameters
- Chicken and Egg type problem, since we initially know neither:
  - Model parameters
  - Assignment of regions to foreground / background
- Let the assignments be a hidden variable and use EM algorithm to learn them and the model parameters



# Learning procedure

- Find regions & their location, scale & appearance
- Initialize model parameters
- Use EM and iterate to convergence:
  - E-step: Compute assignments for which regions are foreground / background
  - M-step: Update model parameters
- Trying to maximize likelihood – consistency in shape & appearance



# Experimental procedure

Two series of experiments:

- Fixed-scale model - Objects the same size (manual normalization)
- Scale-invariant model - Objects between 100 and 550 pixels in width

## Datasets

### Training

- 50% images
- No identification of object within image

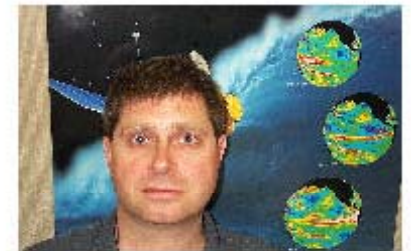
Motorbikes



Airplanes



Frontal Faces



### Testing

- 50% images
- Simple object present/absent test

Cars (Side)



Cars (Rear)

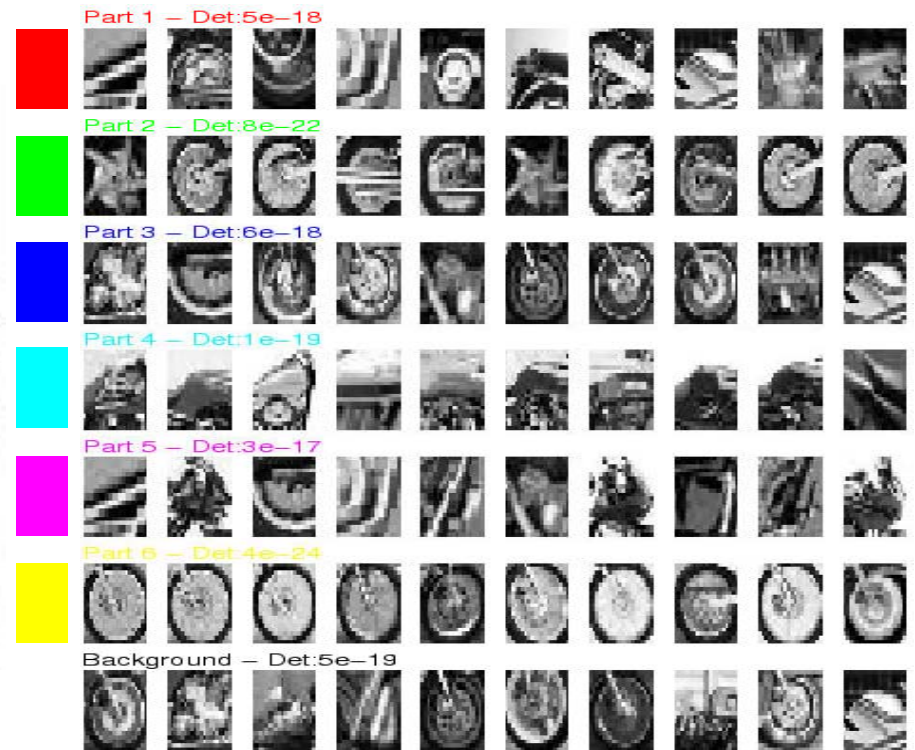
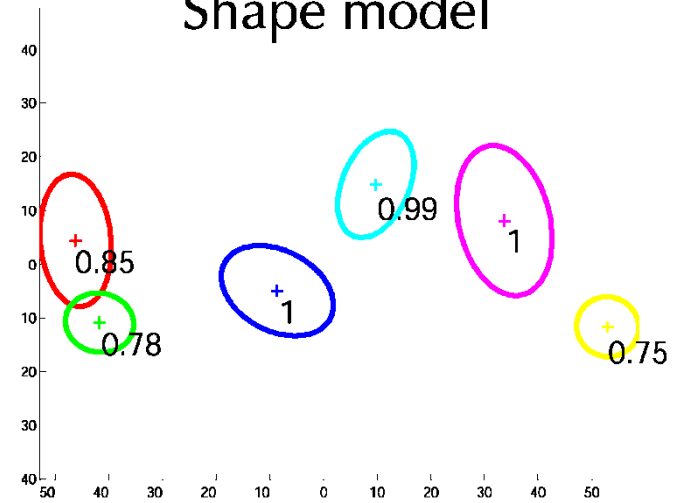
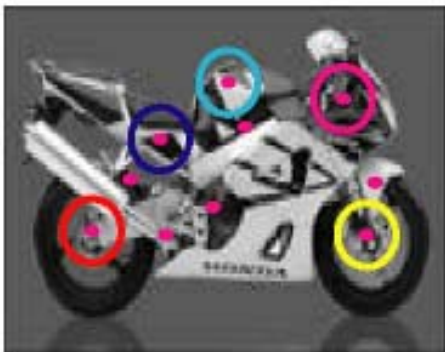


Spotted cats

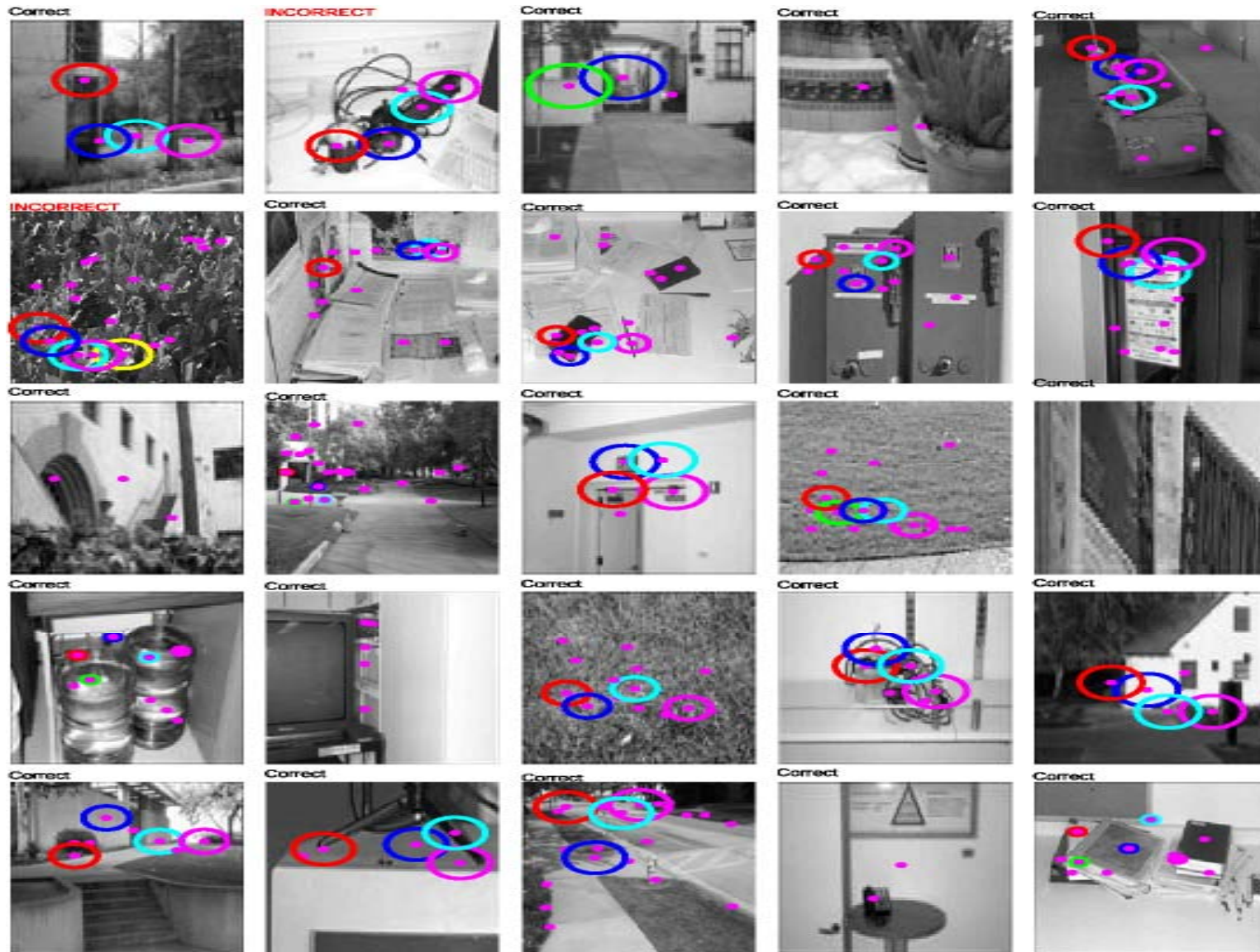


# Motorbikes

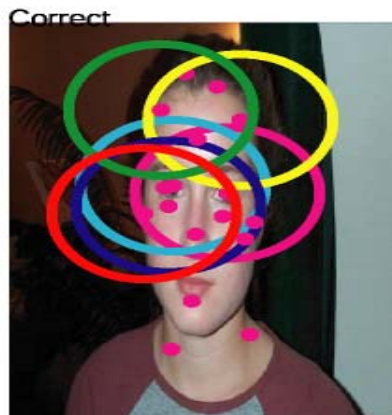
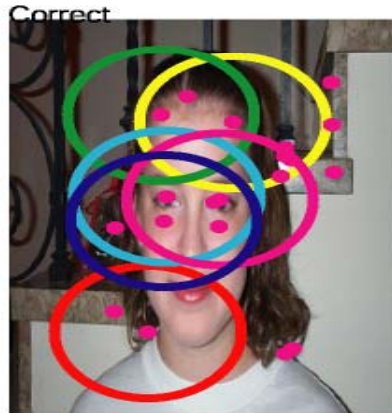
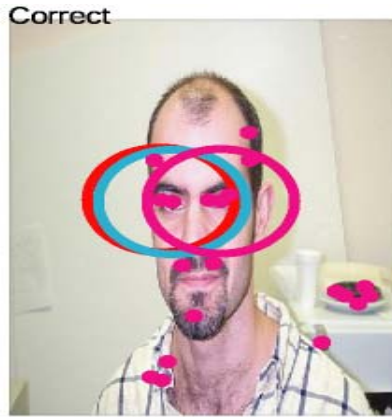
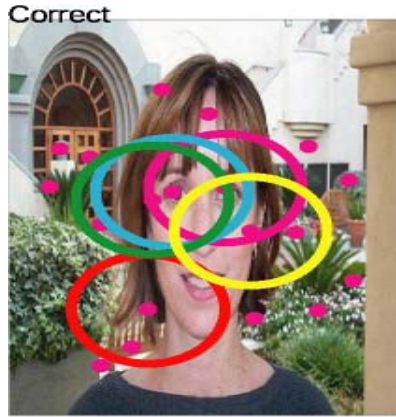
Shape model



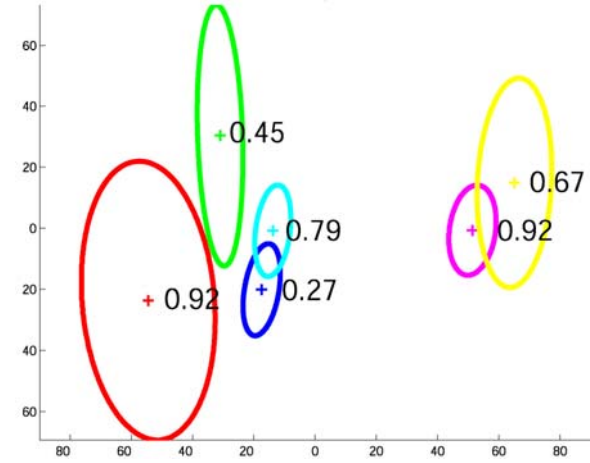
# Background images evaluated with motorbike model



# Frontal faces



Face shape model





# Airplanes

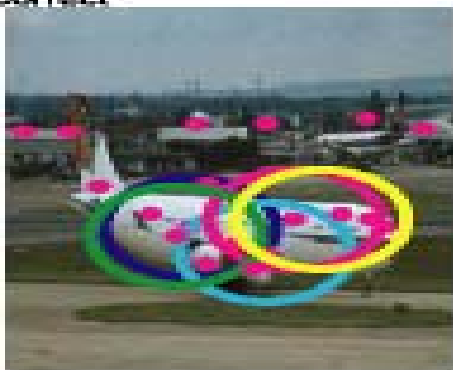
Correct



Correct



Correct



Correct



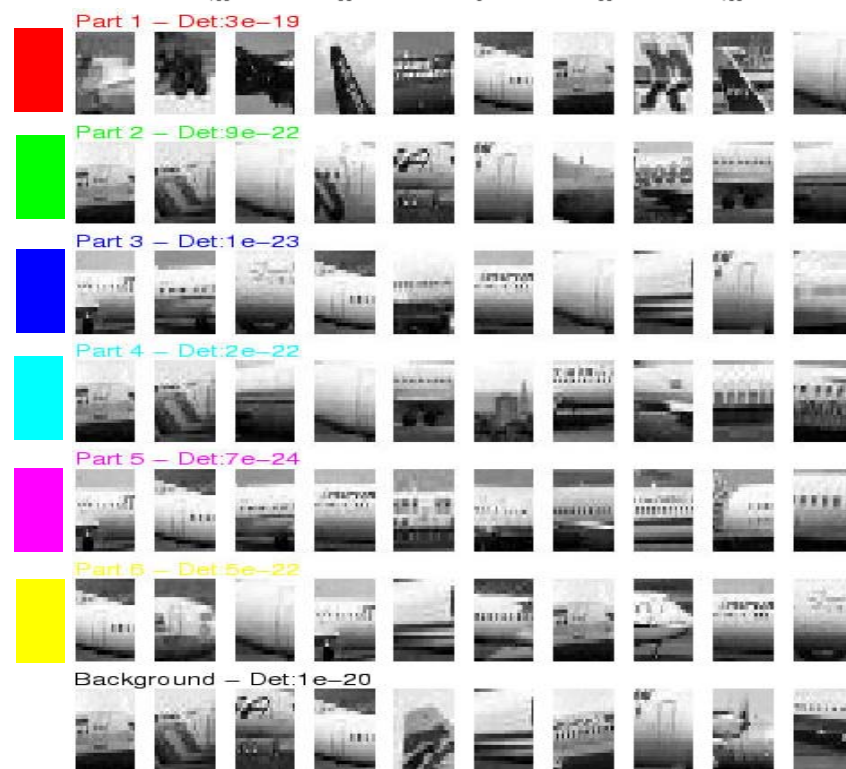
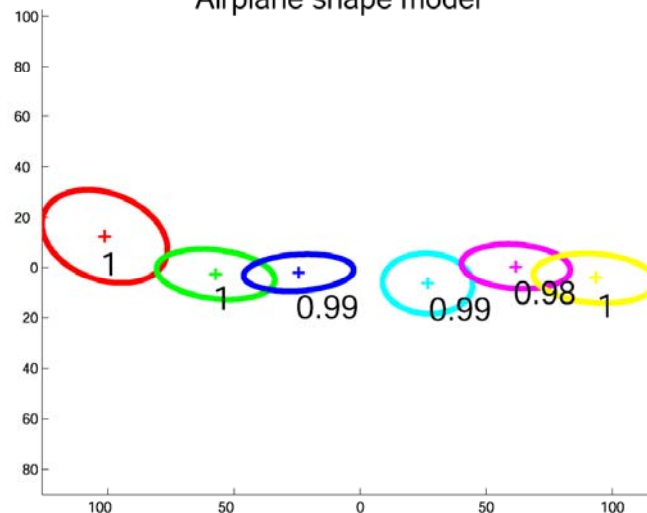
Correct



Correct

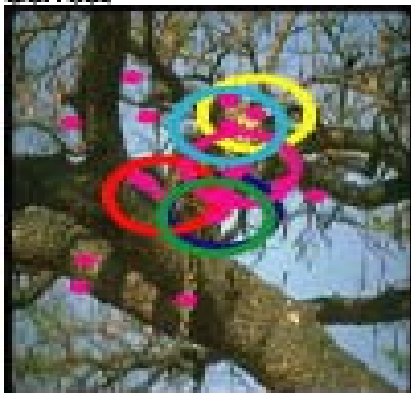


Airplane shape model

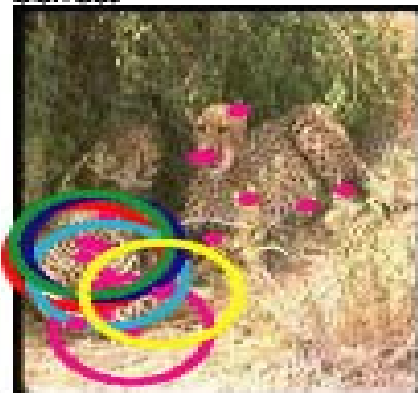


# Spotted cats

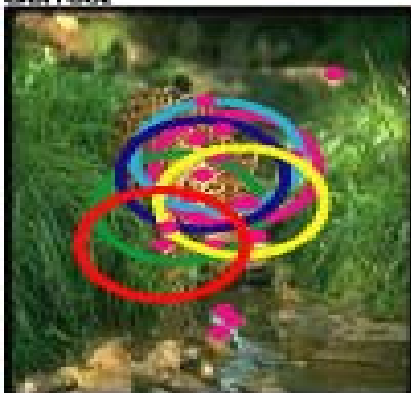
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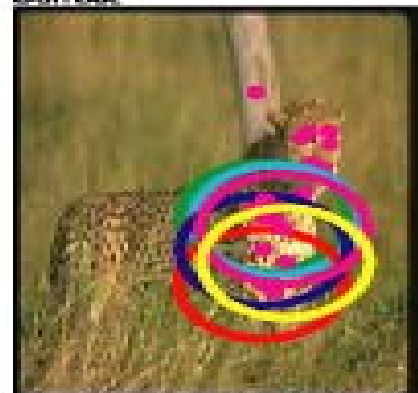
Correct



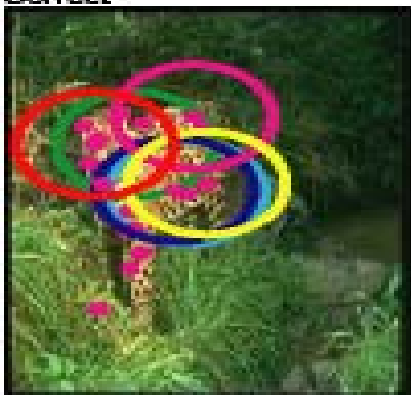
Correct



Correct



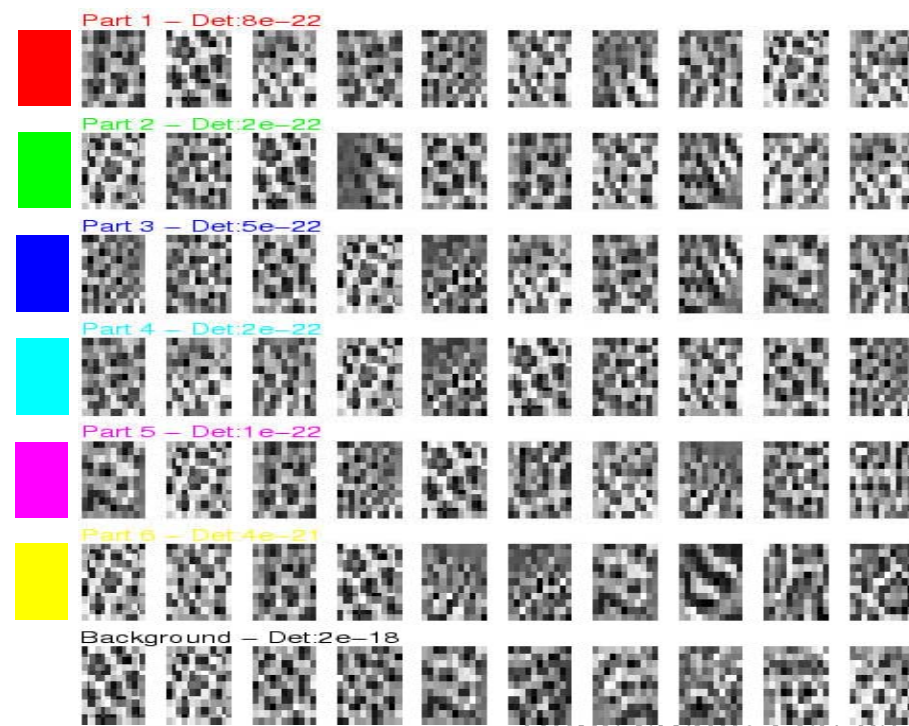
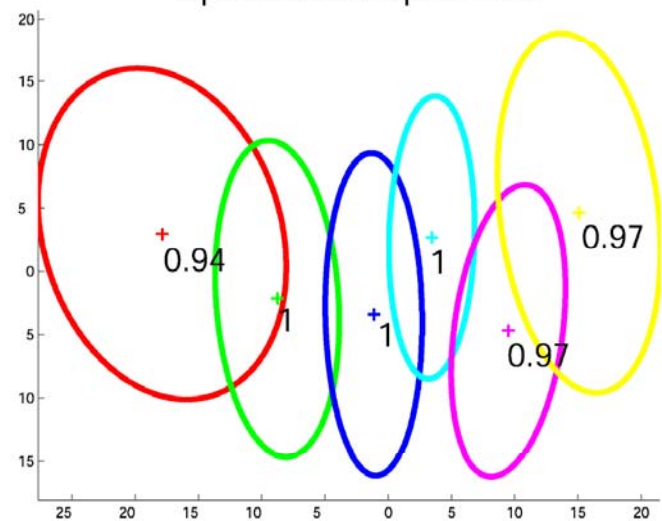
Correct



Correct



Spotted cat shape model



# Summary of results

Dataset	Fixed scale experiment	Scale invariant experiment
Motorbikes	7.5	6.7
Faces	4.6	4.6
Airplanes	9.8	7.0
Cars (Rear)	15.2	9.7
Spotted cats	10.0	10.0

% equal error rate

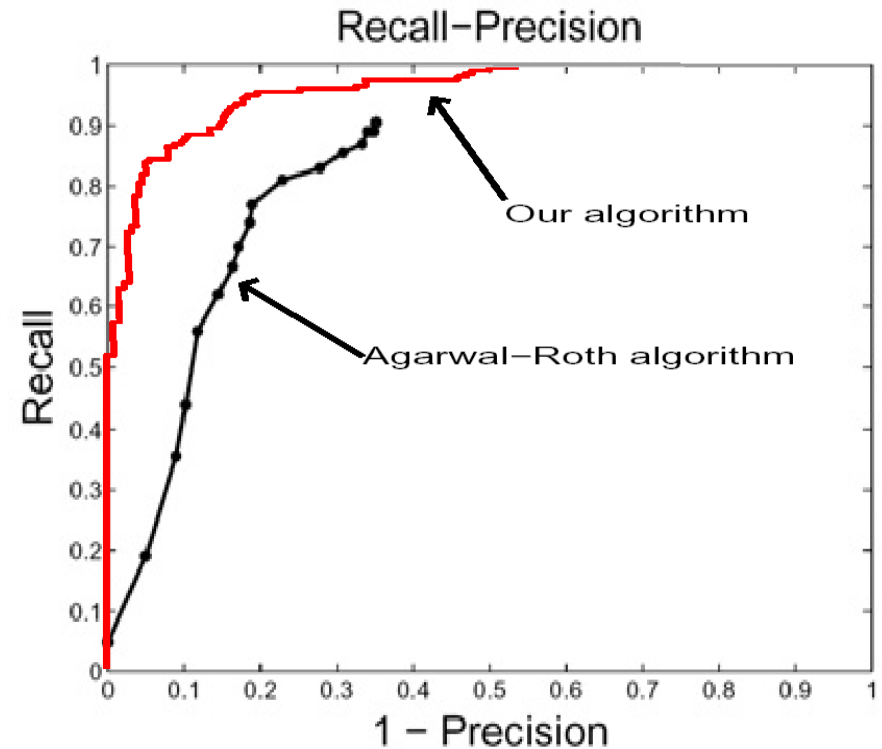
Note: Within each series, same settings used for all datasets

Slide credit: Fergus

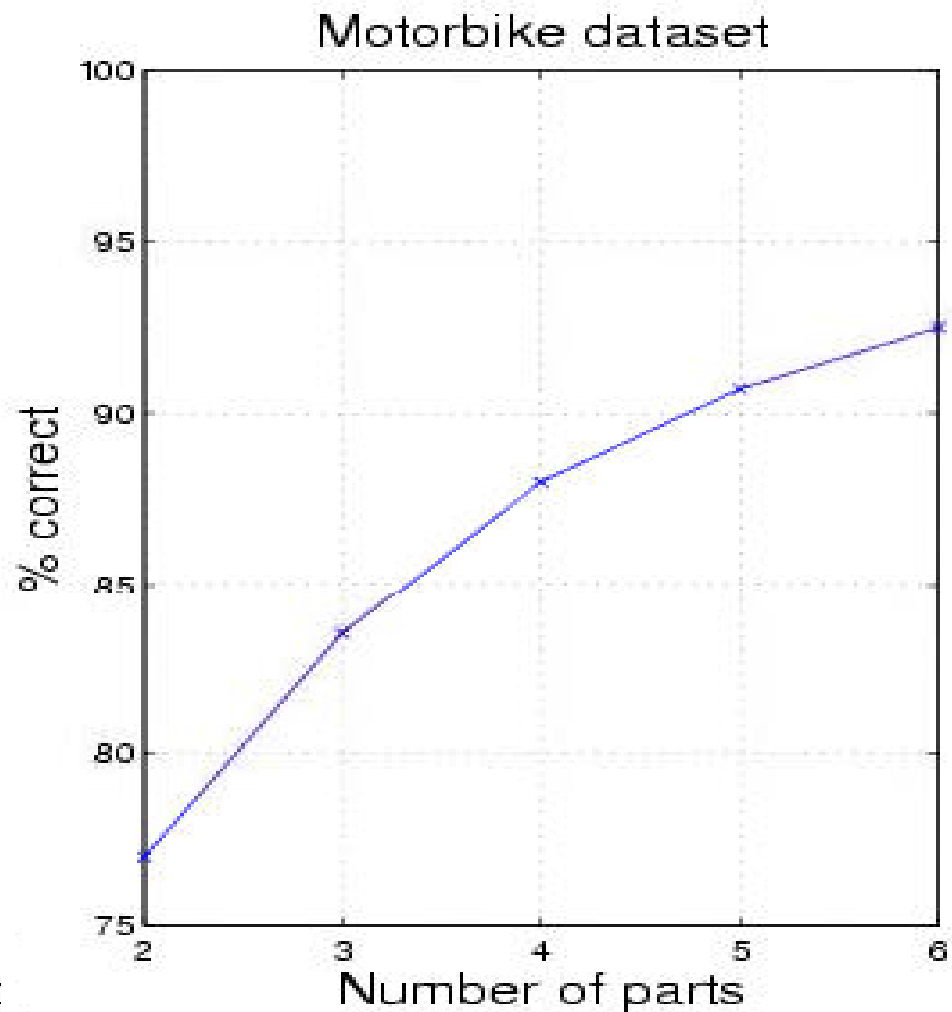
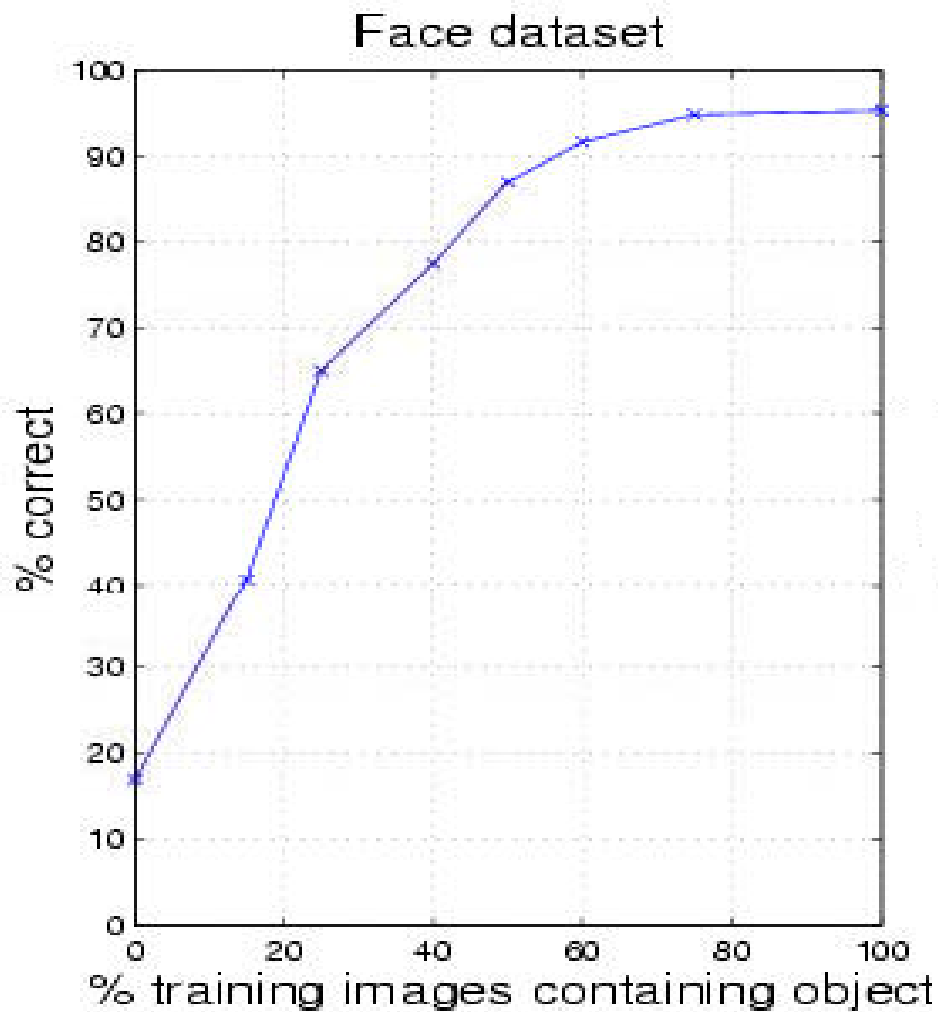
# Comparison to other methods

Dataset	Ours	Others	
Motorbikes	7.5	16.0	Weber et al. [ECCV '00]
Faces	4.6	6.0	Weber
Airplanes	9.8	32.0	Weber
Cars (Side)	11.5	21.0	Agarwal Roth [ECCV '02]

% equal error rate



# Robustness of Algorithm



# Summary -- Fergus

- Comprehensive probabilistic model for object classes
- Learn appearance, shape, relative scale, occlusion etc. simultaneously in scale and translation invariant manner
- Same algorithm gives  $\leq 10\%$  error across 5 diverse datasets with identical settings

## Limitations → future work

- Very reliant on region detector  
Different part types (e.g. edgel curves)
- Only learns a single viewpoint  
Use mixture models
- Need lots of images to learn  
Bayesian learning - fewer images [ICCV '03 (Fei Fei, Fergus, Perona)]
- Need more thorough testing  
Looking towards testing 100's of datasets

Datasets available from:  
<http://www.robots.ox.ac.uk/~vgg/data>

Slide credit: Fergus



# Implicit Shape Model

[Leibe,Schiele04]

Mario Fritz





# Learning Object Appearance Models via Transformed Dirichlet Processes

Erik Sudderth

University of California, Berkeley

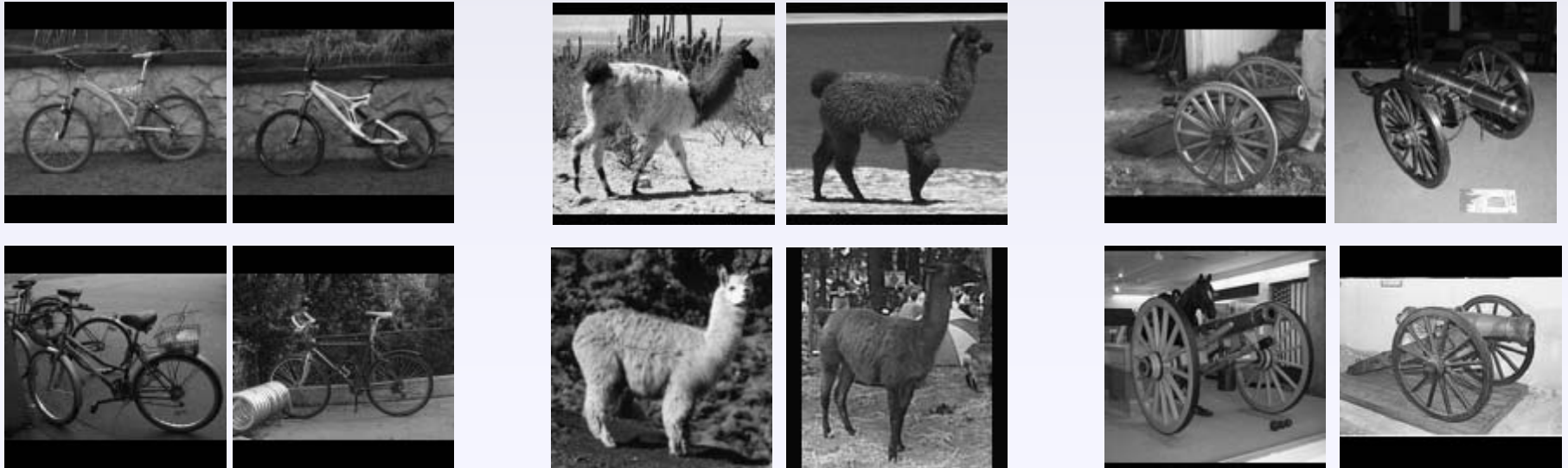


*Joint work  
with*

Antonio Torralba  
William Freeman  
Alan Willsky

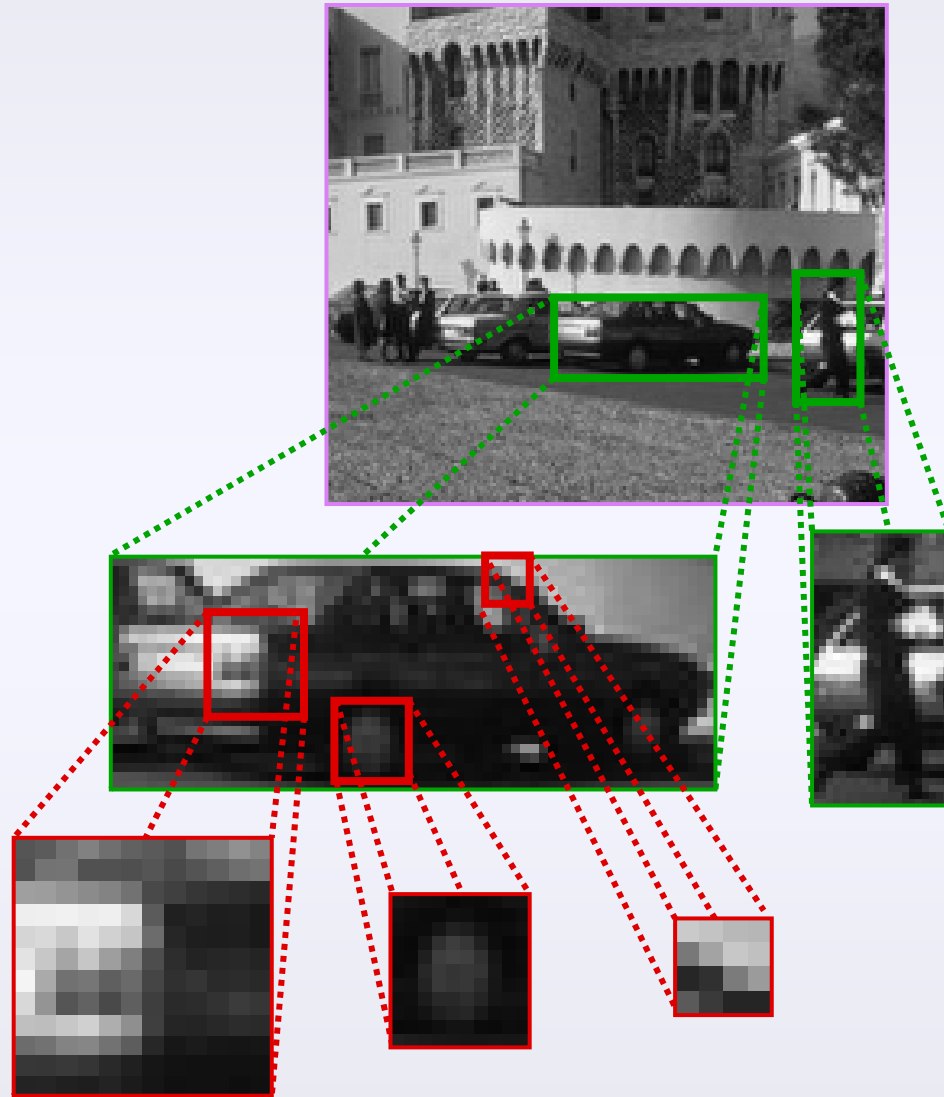


# Visual Object Categorization



- **GOAL:** Visually *recognize* and *localize* object categories
- Robustly *learn* appearance models from few examples
  - Hierarchical model *transfers* knowledge among categories
  - Nonparametric, *Dirichlet process* prior gives flexibility

# Scenes, Objects, and Parts



*Scene*



*Objects*



*Parts*



*Features*

# Outline

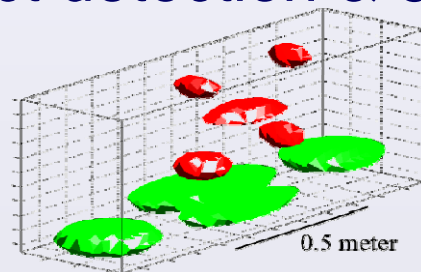
## Object Recognition with Shared Parts

- Learning parts via Dirichlet processes
- Hierarchical DP model for 16 object categories

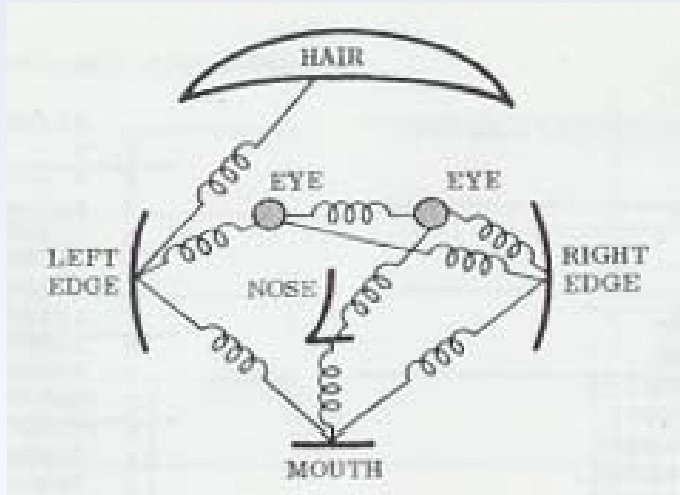


## Multiple Object Scenes

- Transformed Dirichlet processes
- Part-based models for 2D scenes
- Joint object detection & 3D reconstruction

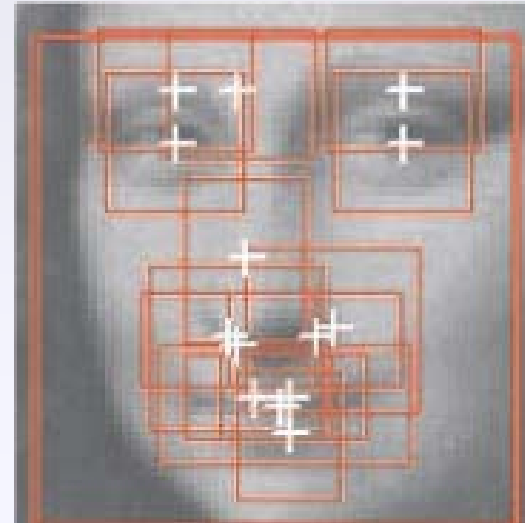


# Describing Objects with Parts



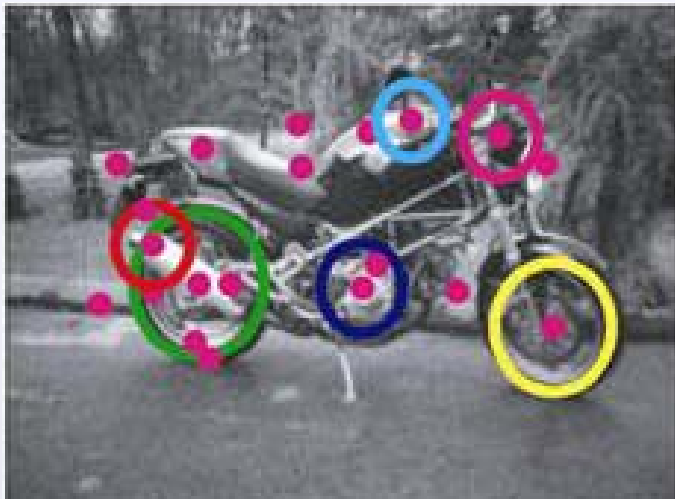
## Pictorial Structures

*Fischler & Elschlager, IEEE Trans. Comp. 1973*



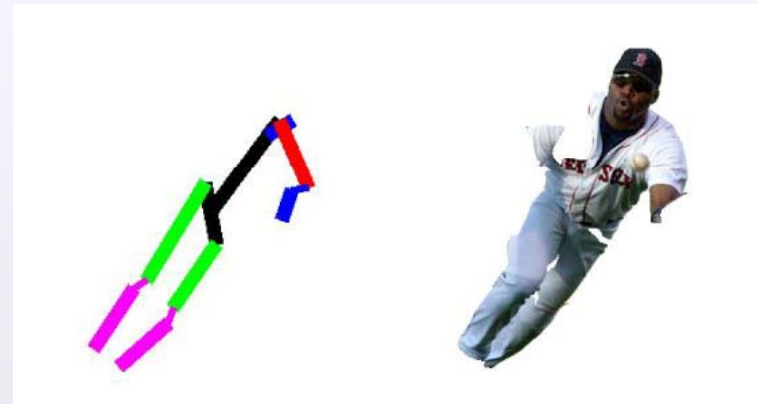
## Cascaded SVM Detectors

*Heisele, Poggio, et. al., NIPS 2001*



## Constellation Model

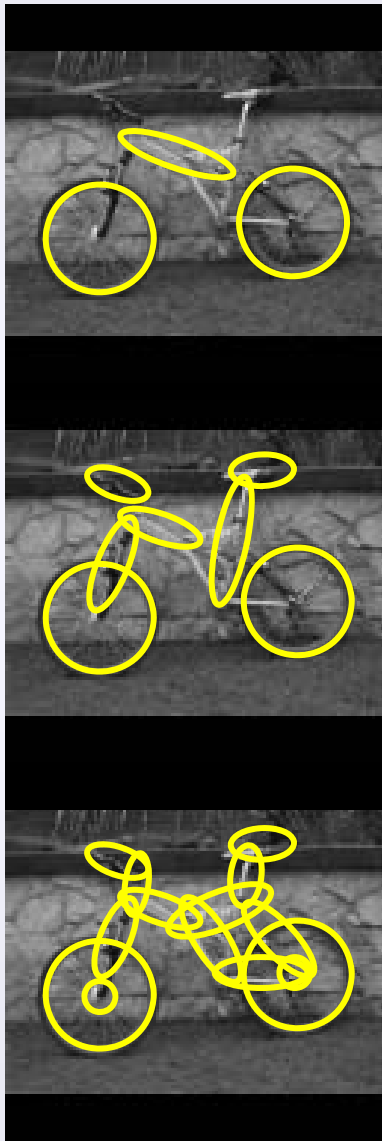
*Fergus, Perona, & Zisserman, CVPR 2003*



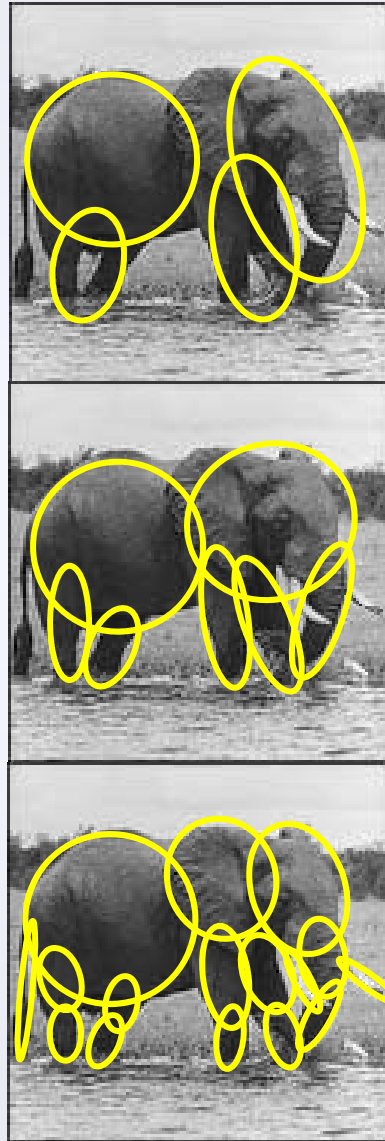
## Model-Guided Segmentation

*Mori, Ren, Efros, & Malik, CVPR 2004*

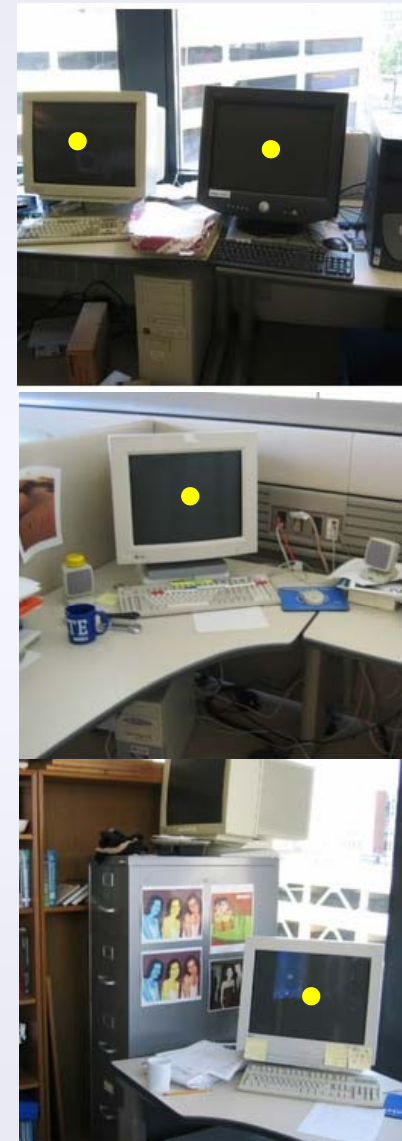
# Counting Objects & Parts



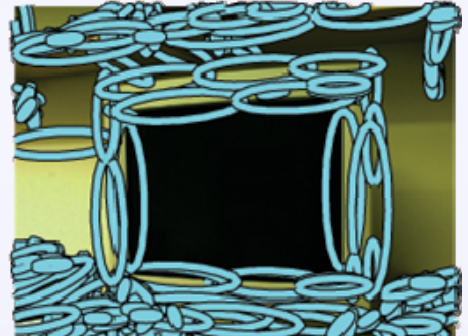
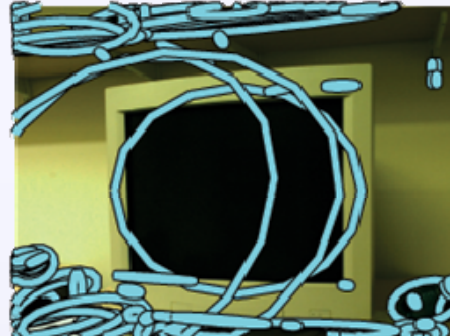
*How many parts?*



*How many objects?*



# From Images to Features



**Affinely Adapted  
Harris Corners**

**Maximally Stable  
Extremal Regions**

**Linked Sequences  
of Canny Edges**

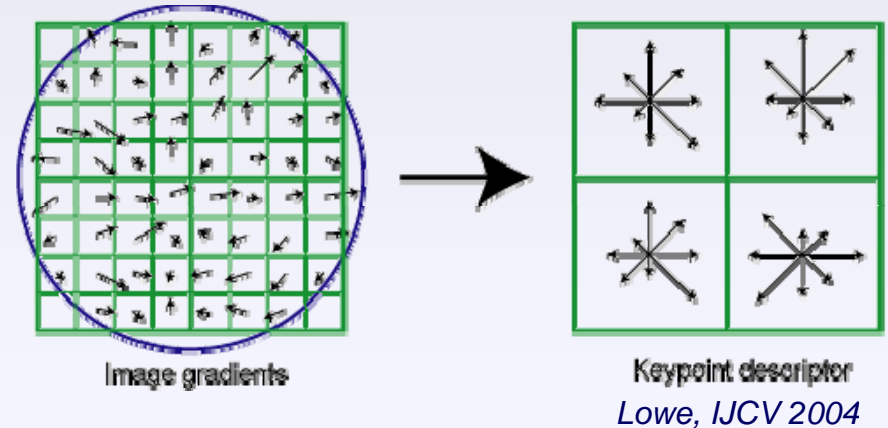
- Some invariance to lighting & pose variations
- Dense, multiscale, over-segmentation of image



# A Discrete Feature Vocabulary

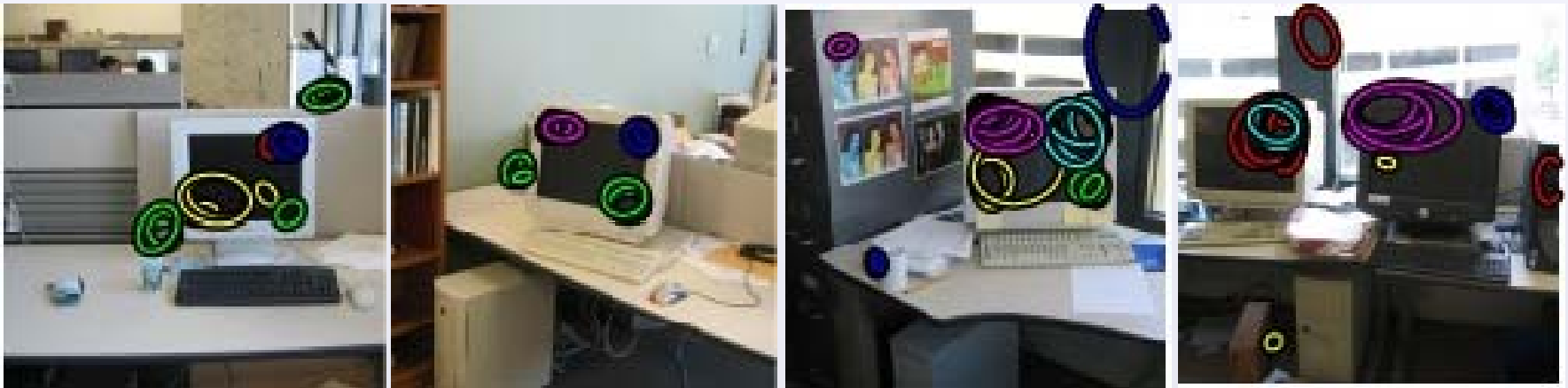
## *SIFT Descriptors*

- Normalized histograms of orientation energy
- Compute ~1,000 word dictionary via K-means
- Map each feature to nearest *visual word*

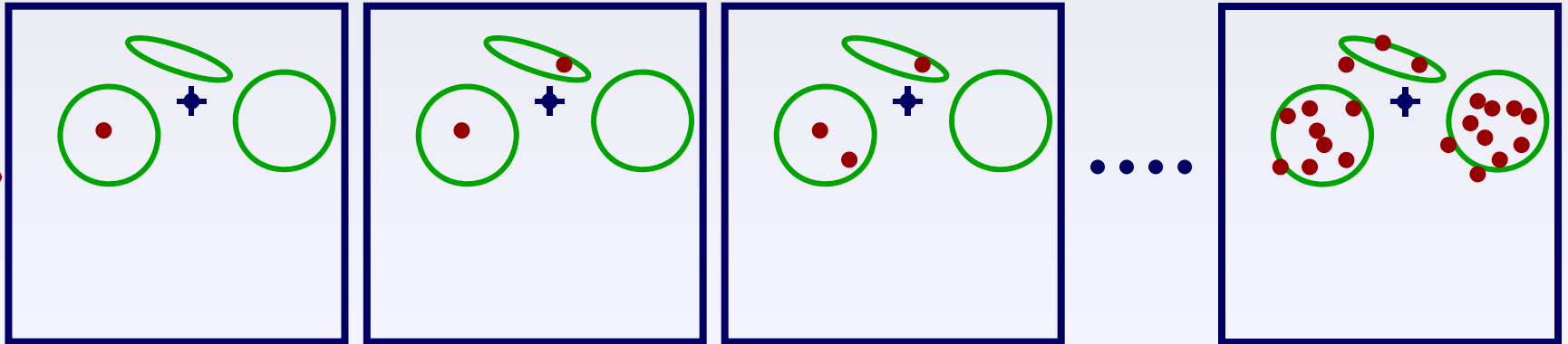


$w_{ji}$   $\longrightarrow$  appearance of feature  $i$  in image  $j$

$v_{ji}$   $\longrightarrow$  2D position of feature  $i$  in image  $j$



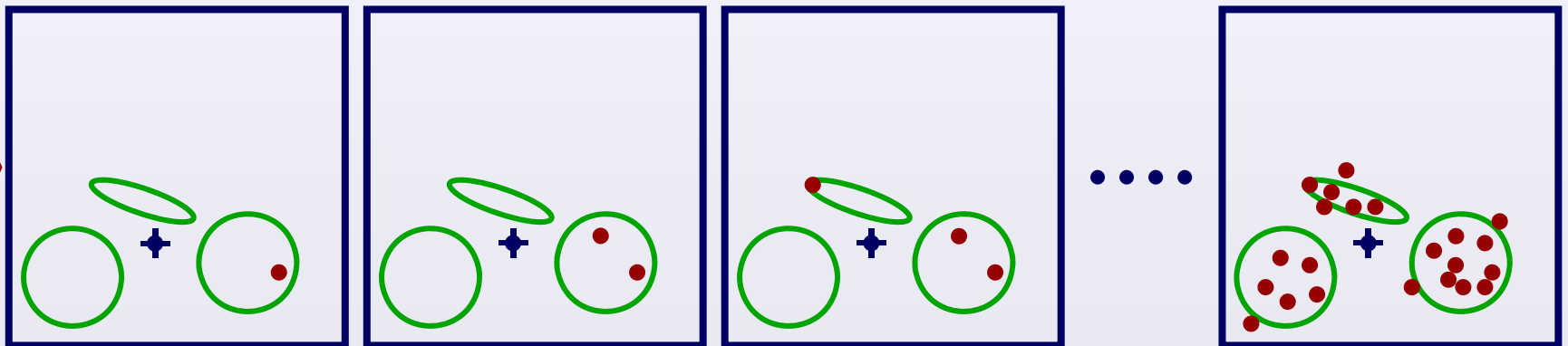
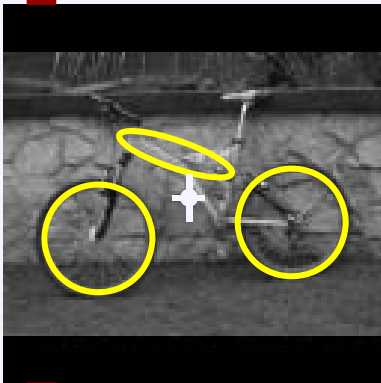
# Generative Model for Objects



**For each image:** Sample a reference position

**For each feature:**

- Randomly choose one part
- Sample from that part's feature distribution



# Objects as Mixture Models

- For a fixed reference position, our generative model is equivalent to a finite mixture model:

$$p(w_{ji}, v_{ji} | \rho_j) = \sum_{k=1}^K \pi_k \eta_k(w_{ji}) \mathcal{N}(v_{ji}; \mu_k + \rho_j, \Lambda_k)$$

Feature appearance

Feature position

Pr(part)

Pr(appearance | part)

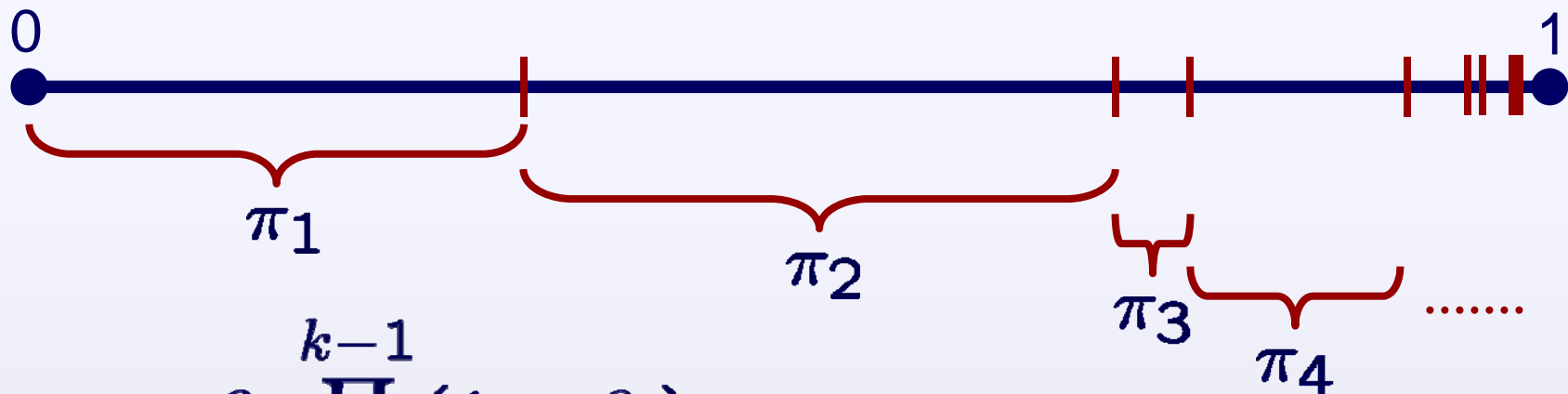
Pr(position | part)

- How many parts should we choose?
  - Too few reduces model accuracy
  - Too many causes overfitting & poor generalization

# Dirichlet Process Mixtures

$$p(x) = \sum_{k=1}^{\infty} \pi_k f(x | \theta_k)$$

- *Dirichlet processes* define a prior distribution on weights assigned to mixture components:



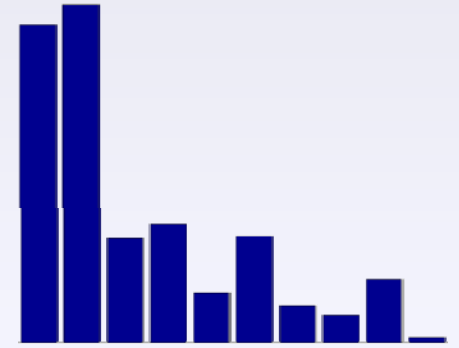
$$\pi_k = \beta_k \prod_{\ell=1}^{k-1} (1 - \beta_\ell)$$

$$\beta_k \sim \text{Beta}(1, \alpha)$$

$\alpha$  → concentration parameter

# Why the Dirichlet Process?

$$p(x) = \sum_{k=1}^{\infty} \pi_k f(x | \theta_k)$$



**Nonparametric  $\neq$  No Parameters**

- Model complexity grows as data observed:
  - Small training sets give *simple, robust* predictions
  - Reduced sensitivity to prior assumptions

**Flexible but Tractable**

- Literature showing attractive *asymptotic properties*
- Leads to simple, effective *computational methods*
  - Avoids challenging model selection issues

# Objects as Distributions

$$p(w_{ji}, v_{ji} | \rho_j) = \sum_{k=1}^{\infty} \underbrace{\pi_k \eta_k(w_{ji})}_{\text{Pr(appearance | part)}} \underbrace{\mathcal{N}(v_{ji}; \mu_k + \rho_j, \Lambda_k)}_{\text{Pr(position | part)}}$$

↑ Feature appearance      ↑ Feature position

- Parts are defined by *parameters*, which encode distributions on visual features:

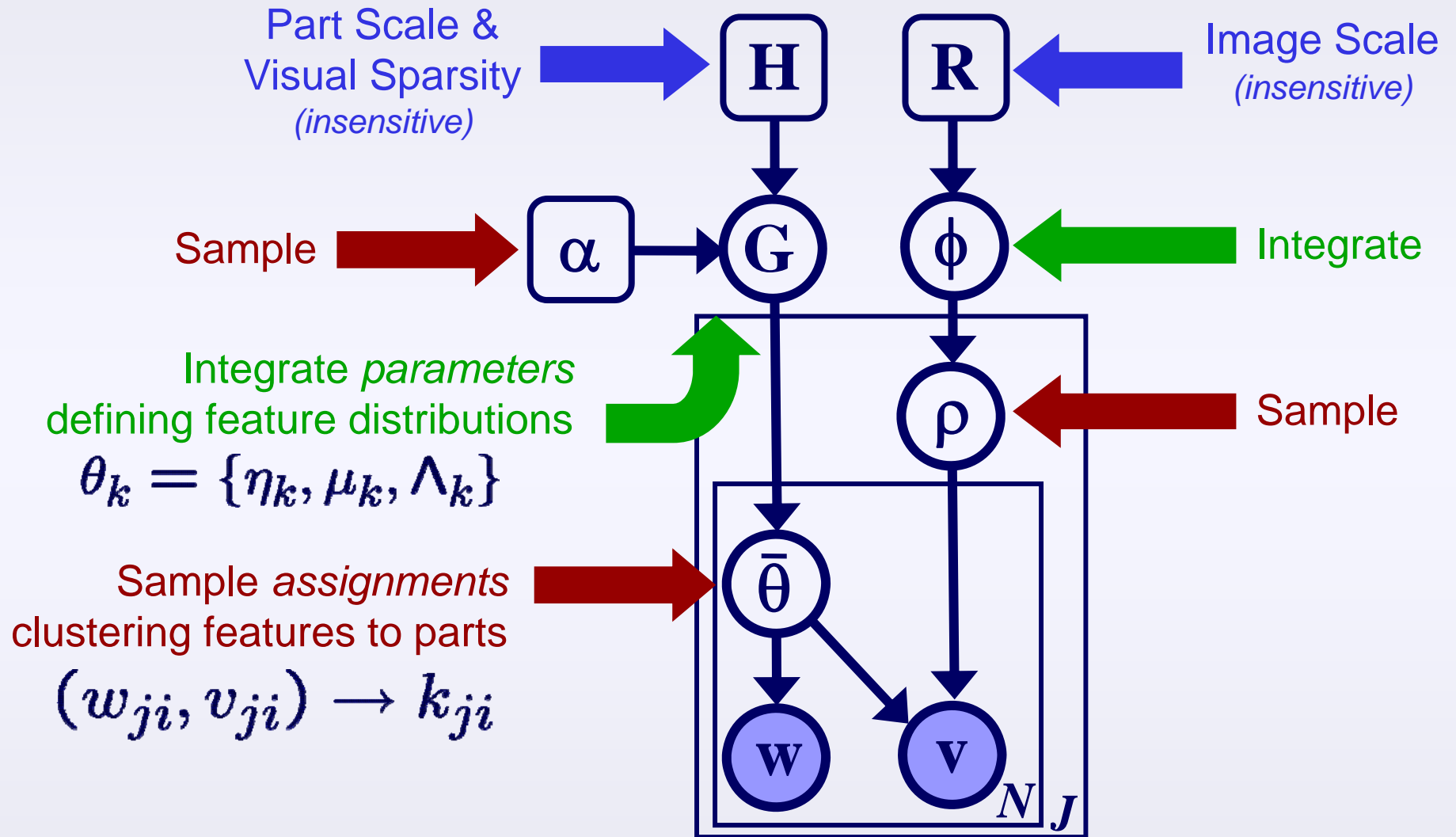
$$\theta_k = \{ \eta_k, \mu_k, \Lambda_k \}$$

- Objects are defined by *distributions* on the infinitely many potential part parameters:

$$G(\theta) = \sum_{k=1}^{\infty} \pi_k \delta(\theta, \theta_k) \quad \pi \sim \text{Stick}(\alpha)$$



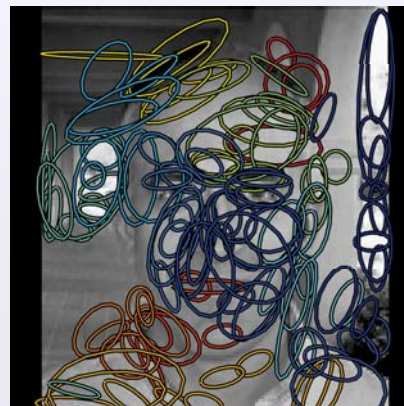
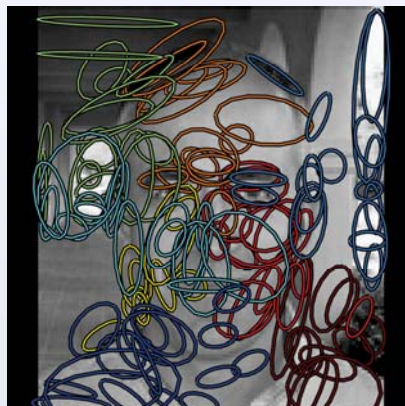
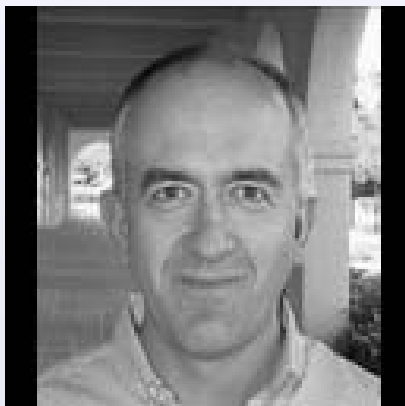
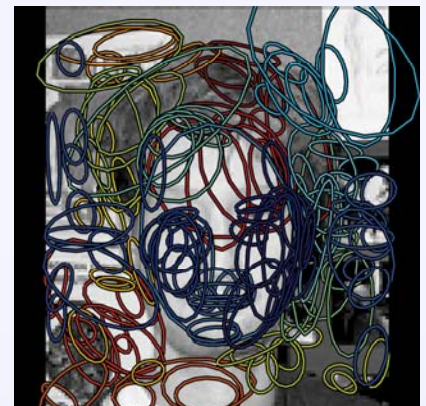
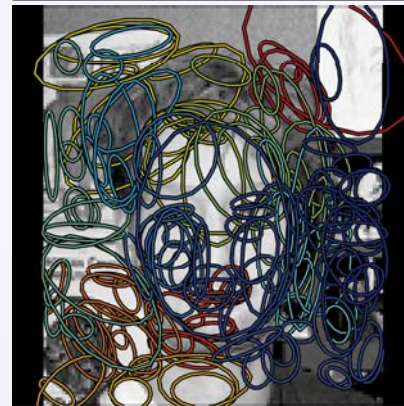
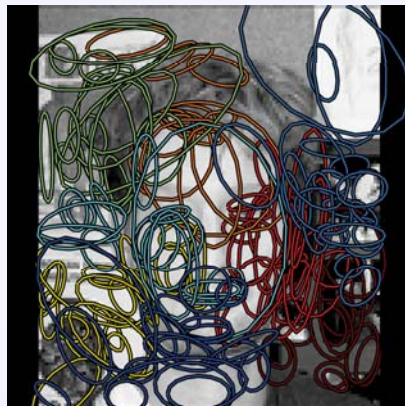
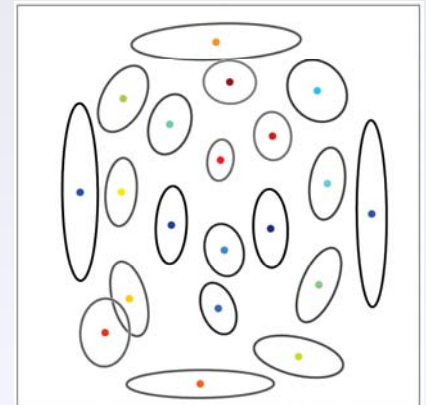
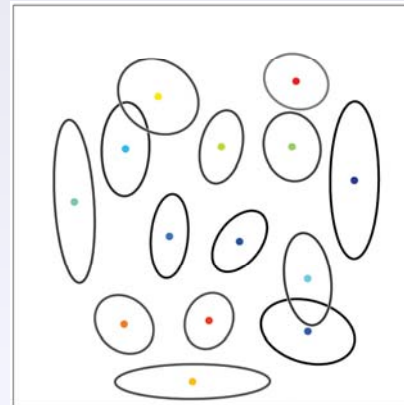
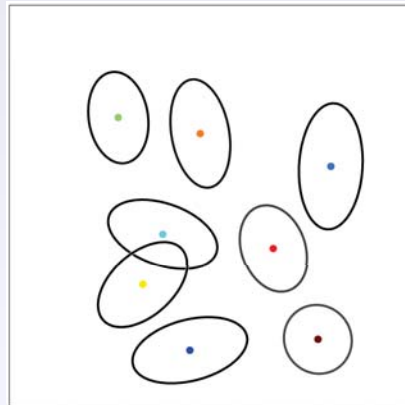
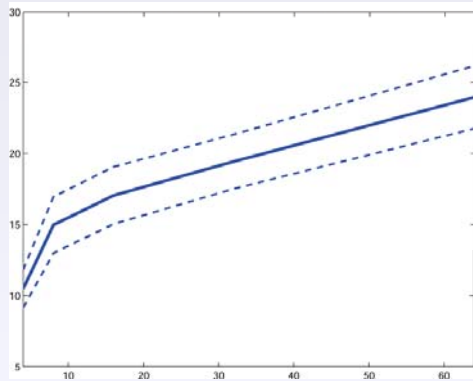
# Learning DPs: Gibbs Sampling



Dirichlet processes have many desirable analytic properties, which lead to efficient *Rao-Blackwellized* learning algorithms



# Decomposing Faces into Parts



4 Images

16 Images

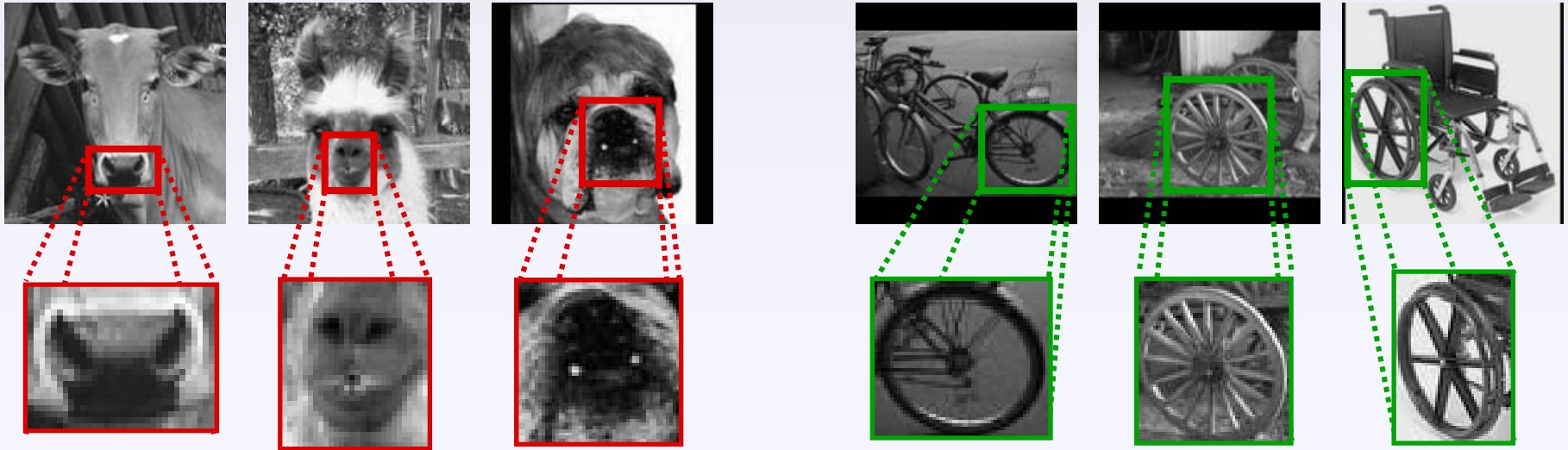
64 Images

# Generalizing Across Categories



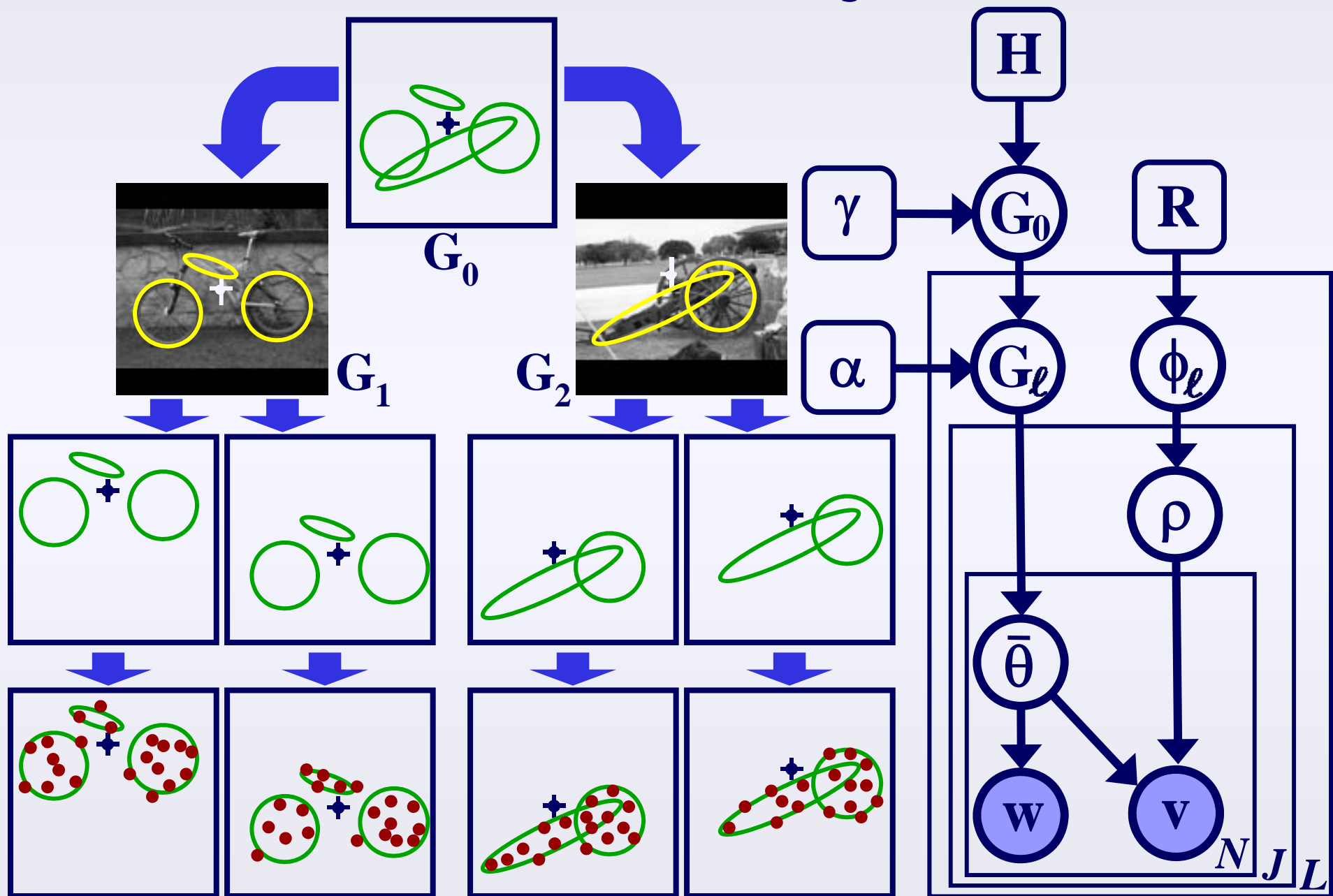
*Can we transfer knowledge from one object category to another?*

# Learning Shared Parts

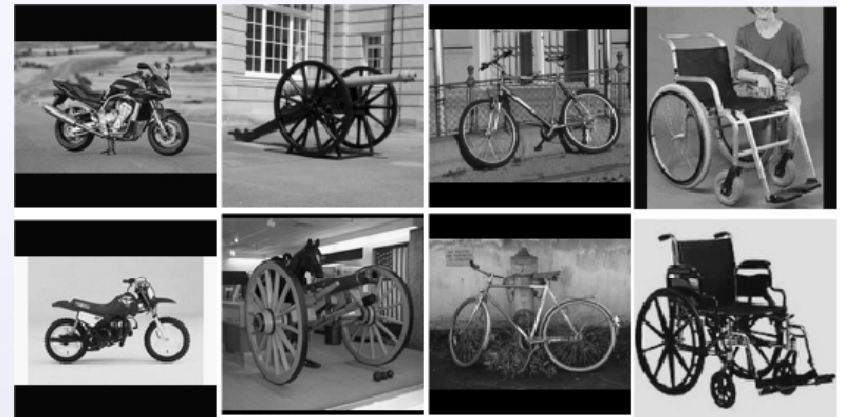
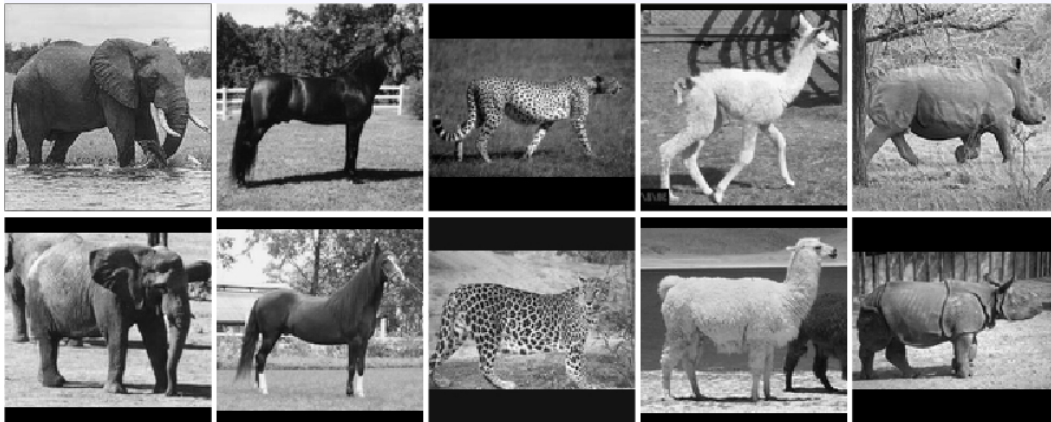


- Objects are often locally similar in appearance
- Discover *parts* shared across categories
  - How many total parts should we share?
  - How many parts should each category use?

# Hierarchical DP Object Model



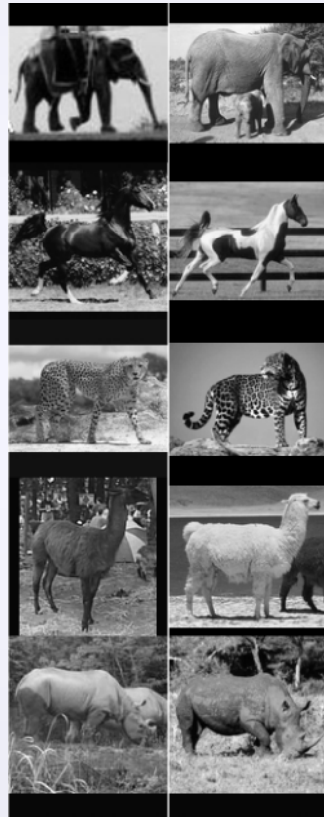
# Sharing Parts: 16 Categories



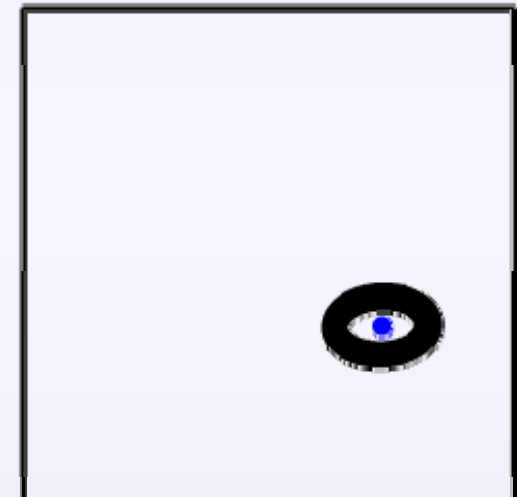
- Caltech 101 Dataset (Li & Perona)
- Horses (Borenstein & Ullman)
- Cat & dog faces (Vidal-Naquet & Ullman)

- Bikes from Graz-02 (Opelt & Pinz)
- Google...

# Visualization of Shared Parts

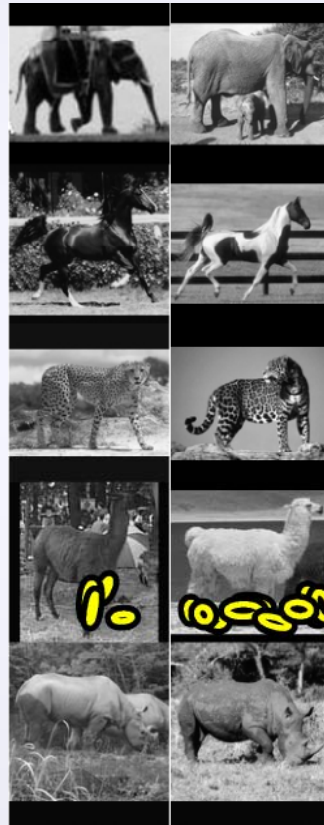


Pr(appearance | part)

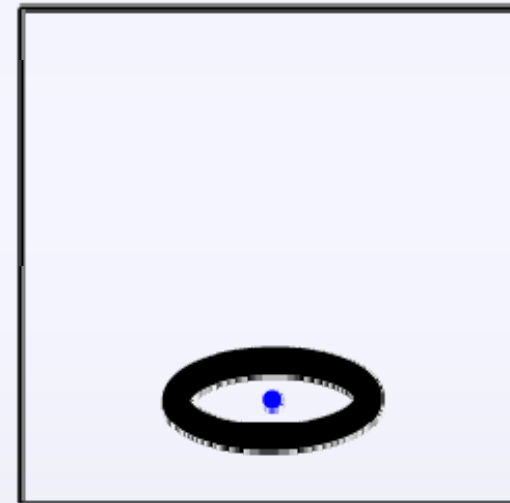


Pr(position | part)

# Visualization of Shared Parts

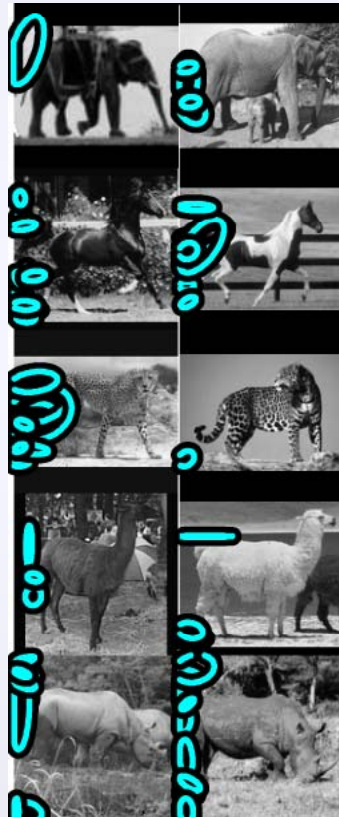


$\Pr(\text{appearance} \mid \text{part})$

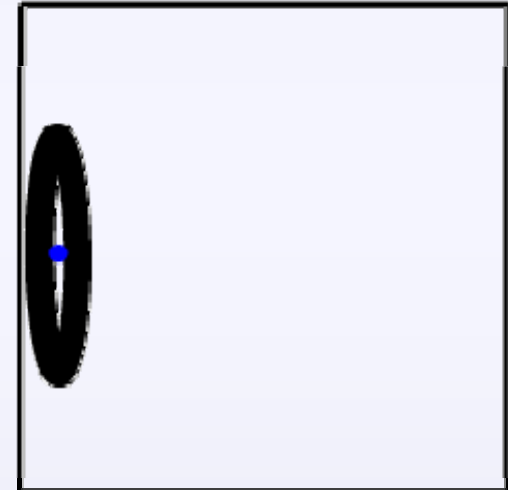


$\Pr(\text{position} \mid \text{part})$

# Visualization of Shared Parts



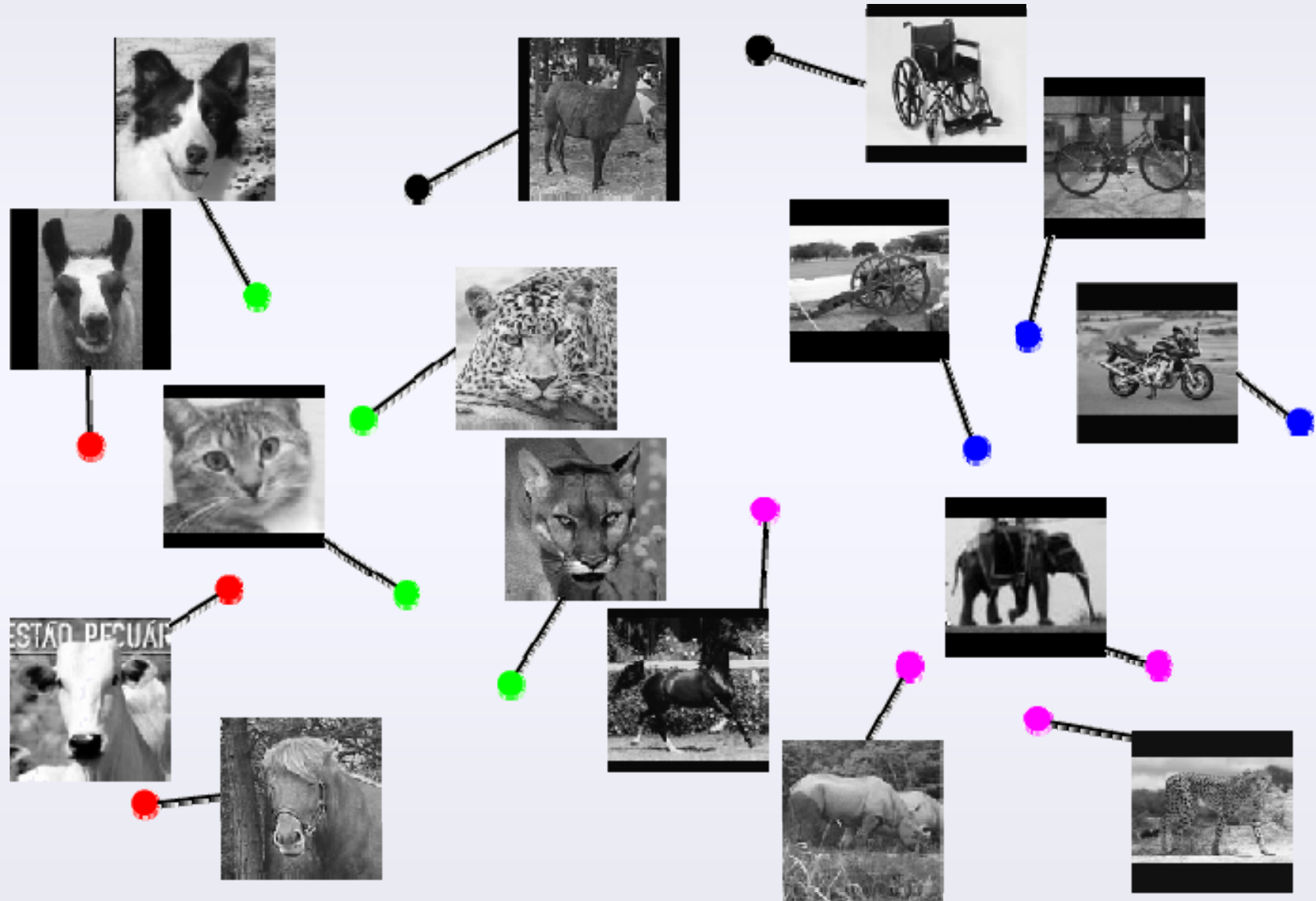
$\text{Pr}(\text{appearance} \mid \text{part})$



$\text{Pr}(\text{position} \mid \text{part})$

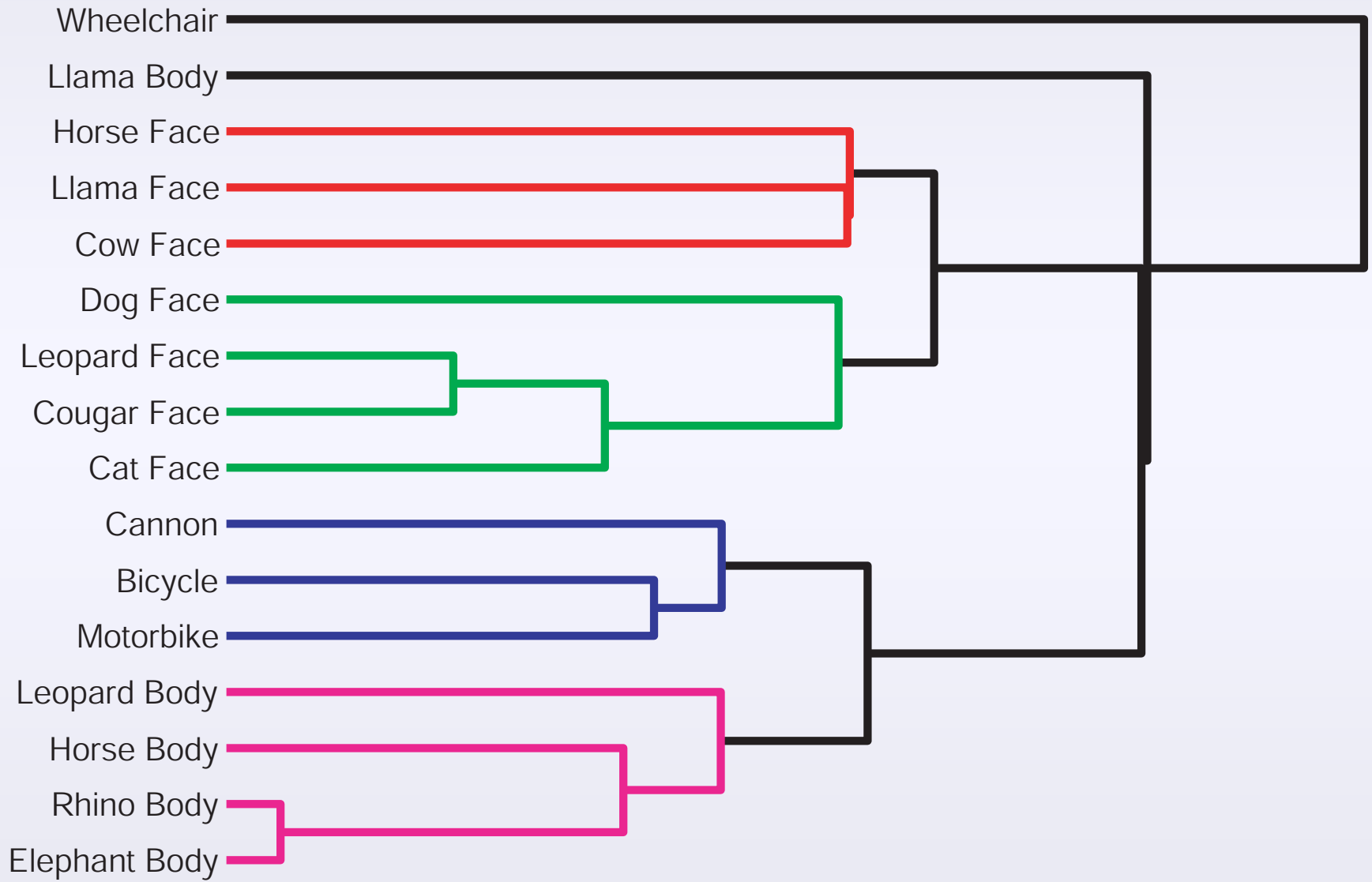


# Visualization of Part Densities



MDS Embedding of  $\Pr(\text{part} \mid \text{object})$

# Visualization of Part Densities

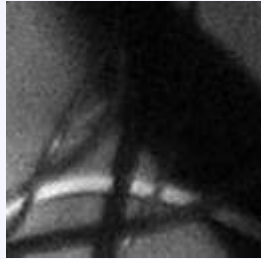
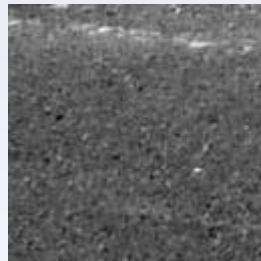
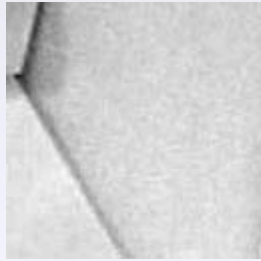


Hierarchical Clustering of  $\Pr(\text{part} \mid \text{object})$

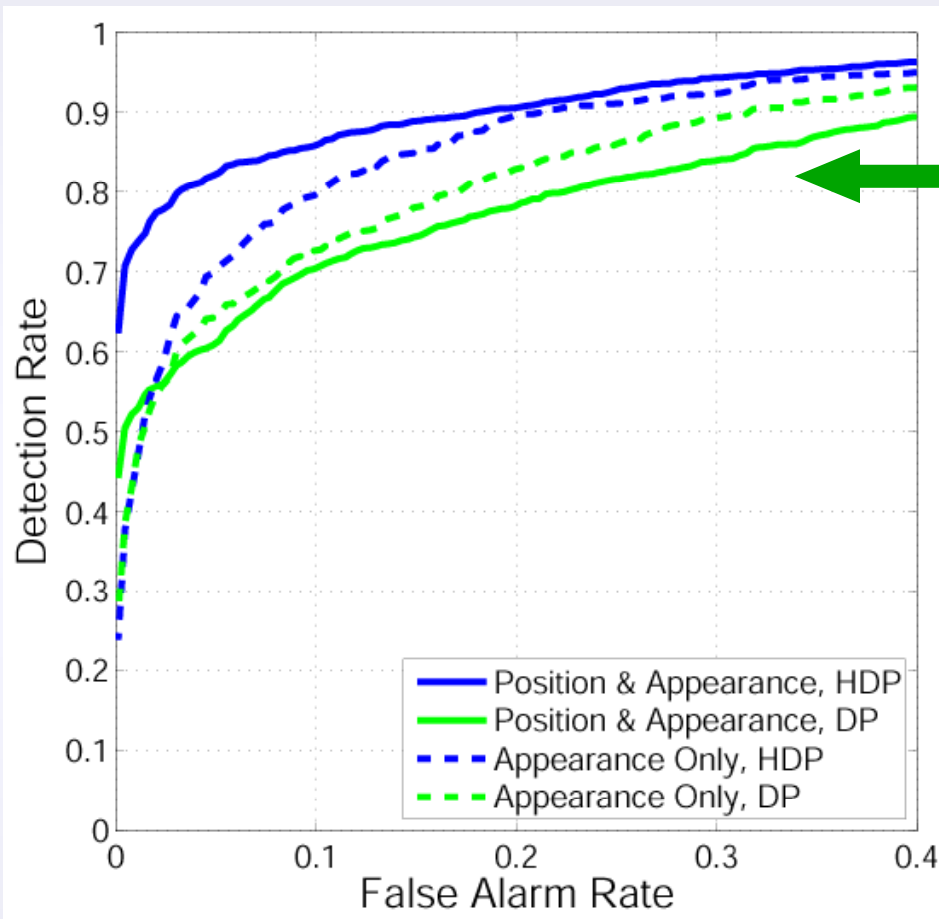
# Detection Task



**V  
E  
R  
S  
U  
S**



# Detection Results

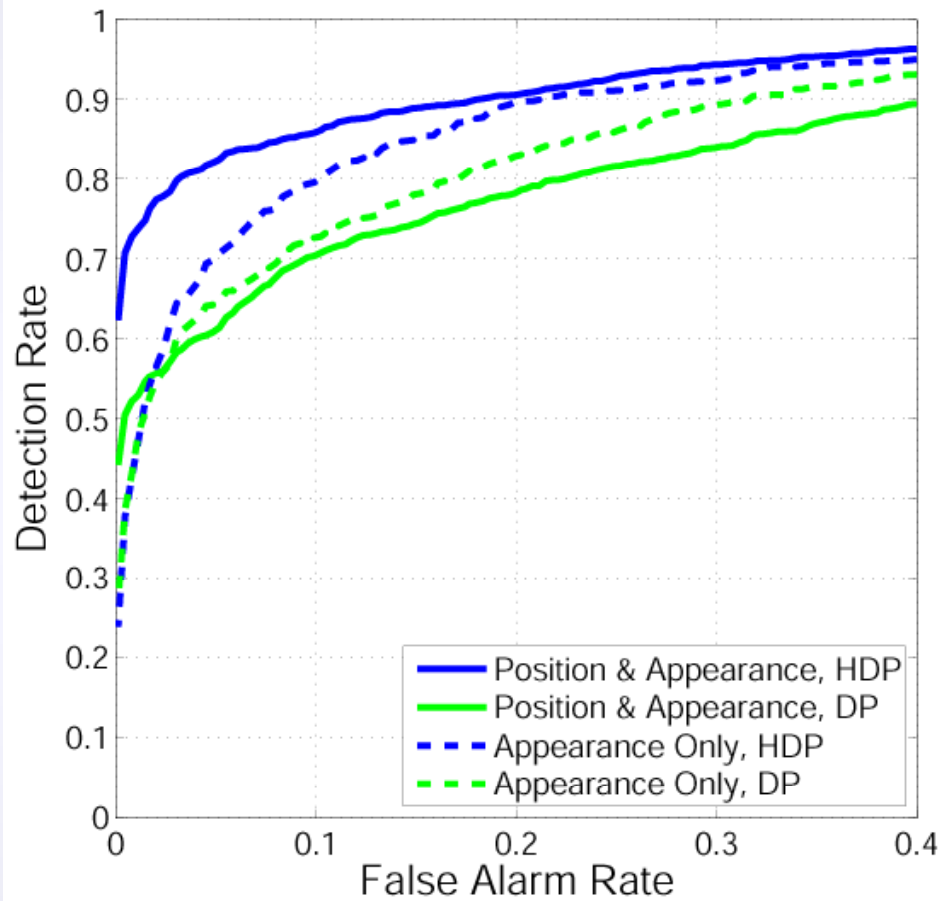


Shared Parts  
*more accurate than*  
Unshared Parts

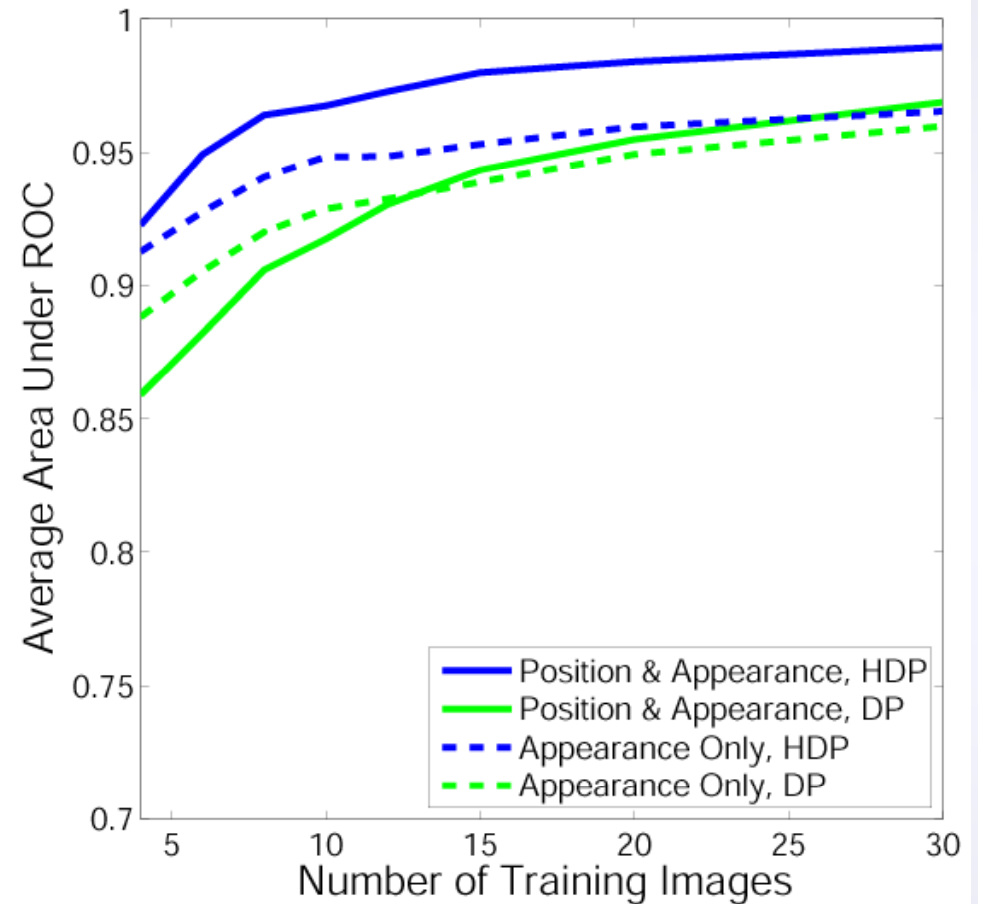
Modeling feature positions  
*improves shared* detection, but  
*hurts unshared* detection

6 Training Images per Category  
(ROC Curves)

# Detection Results

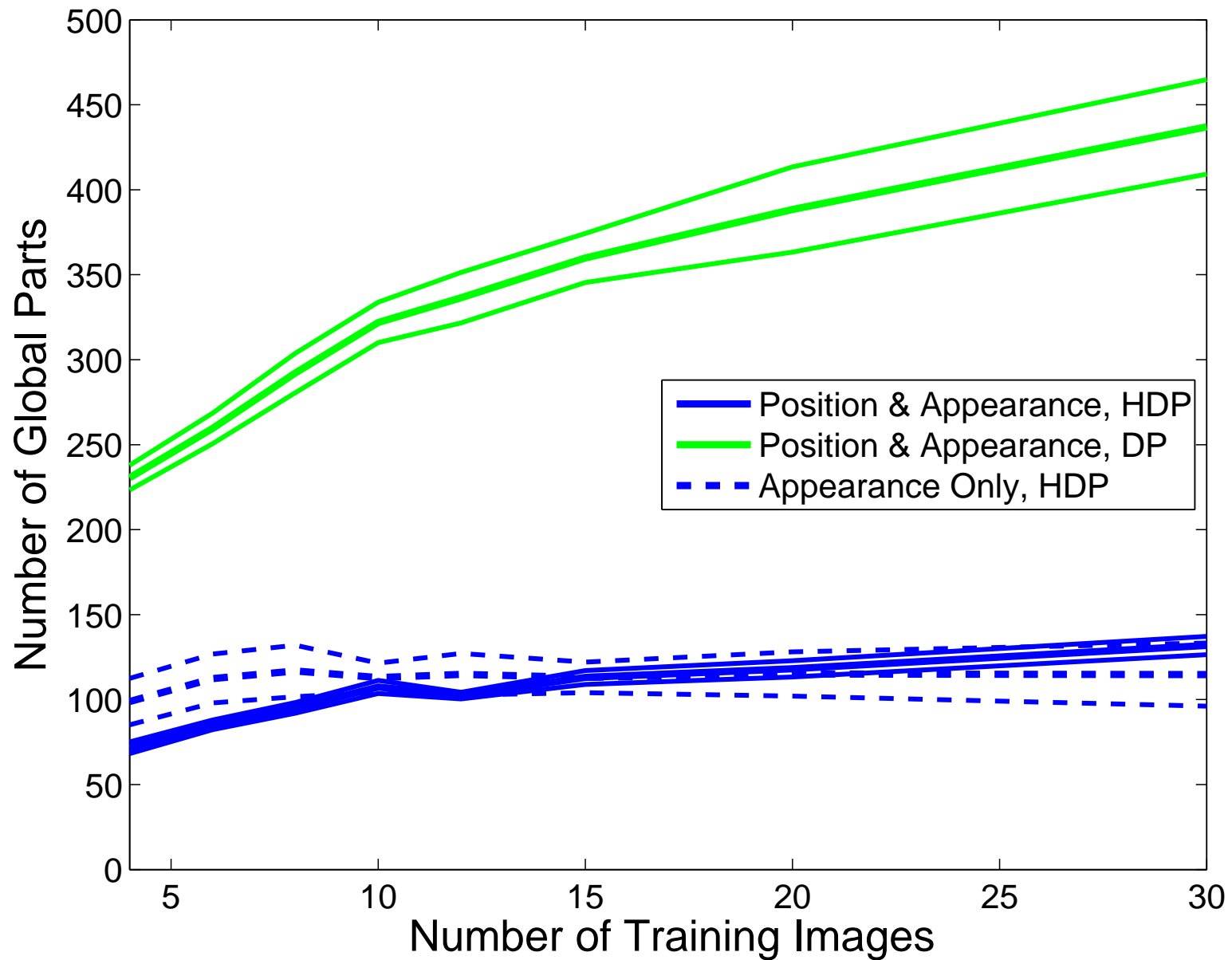


**6 Training Images per Category**  
*(ROC Curves)*



**Detection vs. Training Set Size**  
*(Area Under ROC)*

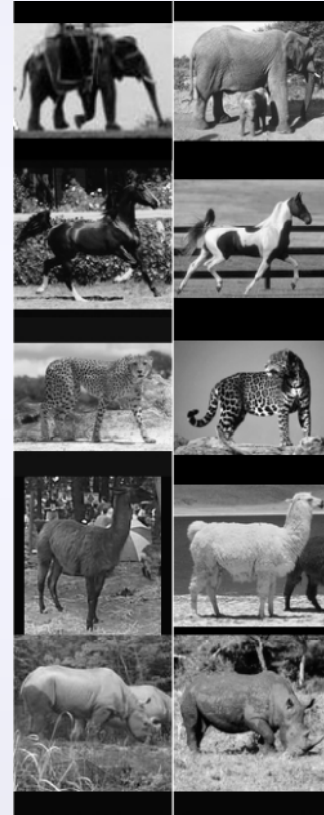
# Sharing Simplifies Models



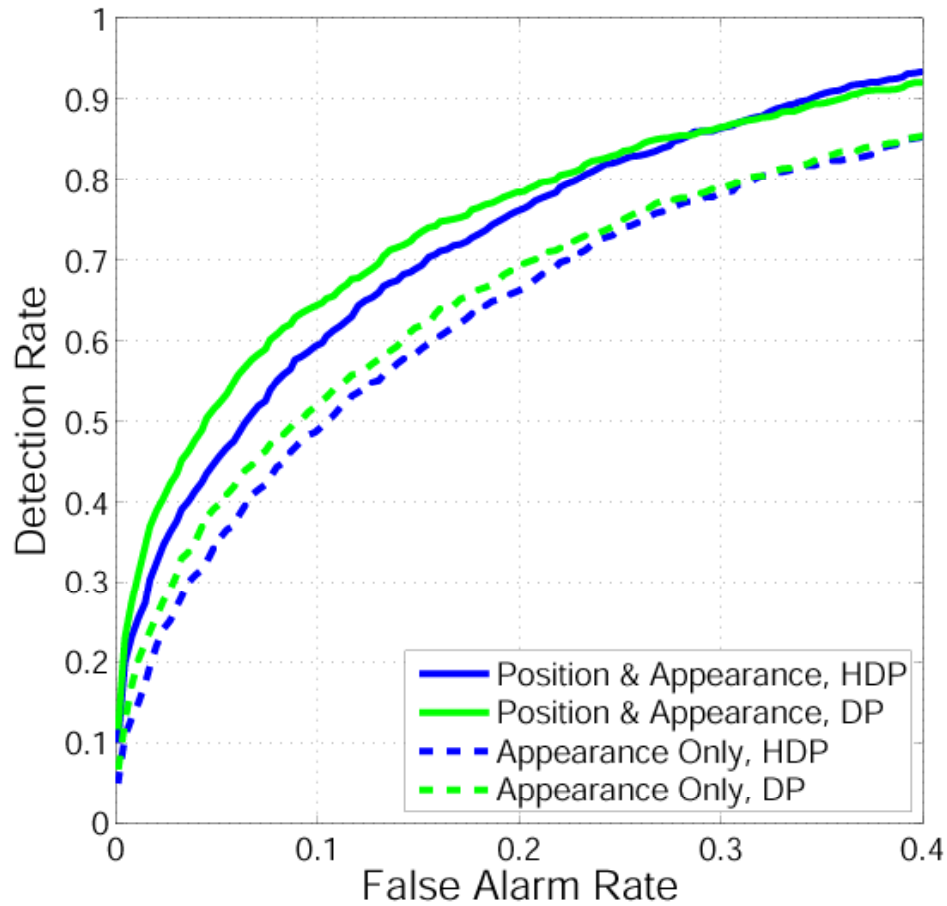
# Recognition Task



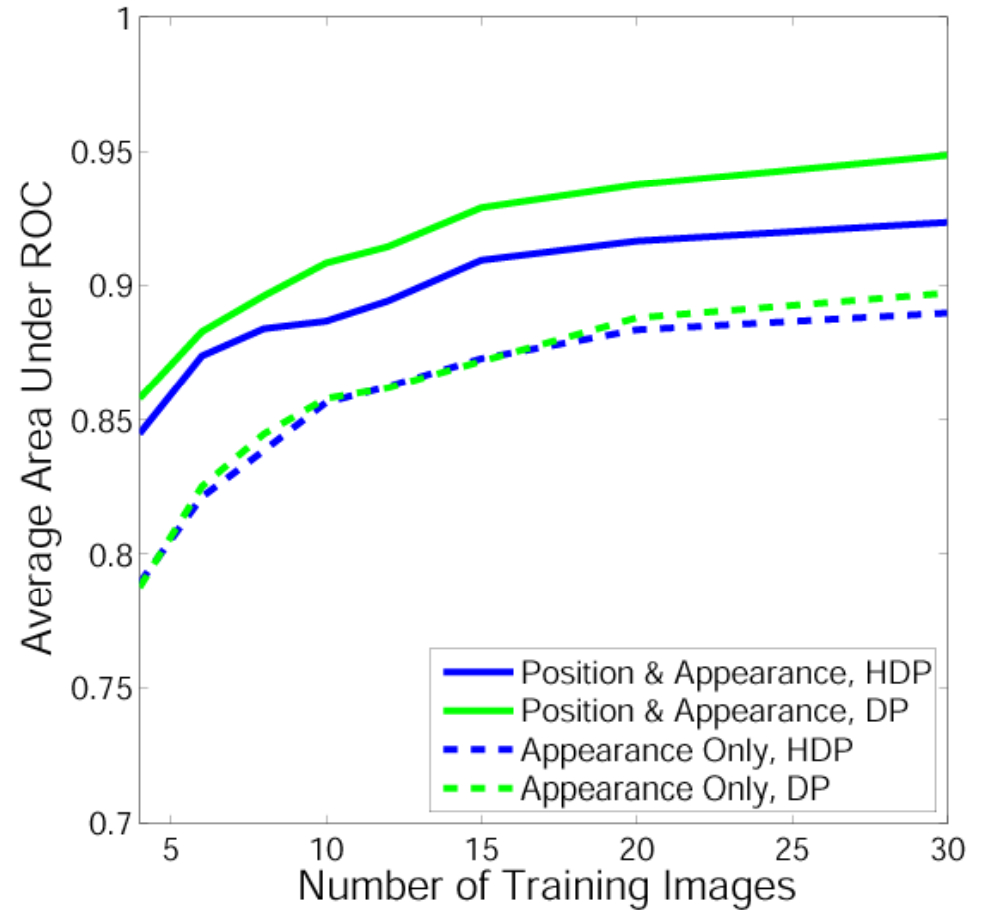
V  
O  
R  
S  
H  
S



# Recognition Results



**6 Training Images per Category**  
(ROC Curves)



**Detection vs. Training Set Size**  
(Area Under ROC)



# Outline

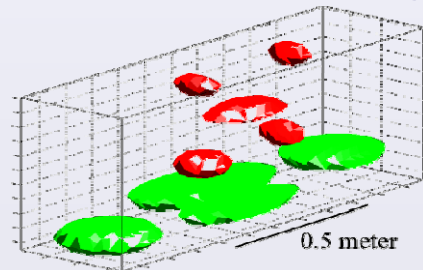
## Object Recognition with Shared Parts

- Learning parts via Dirichlet processes
- Hierarchical DP model for 16 object categories

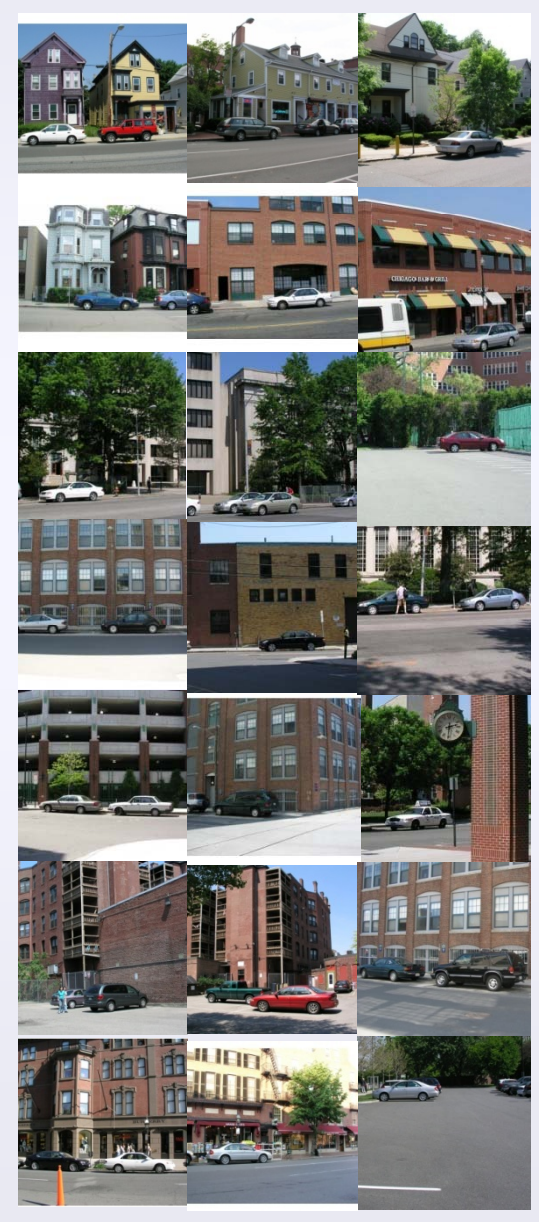


## Multiple Object Scenes

- Transformed Dirichlet processes
- Part-based models for 2D scenes
- Joint object detection & 3D reconstruction



# Semi-supervised Learning



# Object vs. Visual Categories

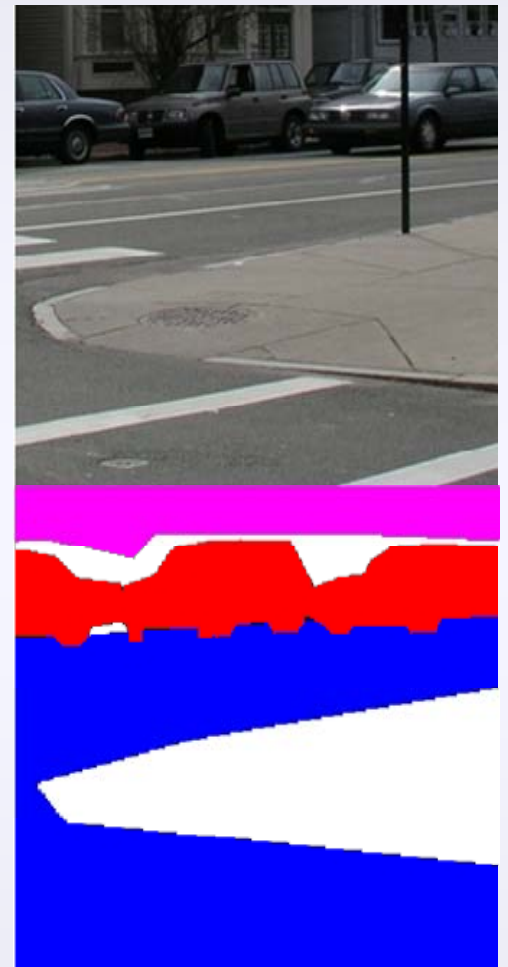
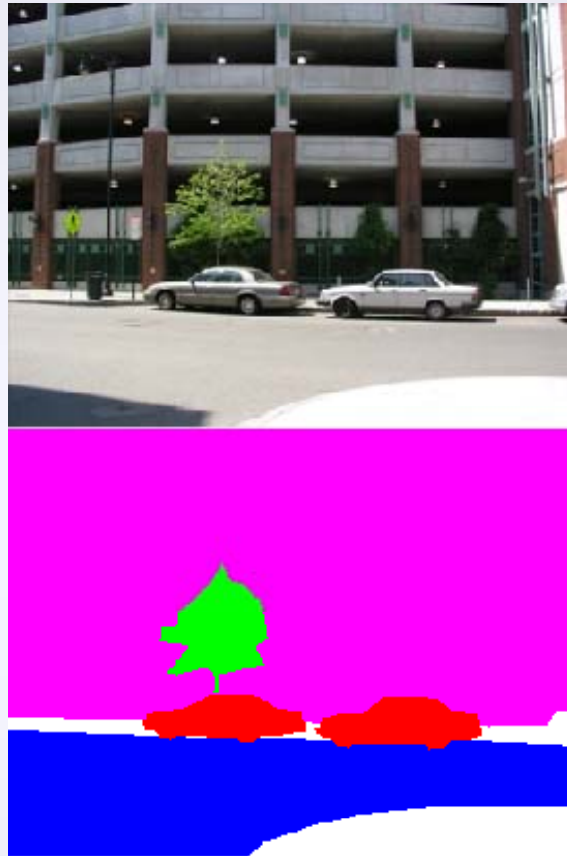
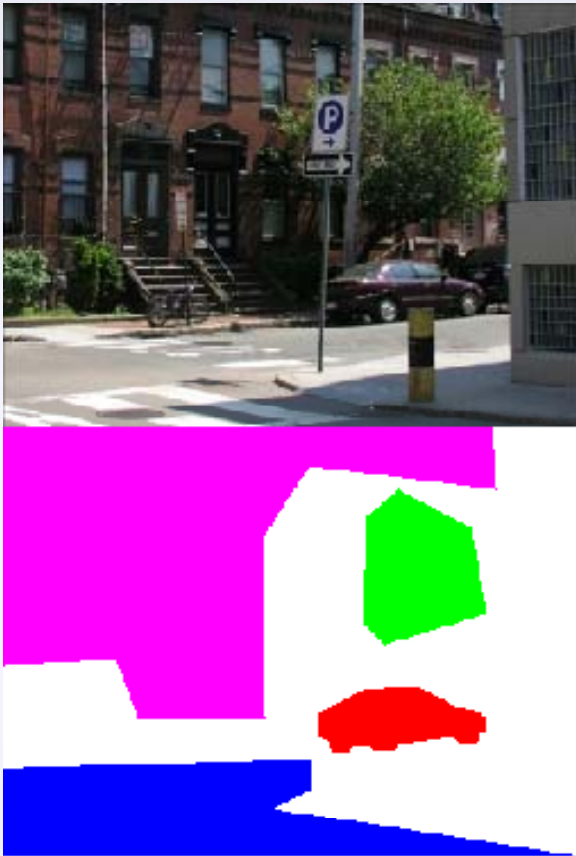
Supervised



Unsupervised

- Assume training data contains object category labels
- Discover underlying visual categories automatically

# Multiple Object Scenes



- How many cars are there?
- Where are those cars in the scene?

*Standard dependent Dirichlet process models (Gelfand et. al., 2005) inappropriate*

# Spatial Transformations

- Let global DP clusters model objects in a *canonical* coordinate frame
- Generate images via a random *set of transformations*:

$$\tau((\mu, \Lambda); \rho) = (\mu + \rho, \Lambda)$$



Parameterized family  
of transformations



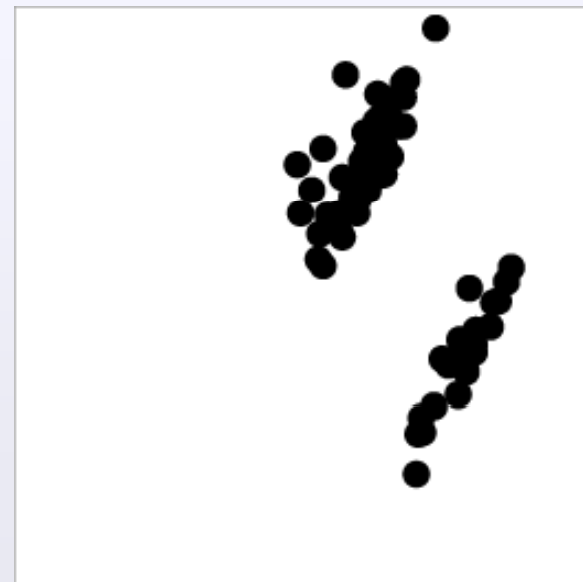
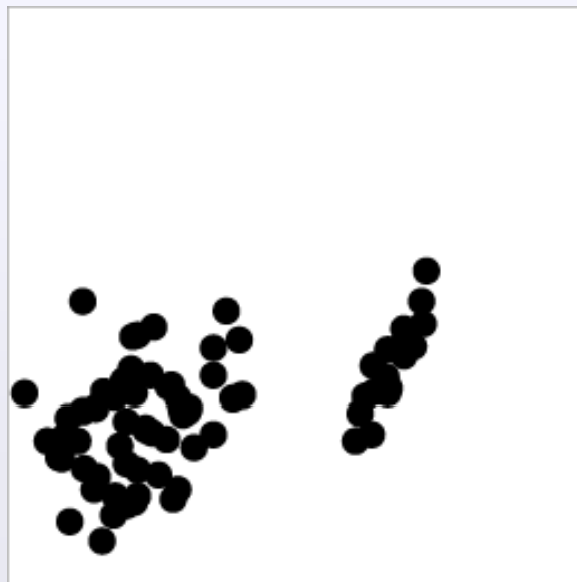
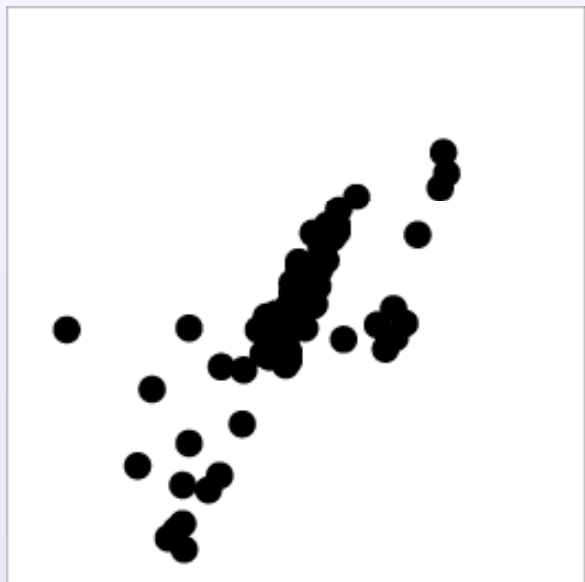
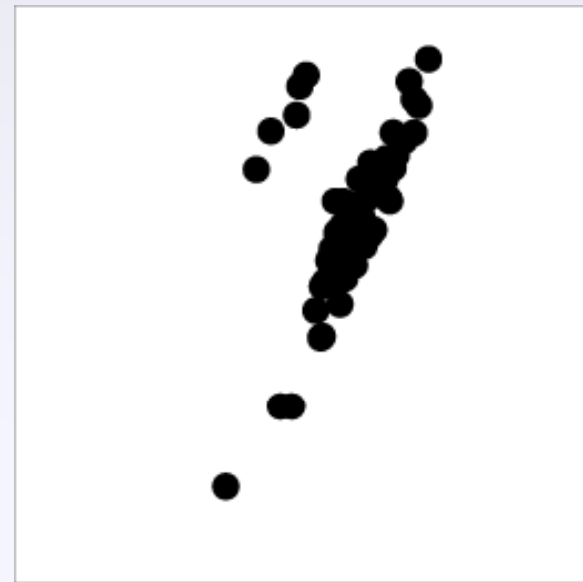
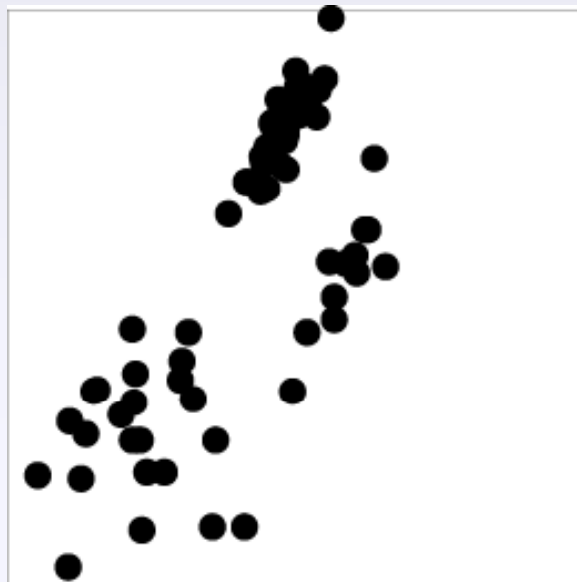
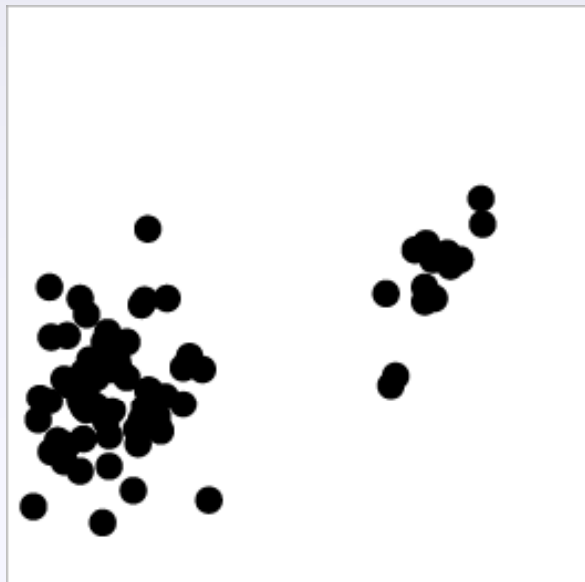
Shift cluster from canonical  
coordinate frame to object  
location in a given image



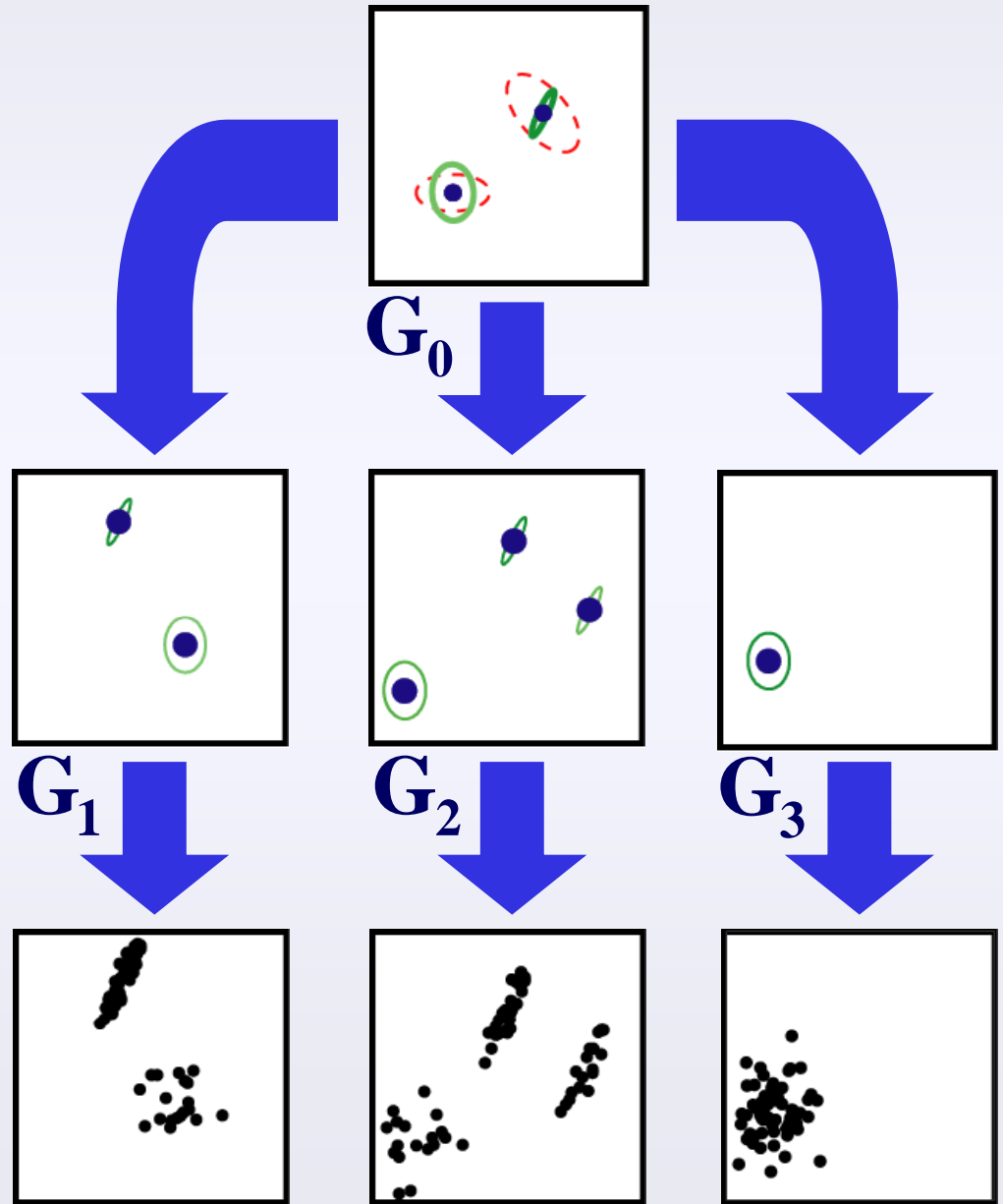
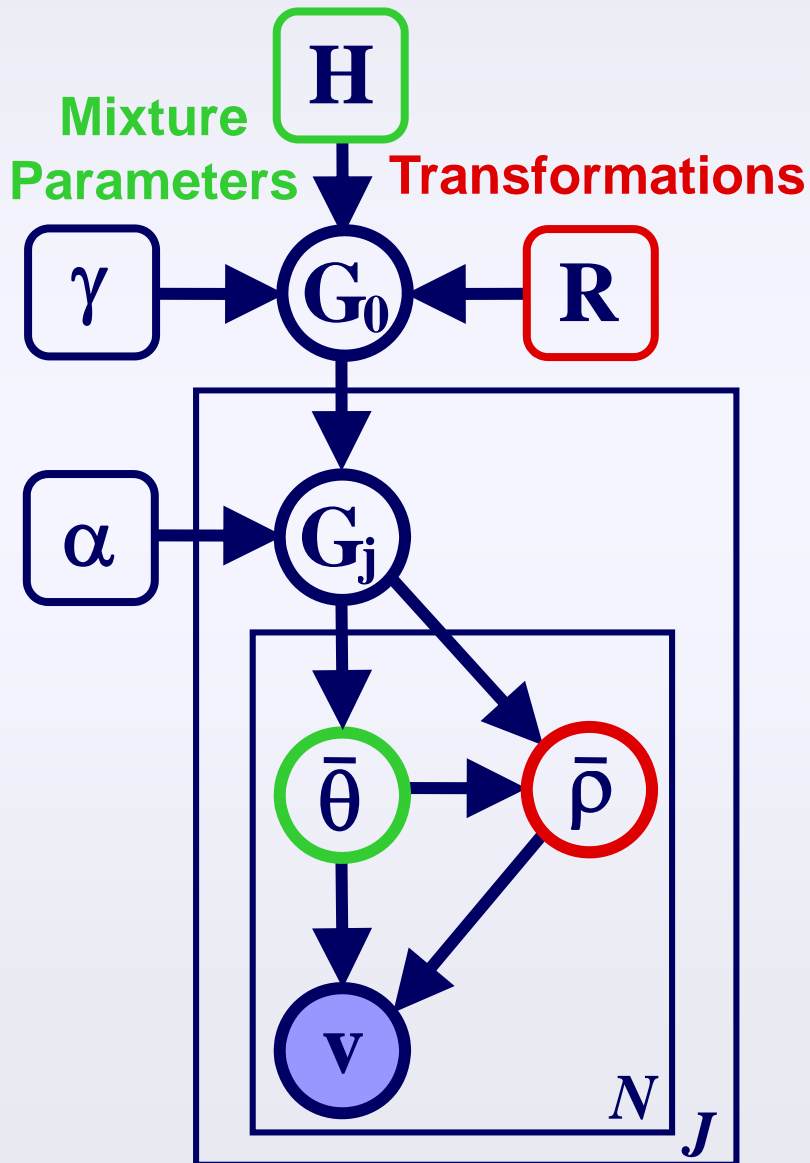
**Layered Motion Models** (Wang & Adelson, Jojic & Frey)

**Nonparametric Transformation Densities** (Learned-Miller & Viola)

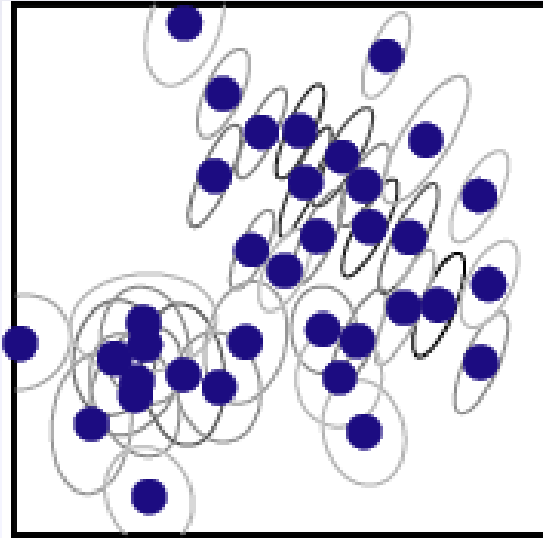
# A Toy World: Bars & Blobs



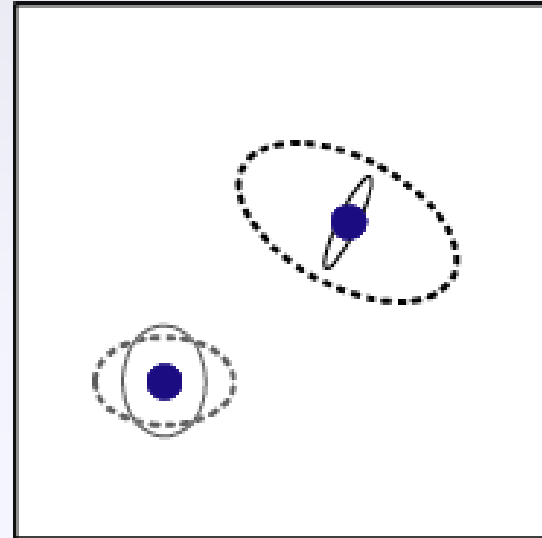
# Transformed Dirichlet Process



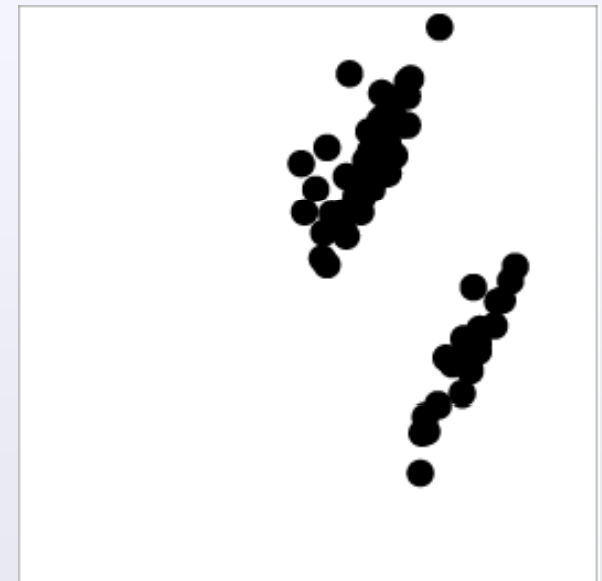
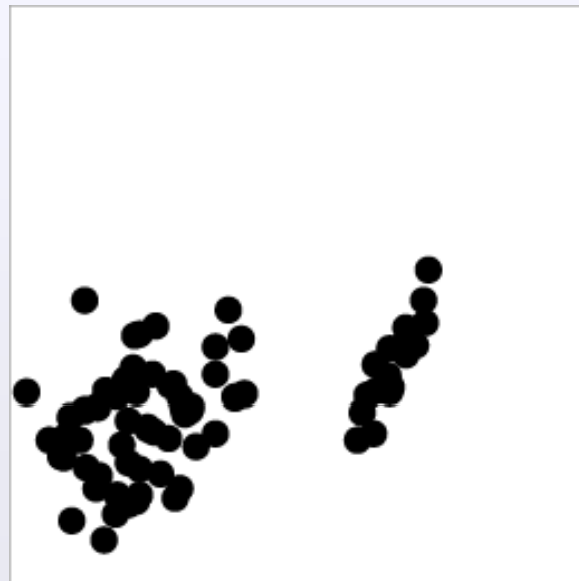
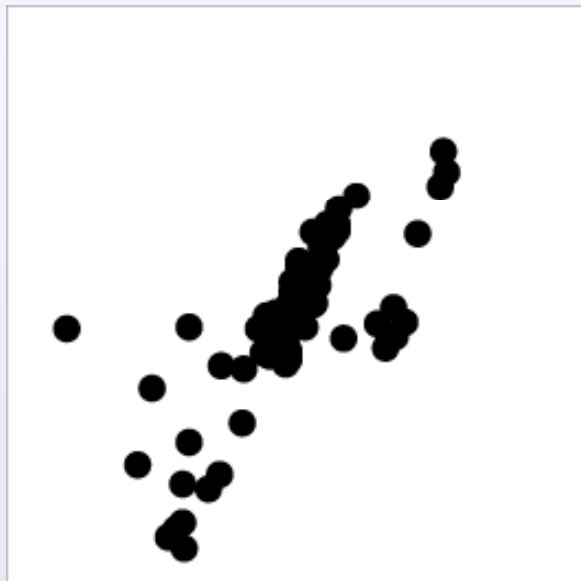
# Importance of Transformations



HDP

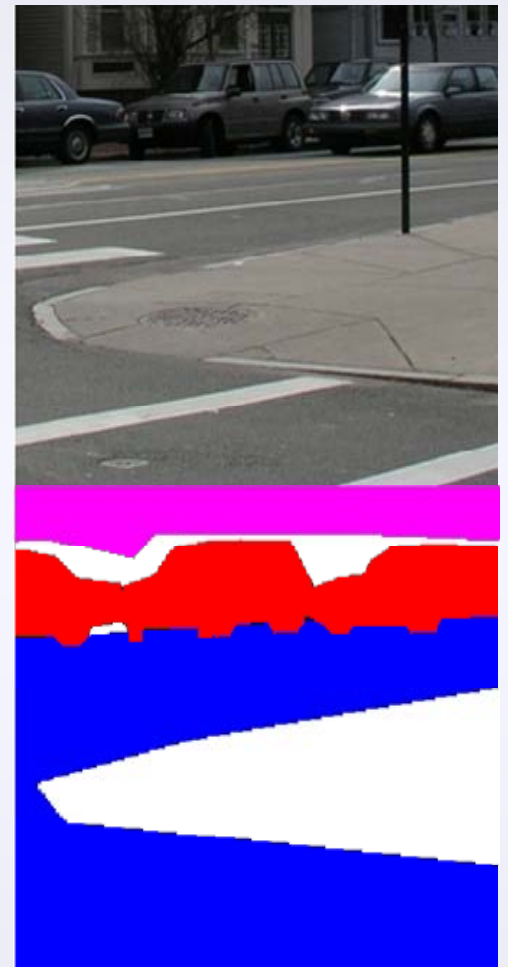
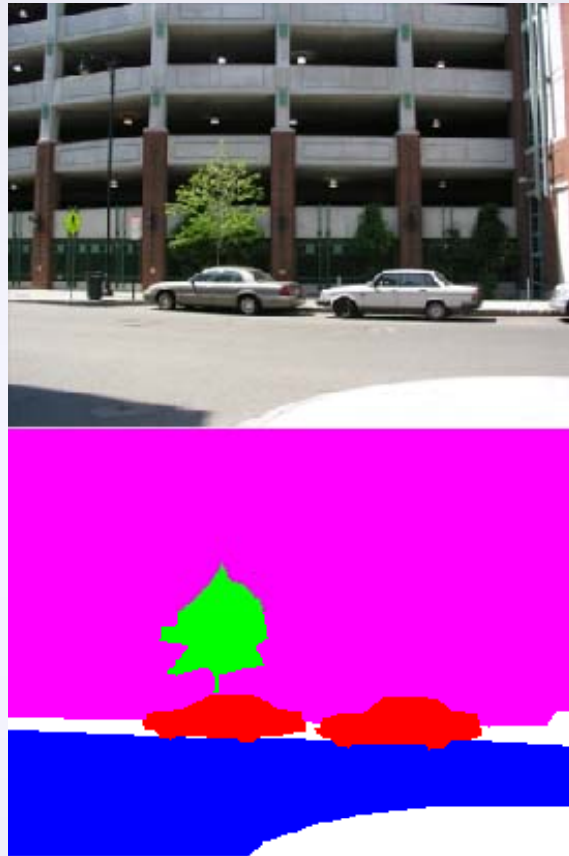
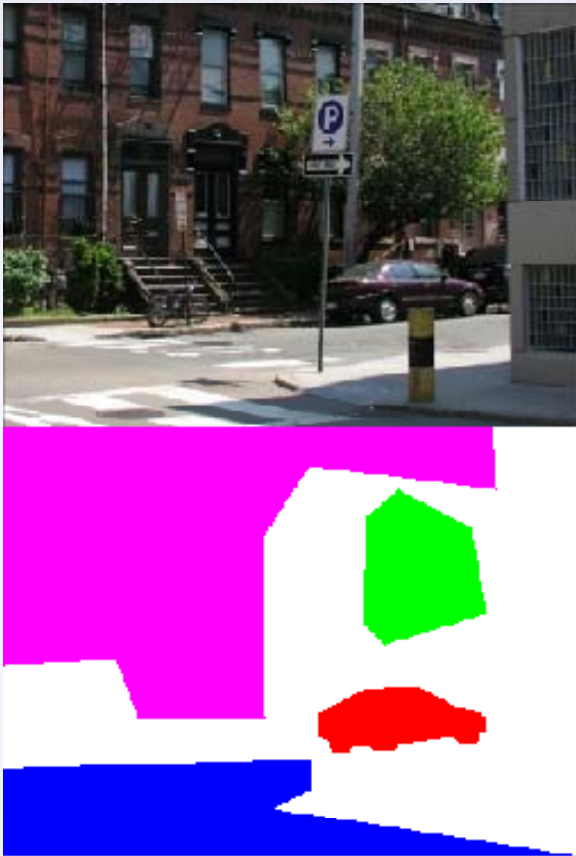


TDP





# Counting & Locating Objects

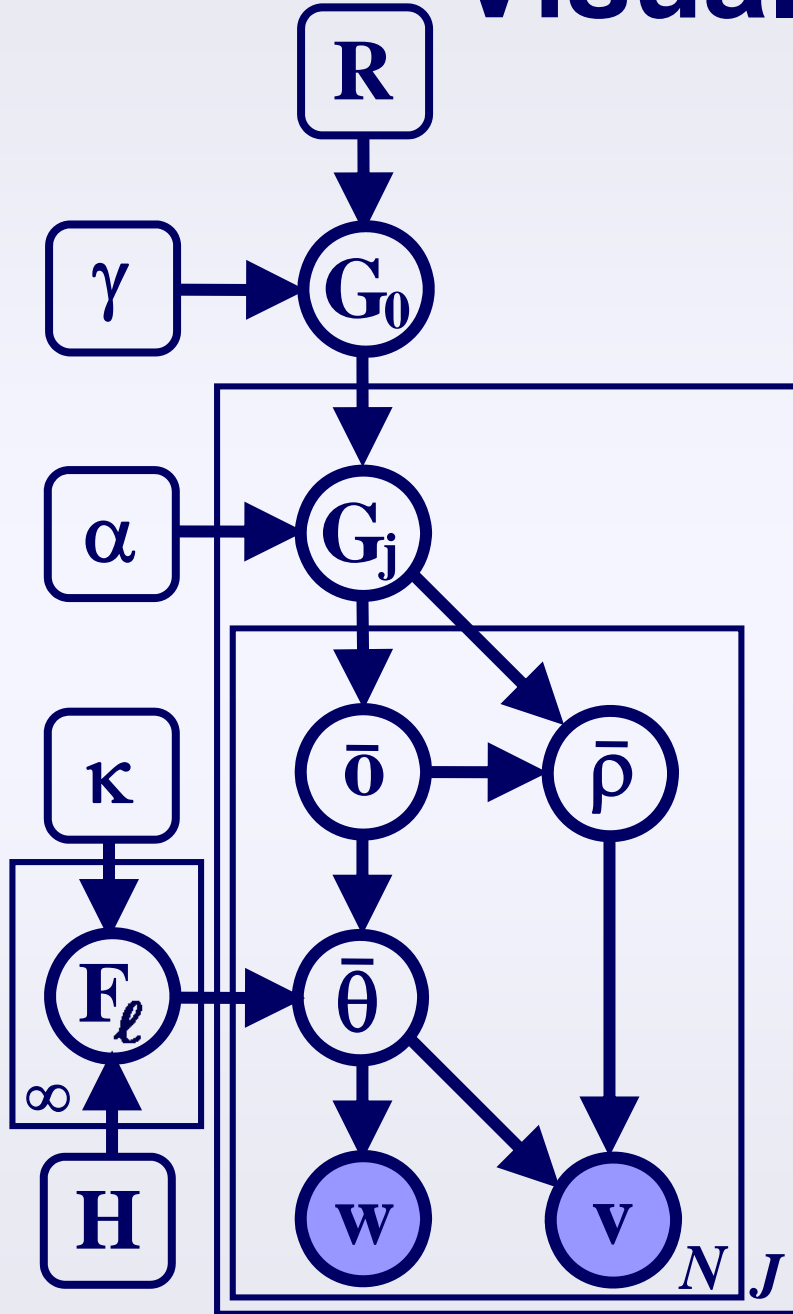


- How many cars are there?
- Where are those cars in the scene?

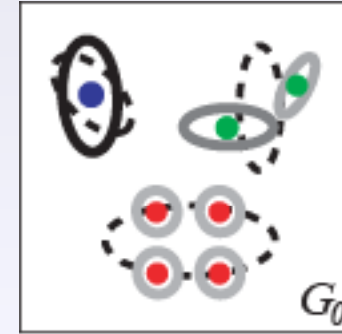
*Dirichlet Processes*

*Transformations*

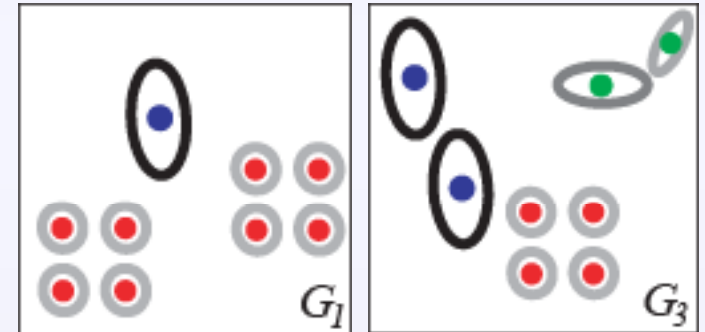
# Visual Scene TDP



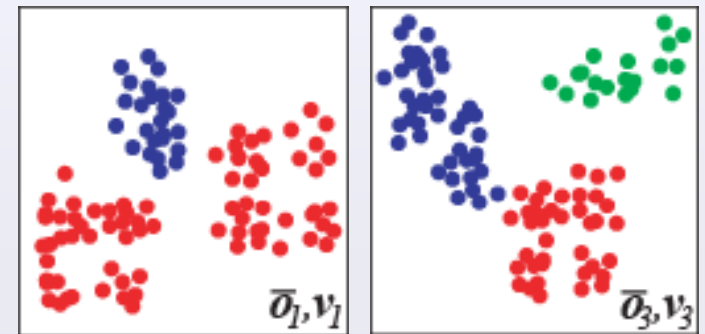
**Global Density**  
 Object category  
 Part size & shape  
 Transformation prior



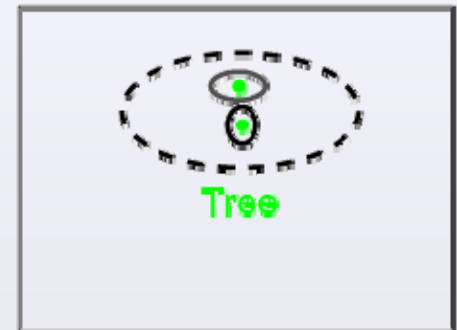
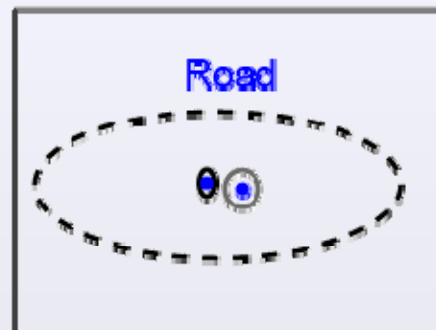
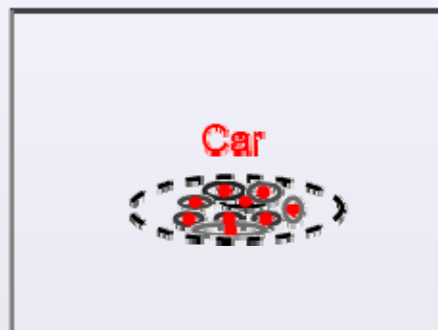
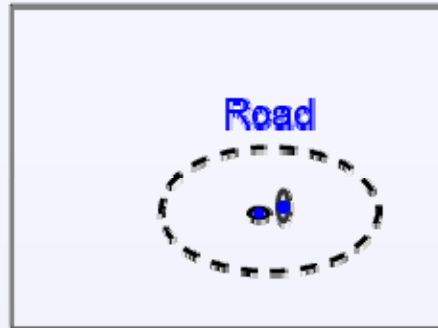
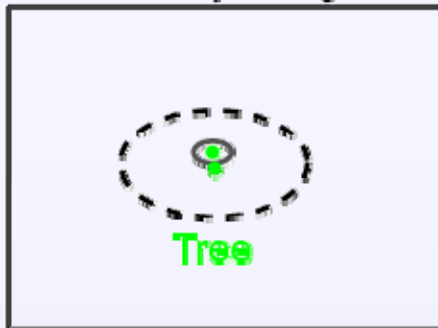
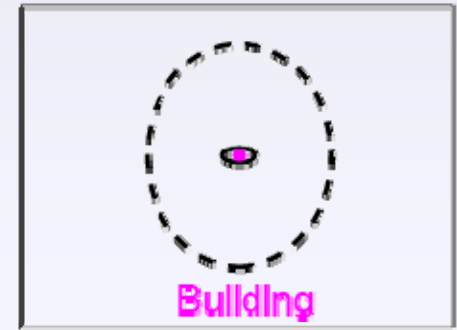
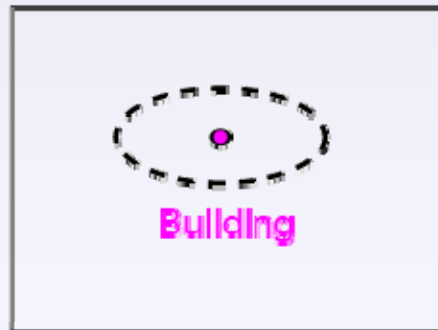
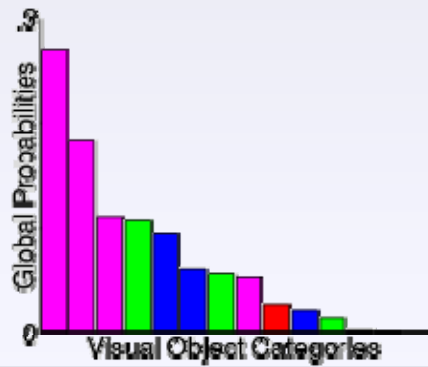
**Transformed Densities**  
 Object category  
 Part size & shape  
 Instance locations



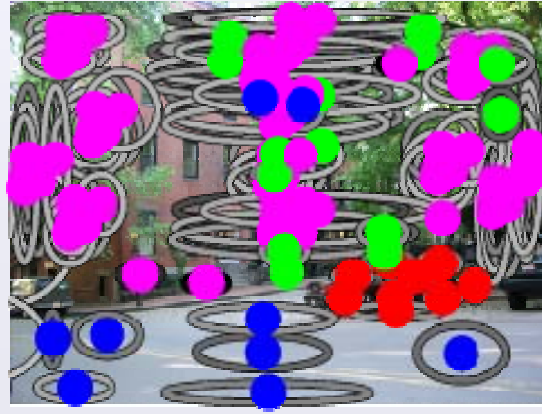
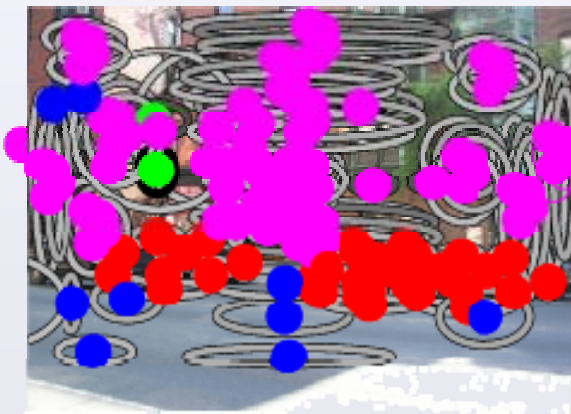
**2D Image Features**  
 Appearance  
 Location



# Street Scene Visual Categories



# Street Scene Segmentations

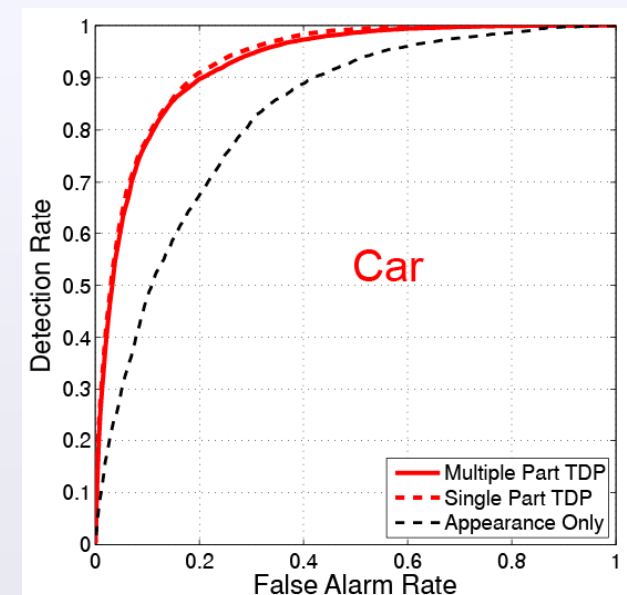
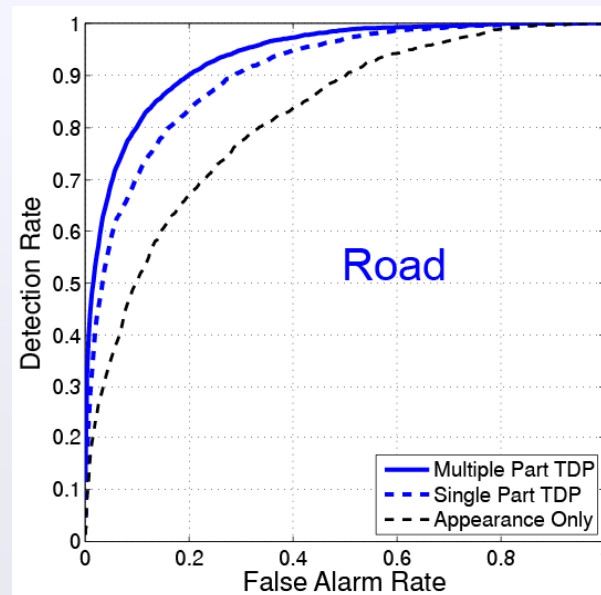
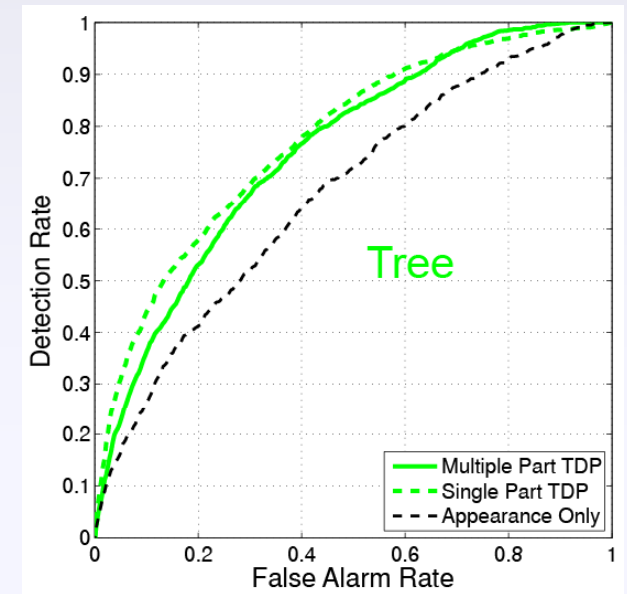
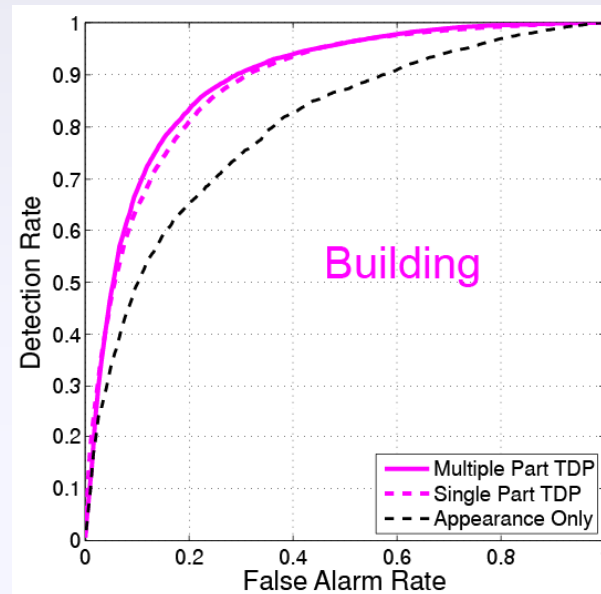


# Appearance Only



- “Bag of features” model, ignores feature positions
- Inferior segmentations, cannot count objects

# Segmentation Performance



# Objects & 3D Reconstruction



*An Office Scene*

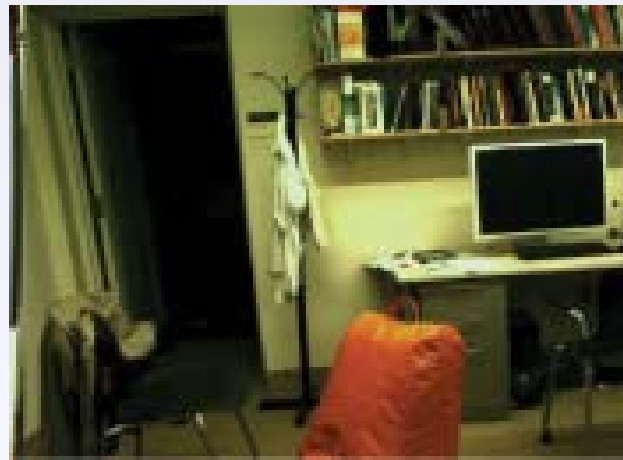
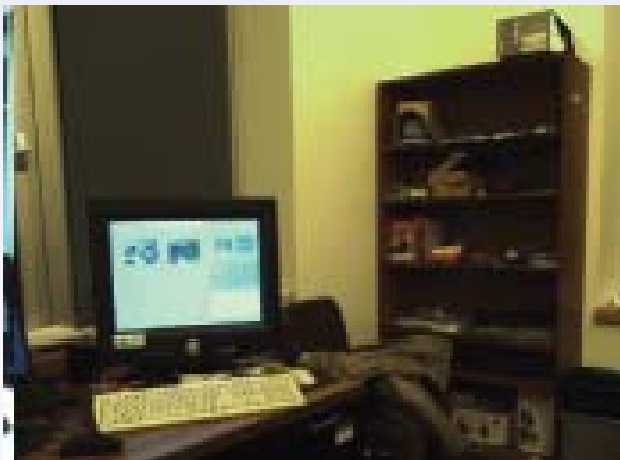
*Green* ↔ *Near*

*Red* ↔ *Far*

- Given 3D structure, segmentation is easier
- Identifying objects regularizes depth estimation

# Office Scene Training Images

*Objects at Multiple Scales*



**Computer Screens**

**Desks**

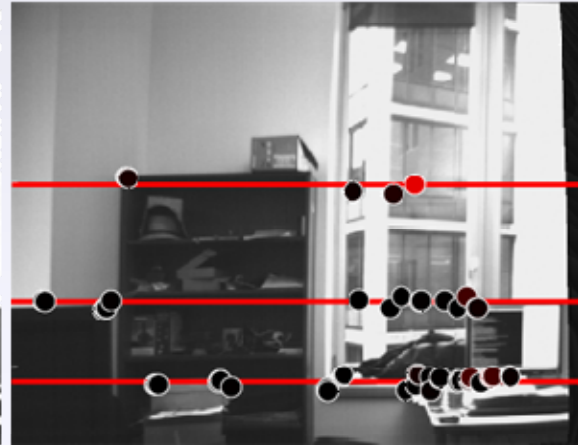
**Bookshelves**



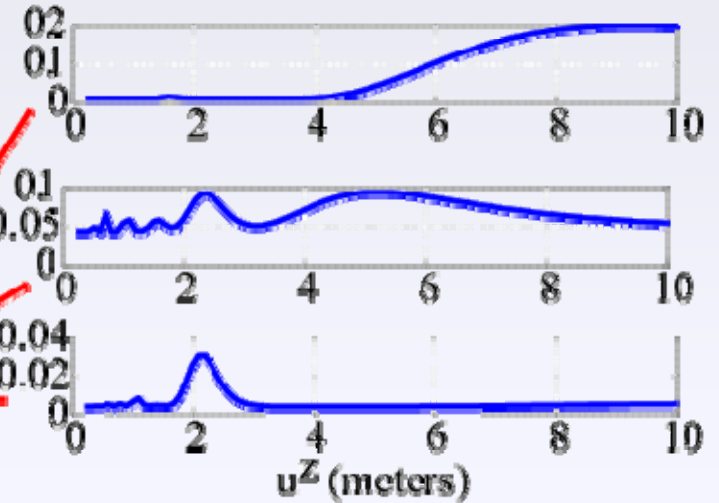
# 3D Structure from Stereo



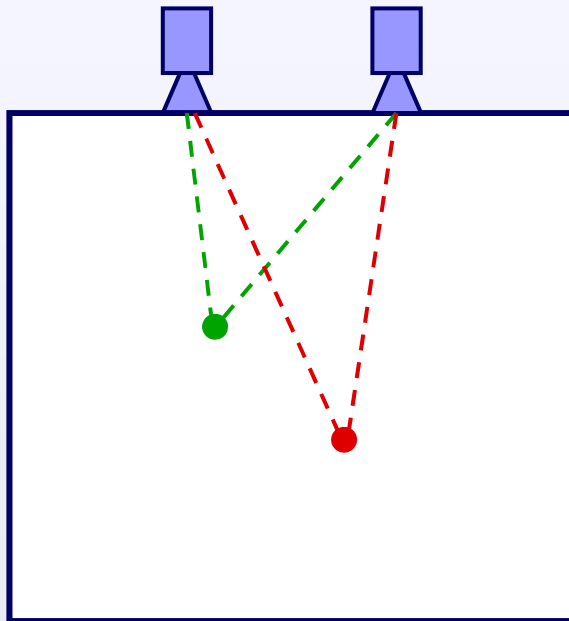
*Reference (left) Image*



*Potential Matches*



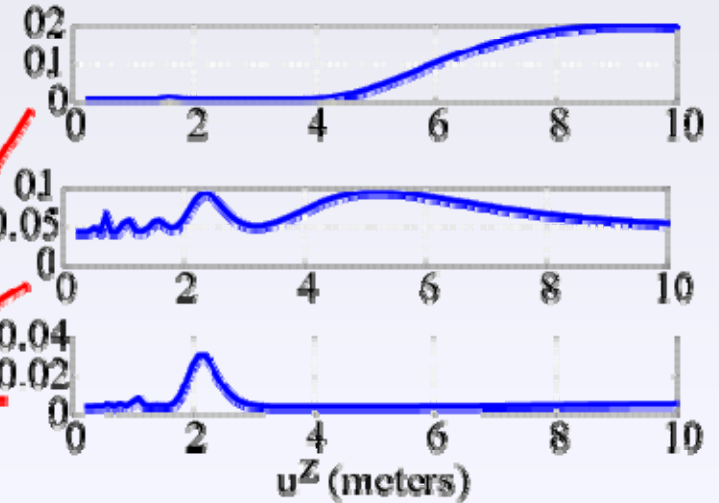
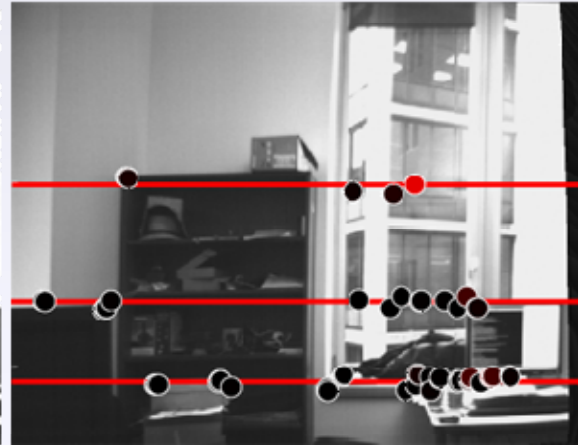
*Depth Densities*



*Overhead View*

$$\text{Depth} = \frac{\delta}{\text{Disparity}}$$

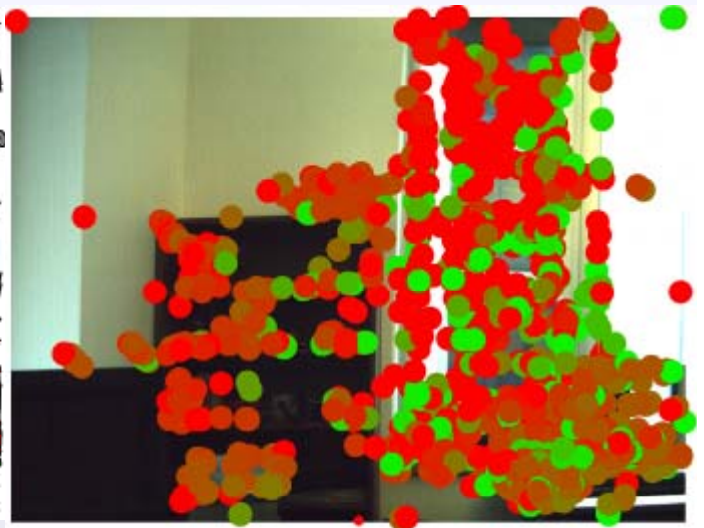
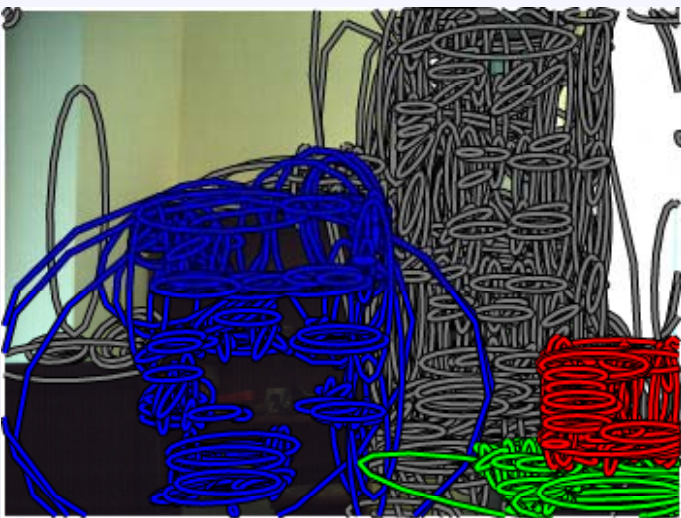
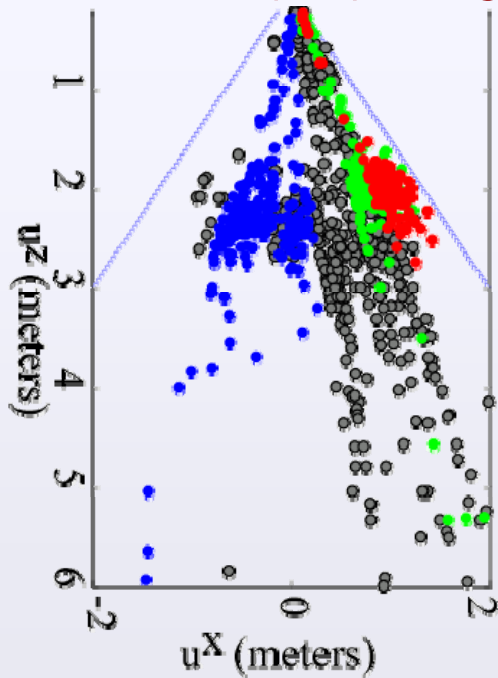
# Greedy Depth Estimates



Reference (left) Image

Potential Matches

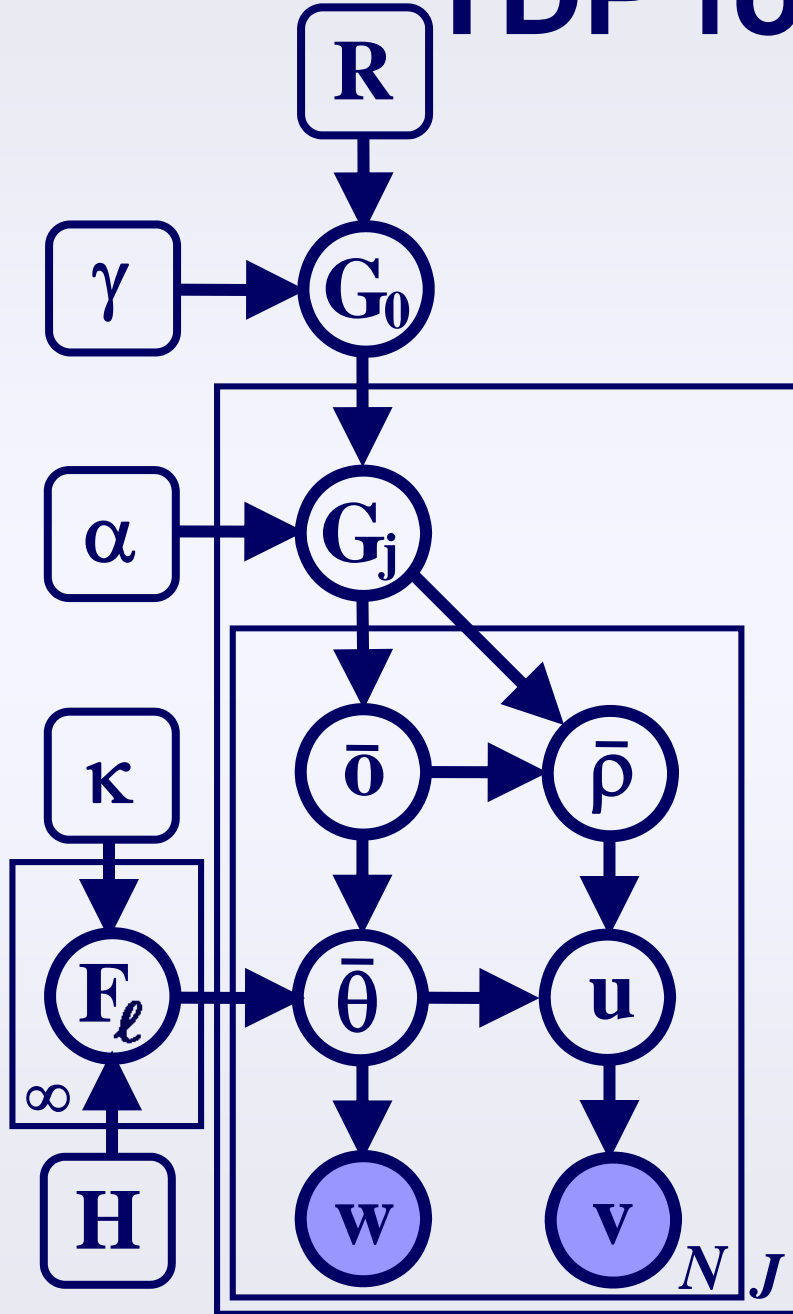
Depth Densities



Green  $\longleftrightarrow$  Near

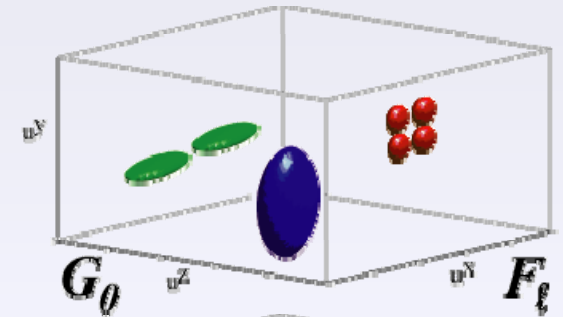
Red  $\longleftrightarrow$  Far

# TDP for 3D Scenes



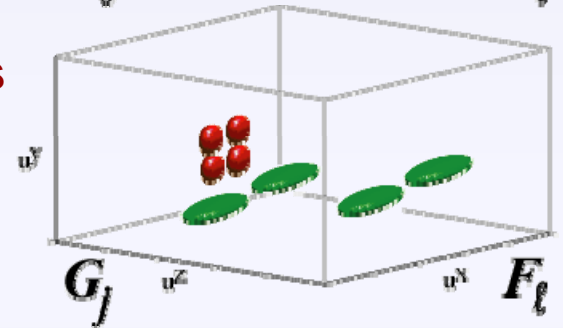
## Global Density

Object category  
Part size & shape  
Transformation prior



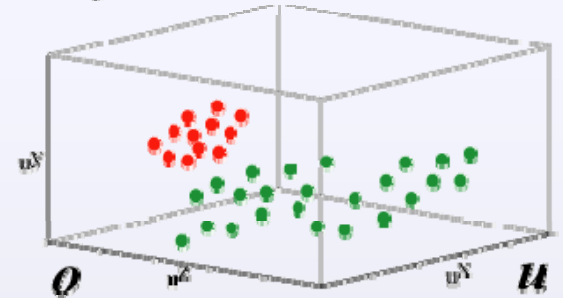
## Transformed Densities

Object category  
Part size & shape  
Transformed locations



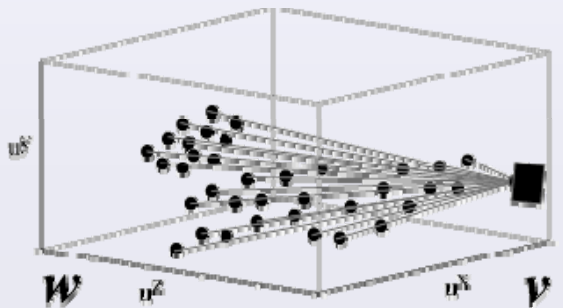
## 3D Scene Features

Object category  
3D Location

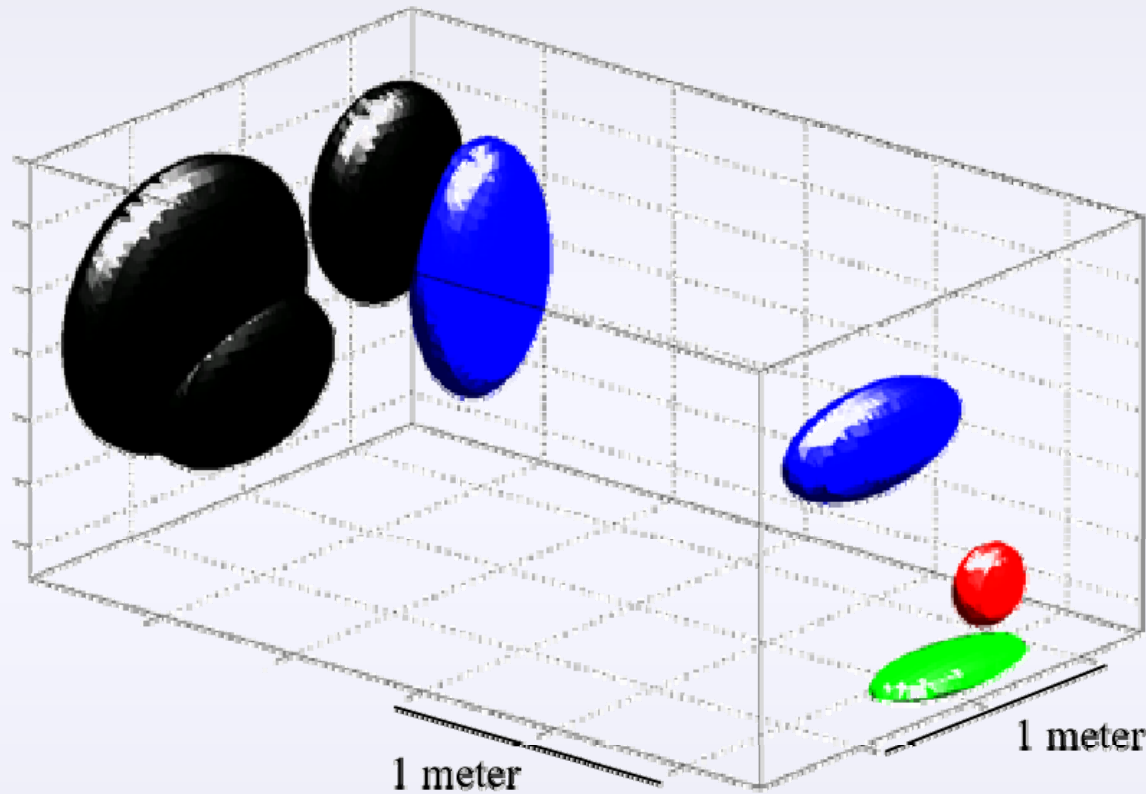


## 2D Image Features

Appearance Descriptors  
2D Pixel Coordinates



# Single-Part Office Scene Model

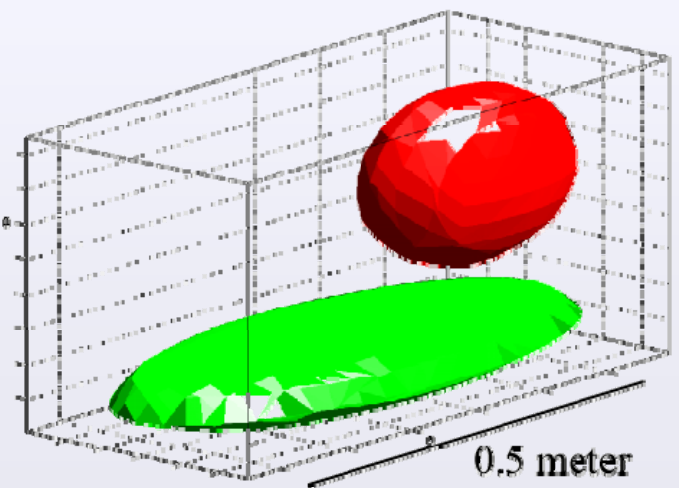
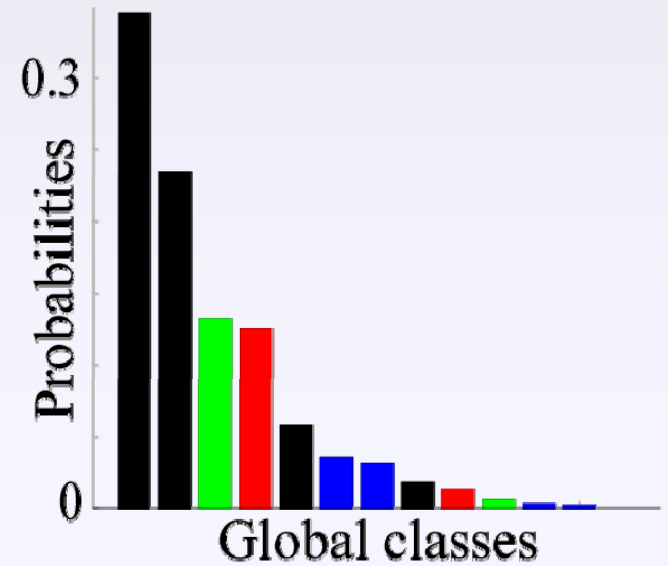


*Background*

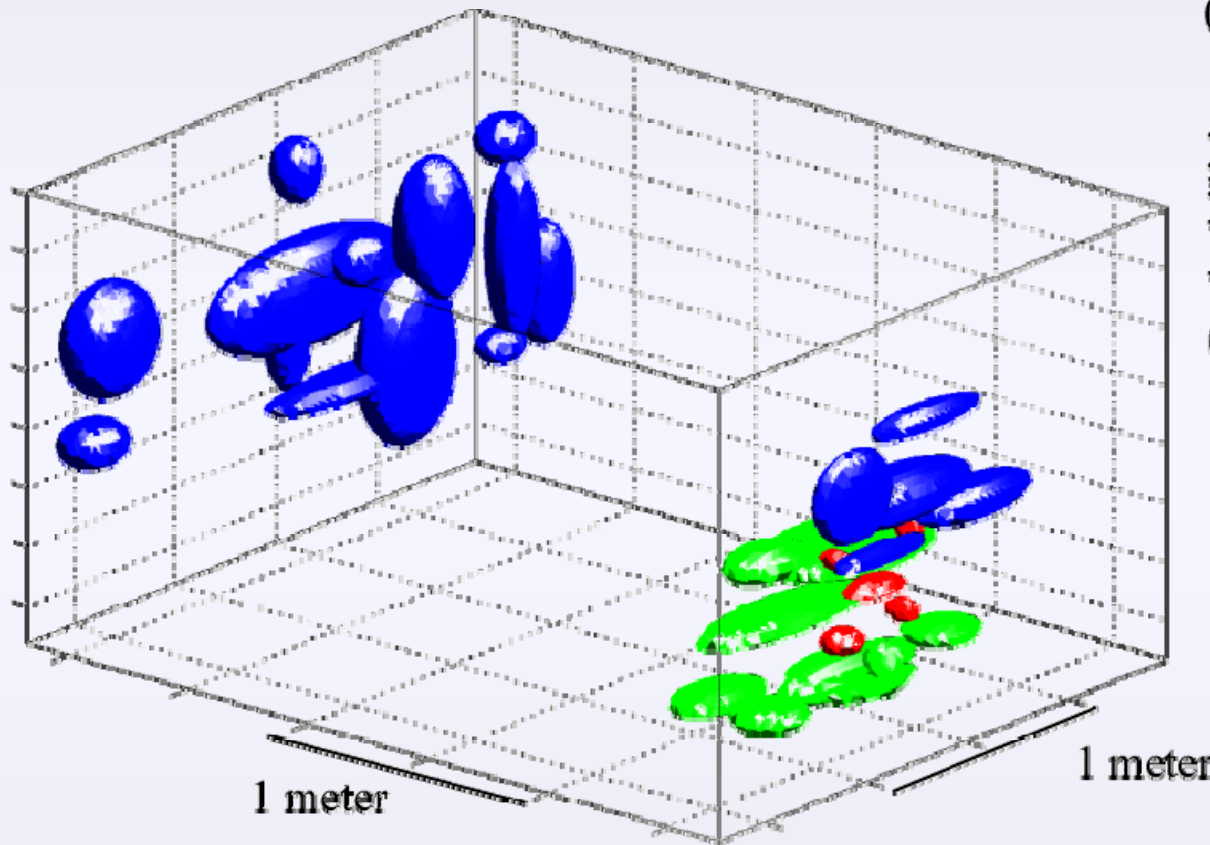
*Bookshelves*

*Computer Screen*

*Desk*



# Multi-Part Office Scene Model

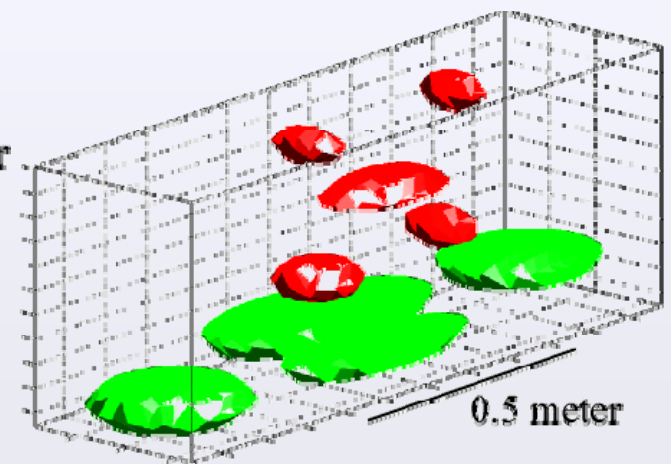
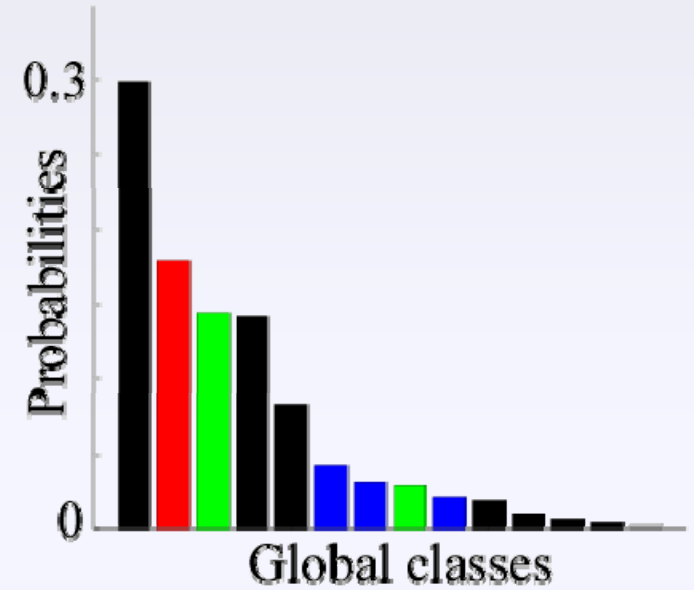


*Background*

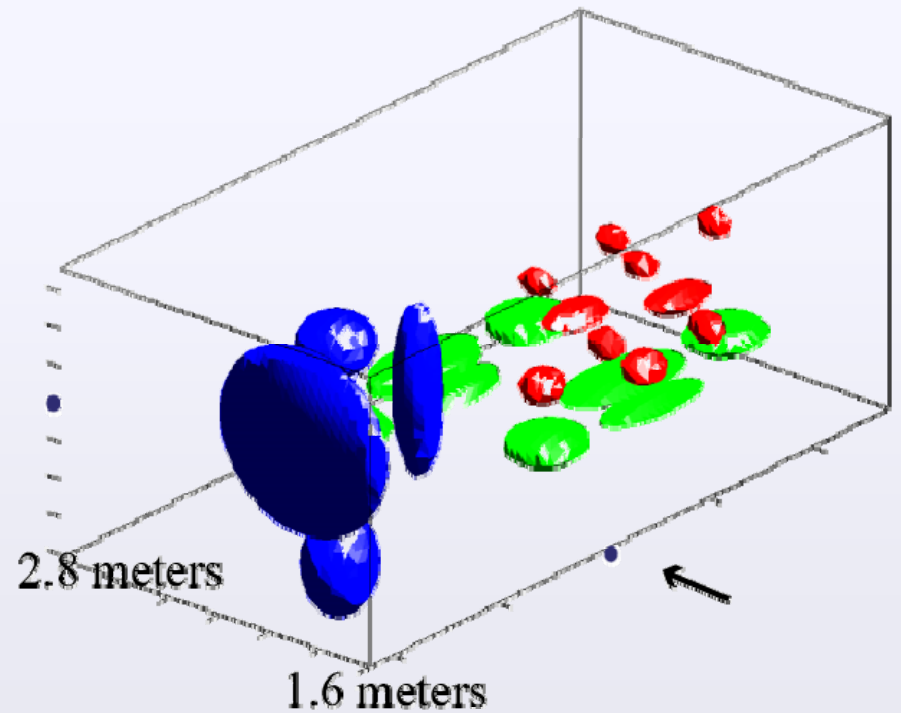
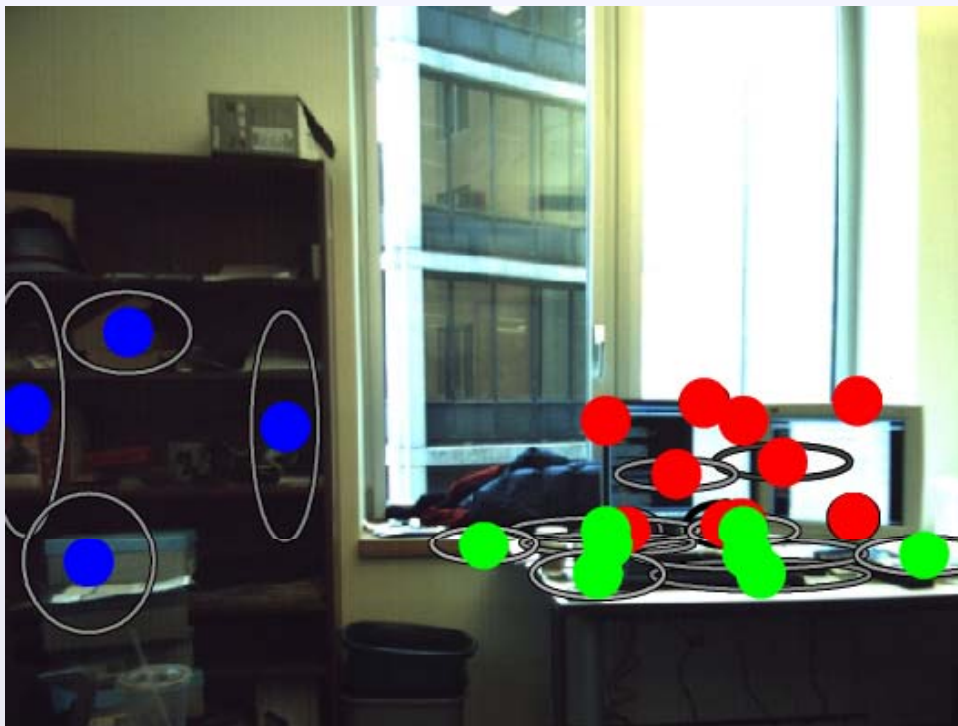
*Bookshelves*

*Computer Screen*

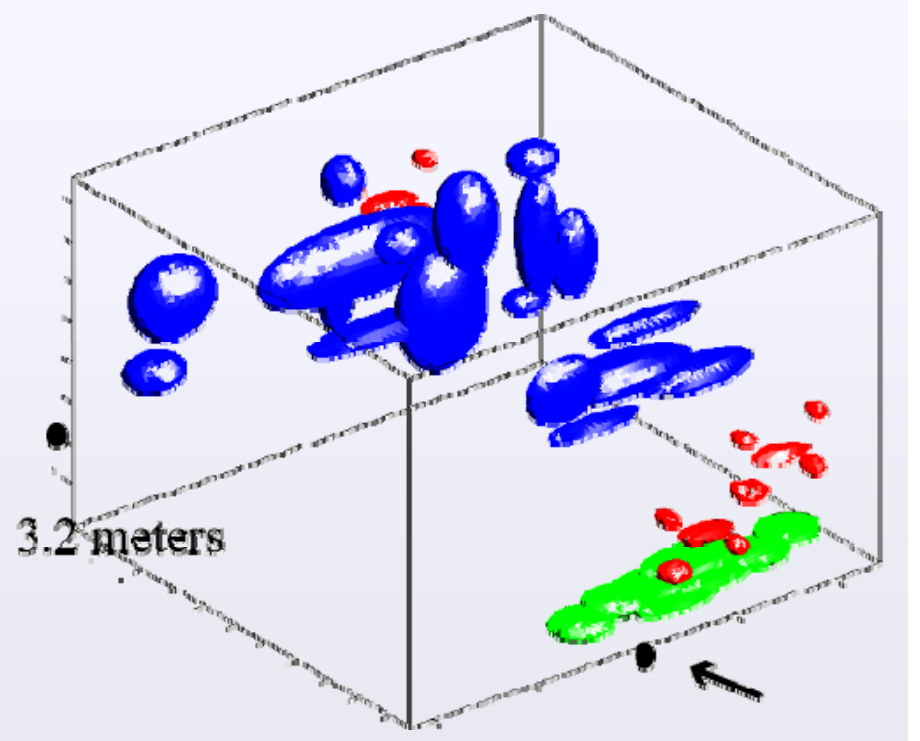
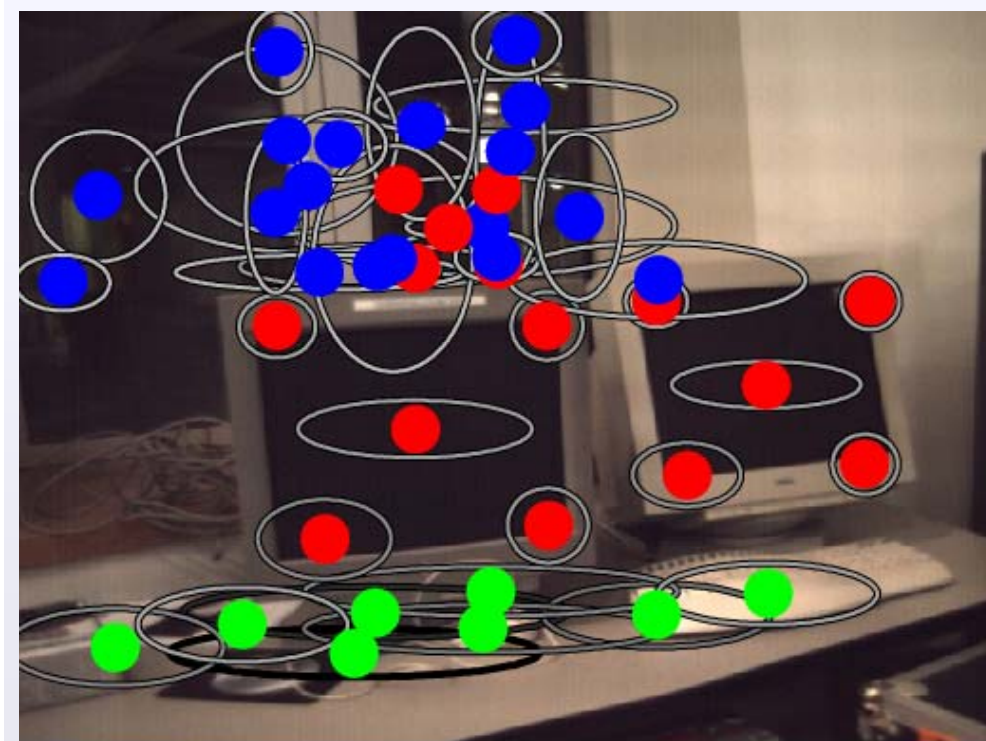
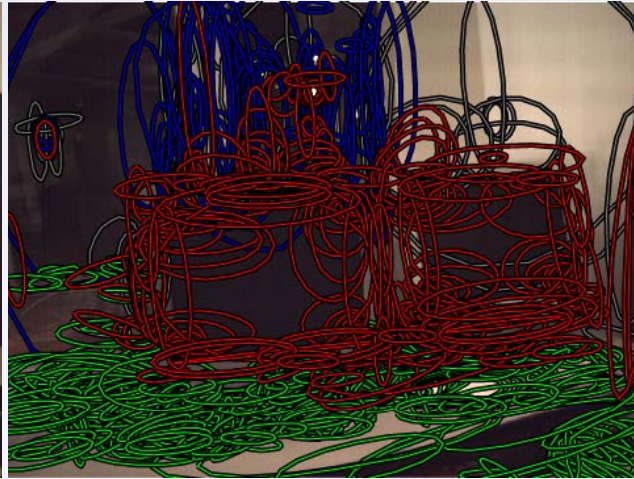
*Desk*



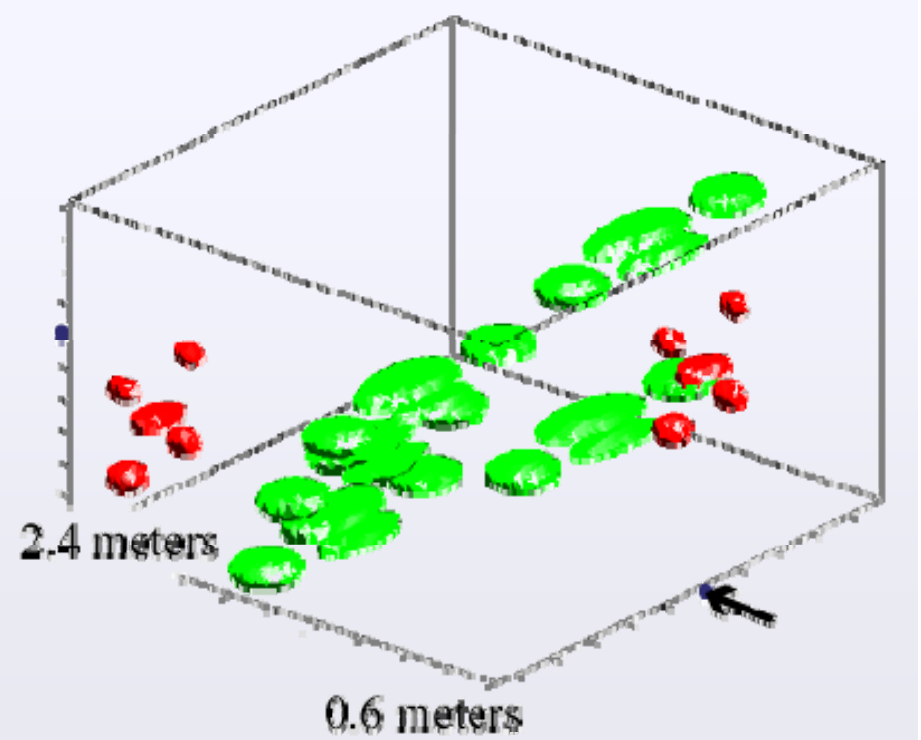
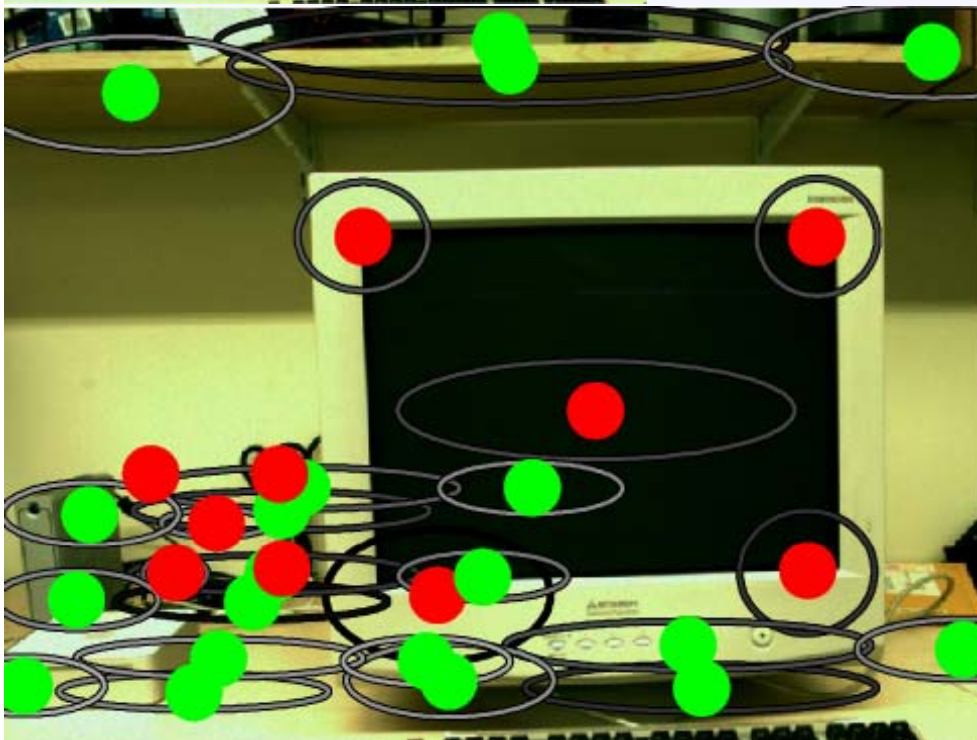
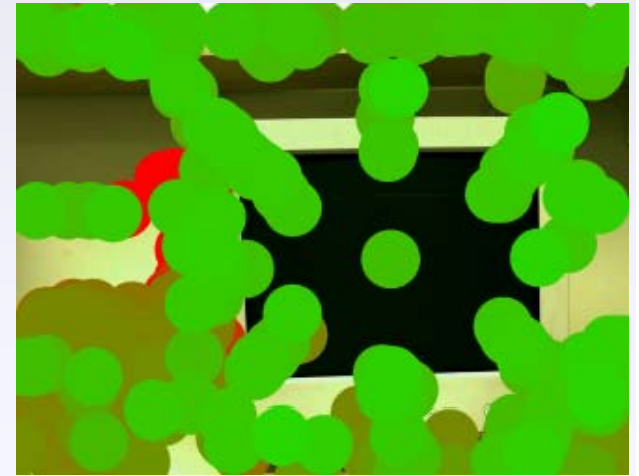
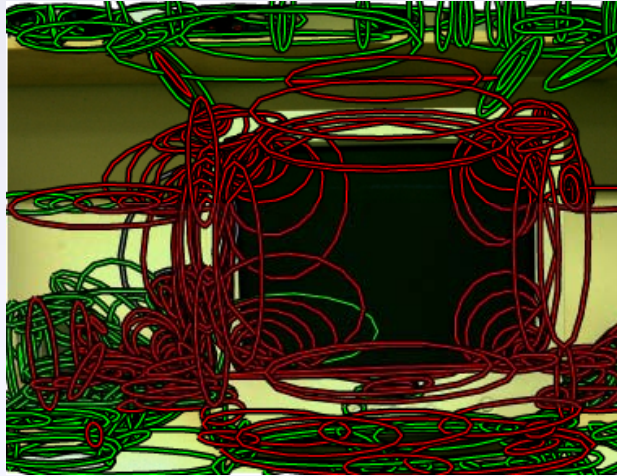
# Stereo Test Image I



# Stereo Test Image II

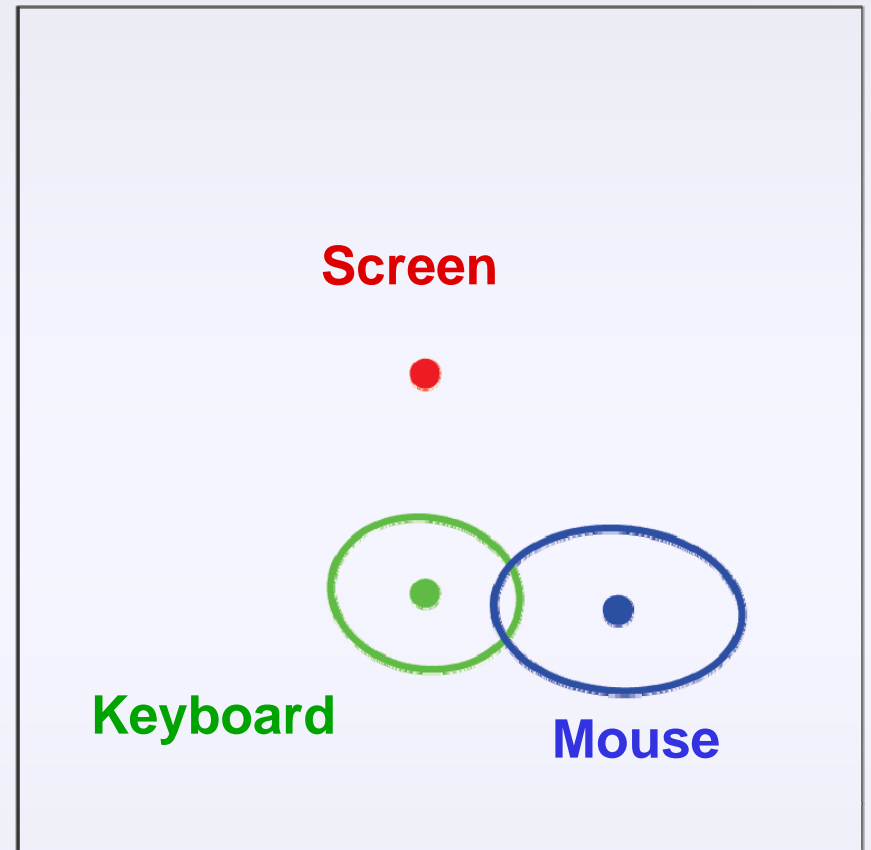


# Ongoing Work: Monocular Test





# Ongoing Work: Context

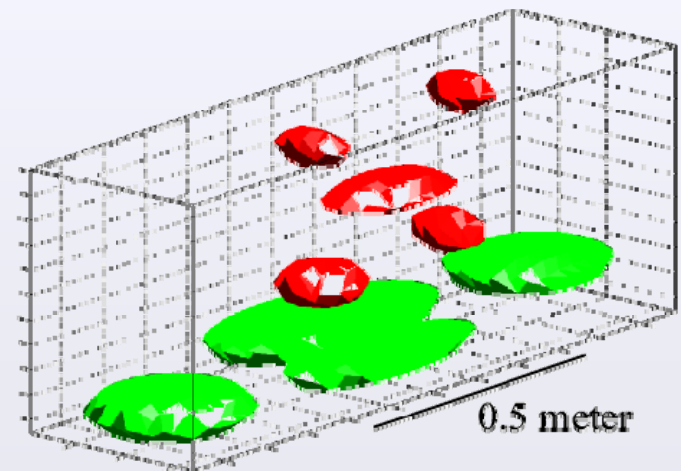
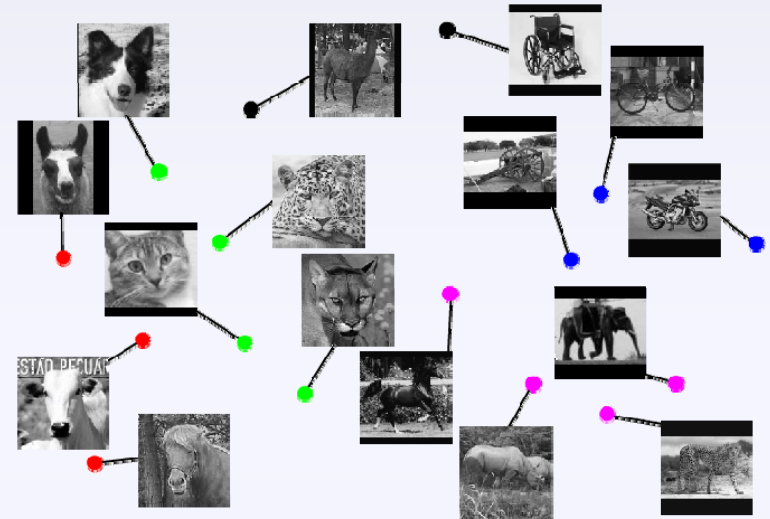


- Developed *fixed-order* contextual scene model
- Extension to Transformed DP model is an open problem
- Needed: Richer models for *background* scene structure

# Sudderth Conclusions

**Transformed Dirichlet Processes** allow...

- flexible *transfer* of knowledge among related object categories
- robust learning from small, *partially labeled* datasets
- an *integrated* view of object recognition & 3D reconstruction
- potential *scaling* of nonparametric methods to complex domains





# Learning a dense multi-view representation for detection, viewpoint classification and synthesis of object categories

\*H. Su   \*M. Sun   L. Fei-Fei   and   S. Savarese.



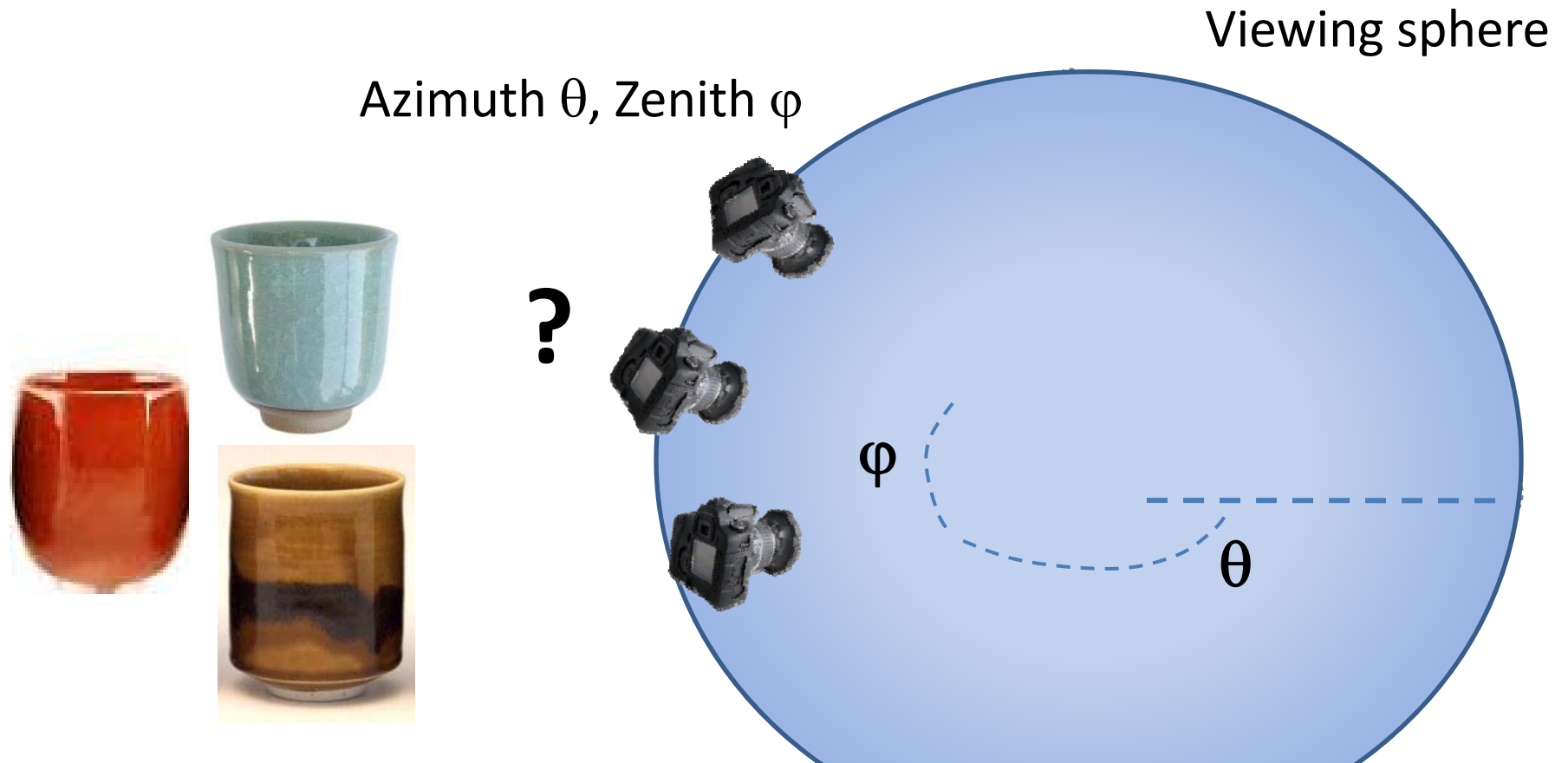
Min Sun  
University of Michigan, USA



Hao Su  
Beihang University, China  
Stanford, USA



# Our goals



- Detect objects under generic view points
- Estimate object pose
- Predict object appearance from novel views

# Our goals



- Detect objects under generic view points
- Estimate object pose
- Predict object appearance from novel views
- Generic and work for any category

# Current paradigm

- Leung et al '99
- Weber et al. '00
- Schneiderman et al. '01

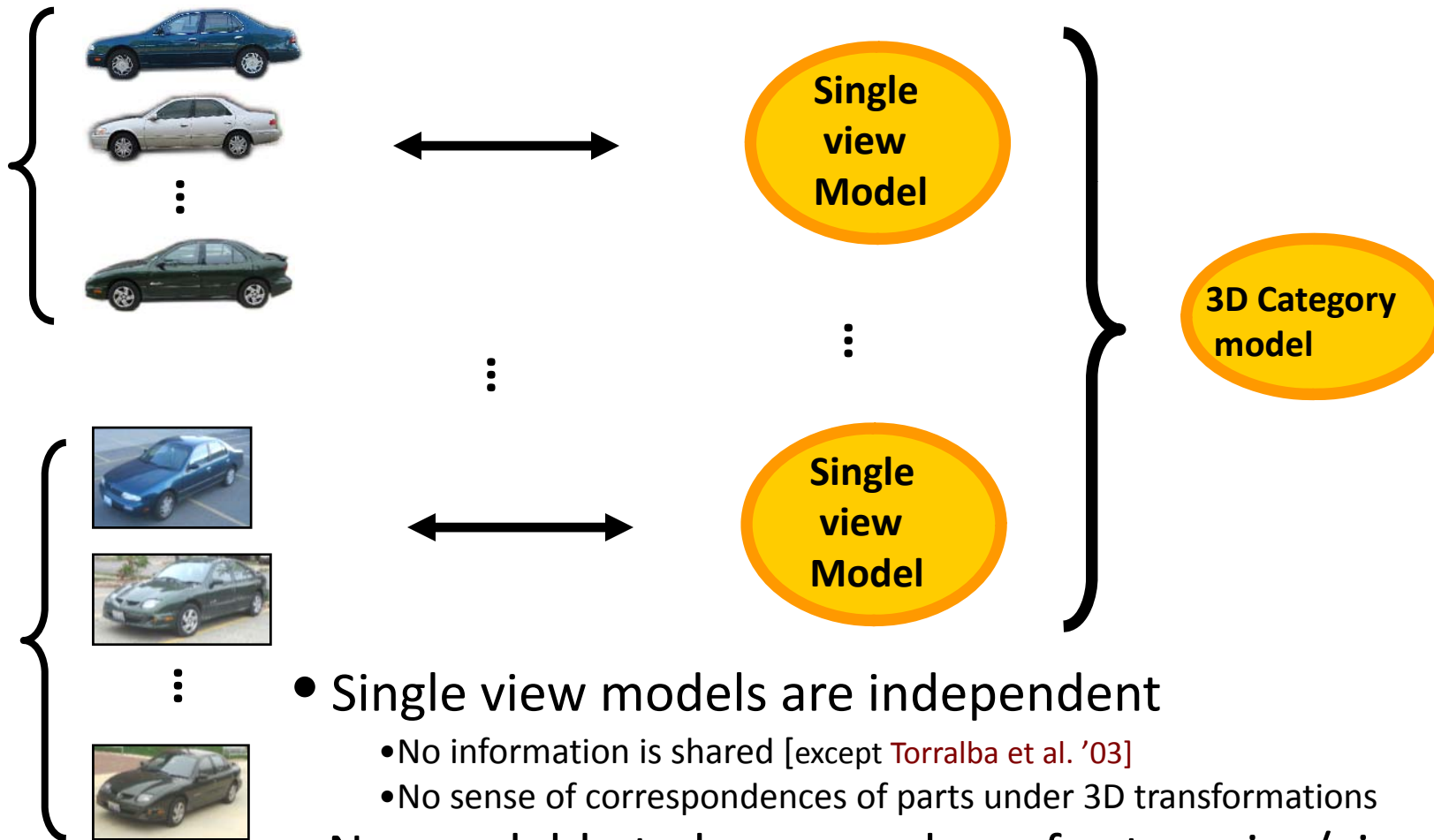
- Ullman et al. '02
- Fergus et al. '03
- Torralba et al. '03

- Felzenszwalb & Huttenlocher '03
- Fei-Fei et al. '04
- Bart et al '04
- Leibe et al. '04

- Kumar & Hebert '04
- Sivic et al. '05
- Shotton et al '05
- Grauman et al. '05

- Sudderth et al '05
- Torralba et al. '05
- Lazechnik et al. '06
- Todorovic et al. '06
- Bosh et al '07

- Vedaldi & Soatto '08
- Zhu et al 08



- Single view models are independent

- No information is shared [except [Torralba et al. '03](#)]
- No sense of correspondences of parts under 3D transformations

- Non scalable to large number of categories/view-points



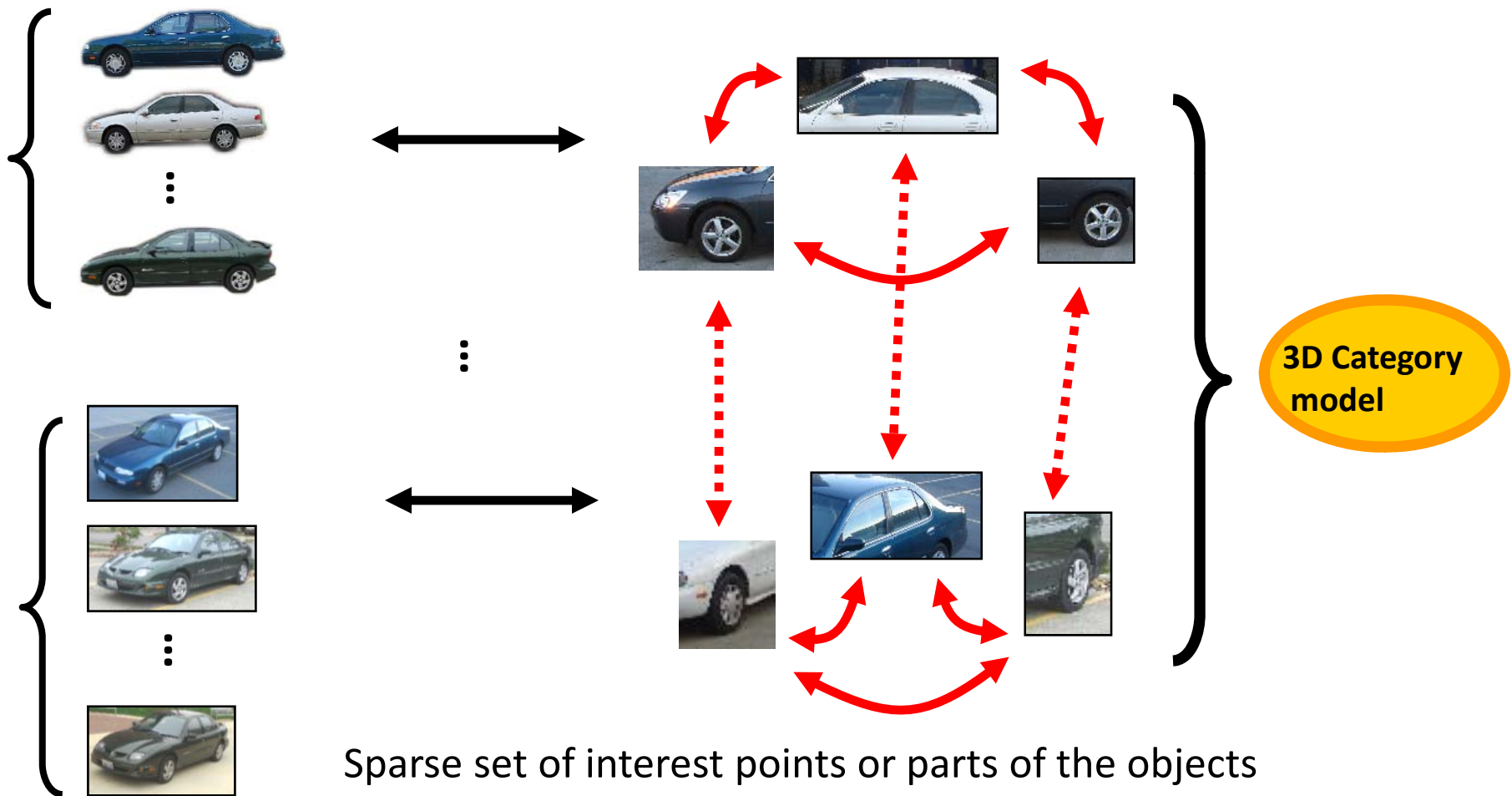
# A new recent paradigm

- Thomas et al. '06
- Kushal, et al., '07
- Savarese et al, 07, 08

- Chiu et al. '07
- Hoiem, et al., '07
- Yan, et al. '07

- Liebelt et al., '08
- Xiao et al., '08
- Liebelt et al., '08
- Xiao et al., '08

- Sun et al 09
- Farhadi let al ICCV 09
- Arie-Nachimson & Basri, 'ICCV 09



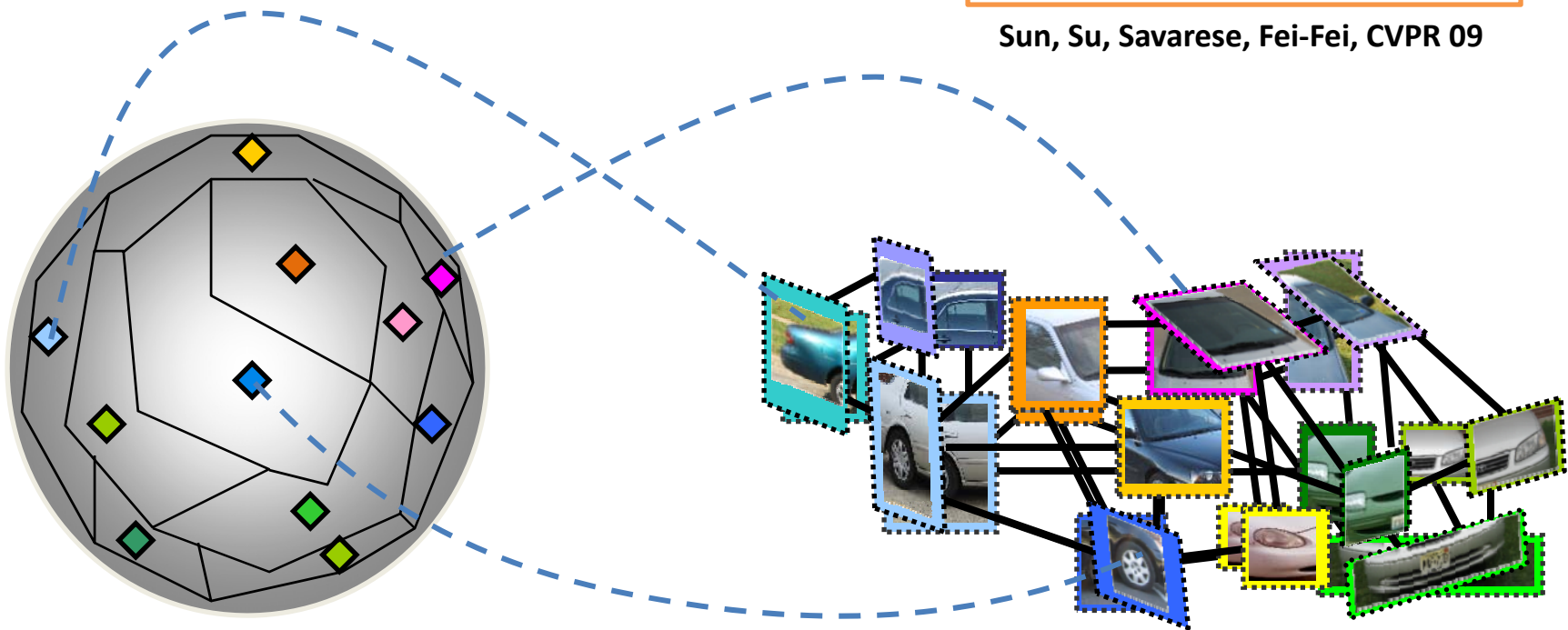
Sparse set of interest points or parts of the objects are linked across views.

# A new recent paradigm

Savarese, Fei-Fei, ICCV 07

Savarese, Fei-Fei, ECCV 08

Sun, Su, Savarese, Fei-Fei, CVPR 09



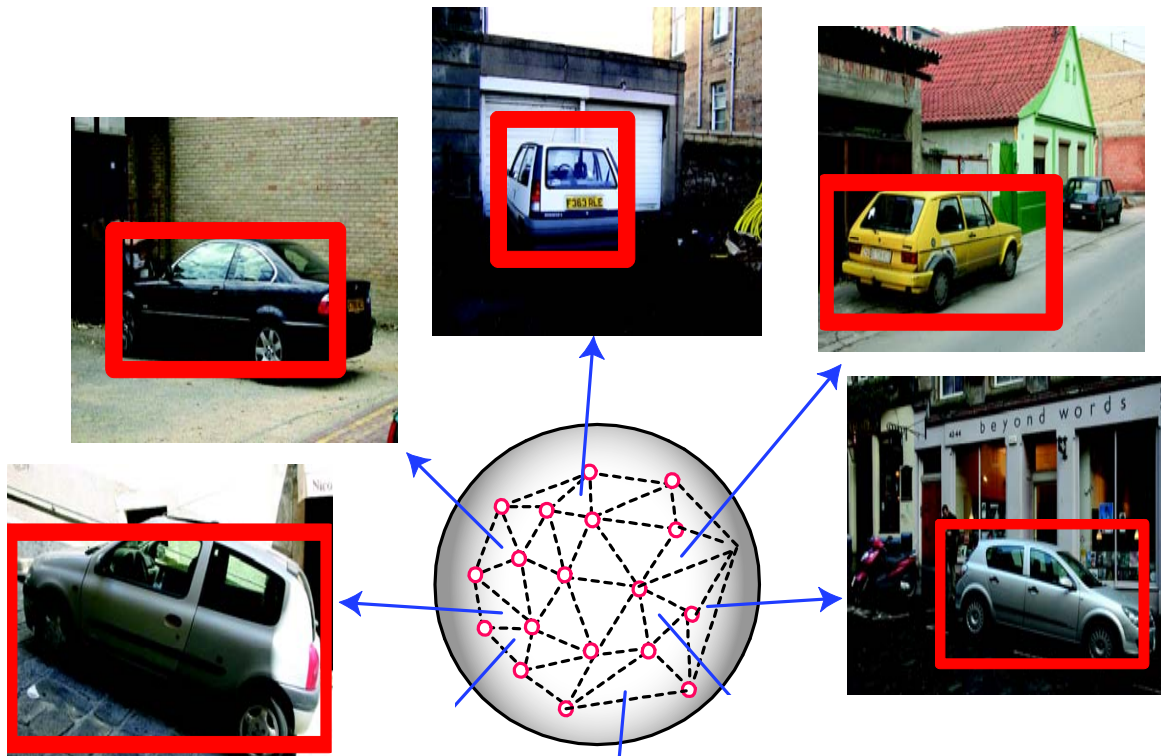
- Canonical parts captures view invariant diagnostic appearance information
- 2d  $\frac{1}{2}$  structure linking parts via weak geometry

# Drawbacks

- Supervision
  - Part labels required
  - Pose labels required
    - Except [Savarese & Fei-Fei 07, 08] , but...  
[Arie-Nachimson & Basri ICCV 09]
- No pose estimation
  - Except [Savarese & Fei-Fei 07, 08] [Sun et al 09] [Liebelt 08] [Arie-Nachimson & Basri ICCV 09]  
[Farhadi ICCV 09]
  - Few poses (at most 8 azimuth, 3 zenith)
  - Still inaccurate
- No or limited ability to synthesize novel views
- Tested on few categories
  - Usually 1-2, but no more than 8 [Savarese & Fei-Fei 07, 08] [Sun et al 09]

# Propose a new multi-view model to:

- Detect objects from any viewing angles
- Accurately estimate object pose
- Synthesize object appearance from novel views



# Key contributions

- **Representation**

- **Learning** representation on the viewing sphere:

- Model object appearance and shape from any position on the viewing sphere
- Enable view synthesis from novel view points

- **Multi-view generative part-based model** [Sun et al. CVPR 09]

- Object is represented by collections of parts
- Parts are linked across views
- Parts and relationships are probabilistic

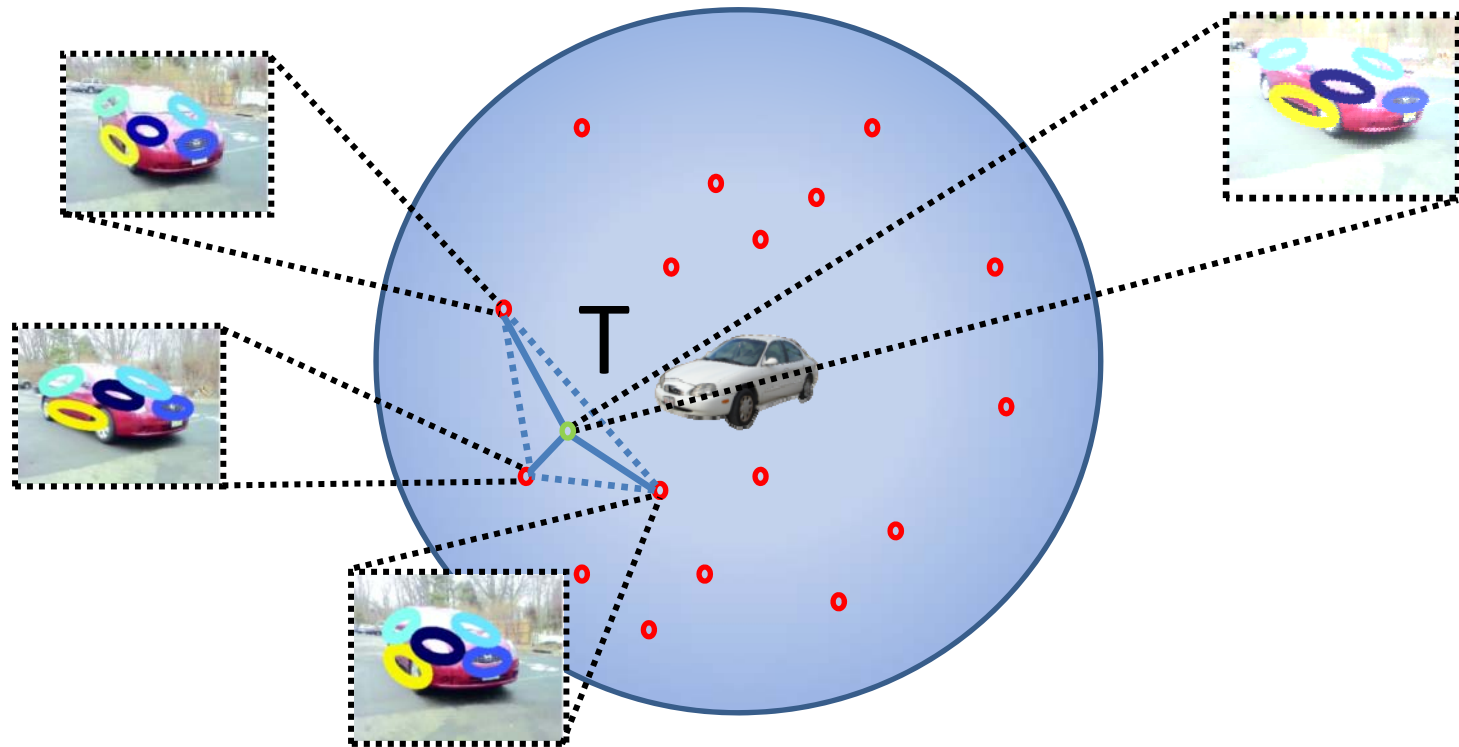
- **Semi-supervised learning**

- No part or pose labels are required

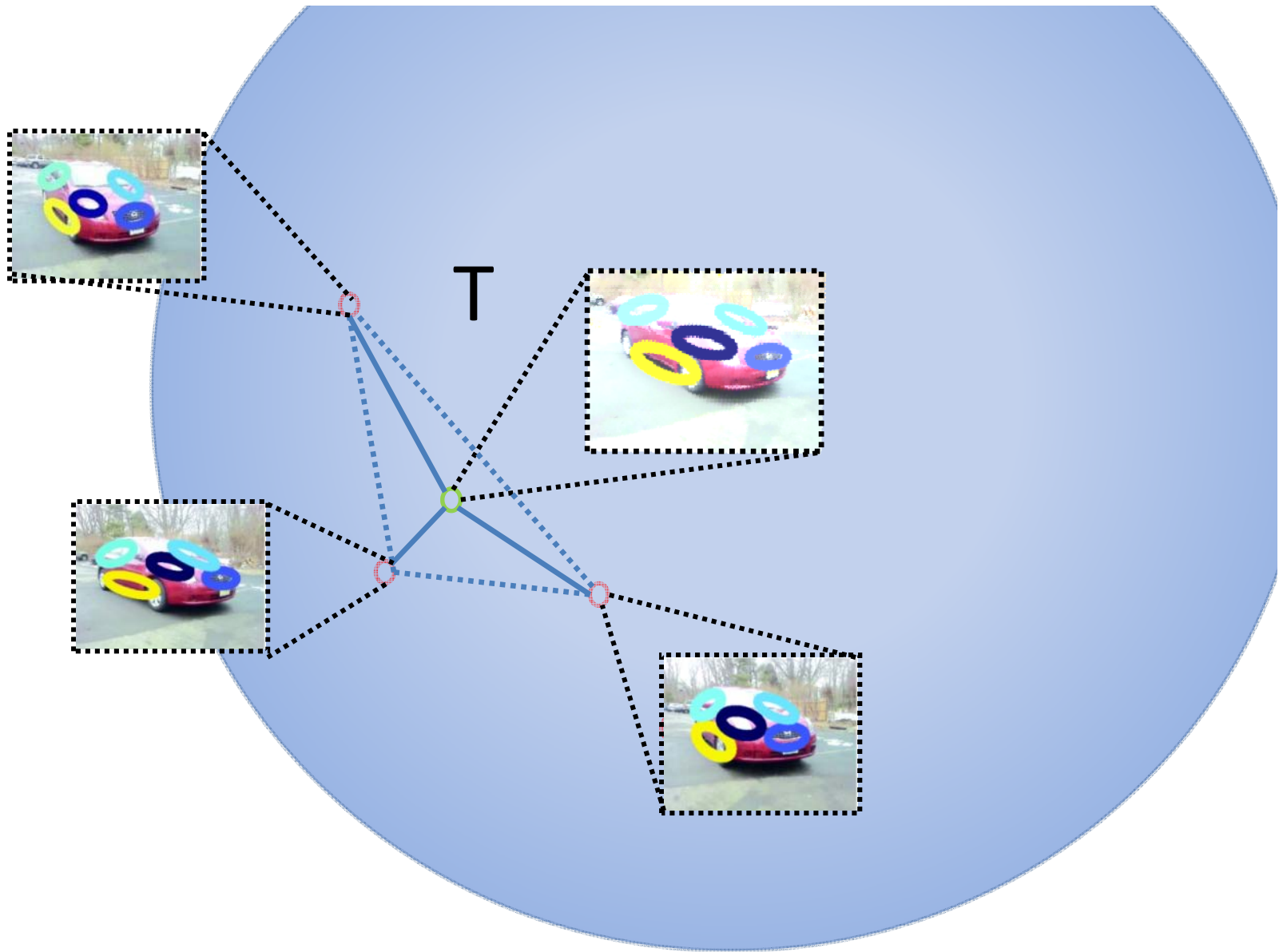
- **Incremental:**

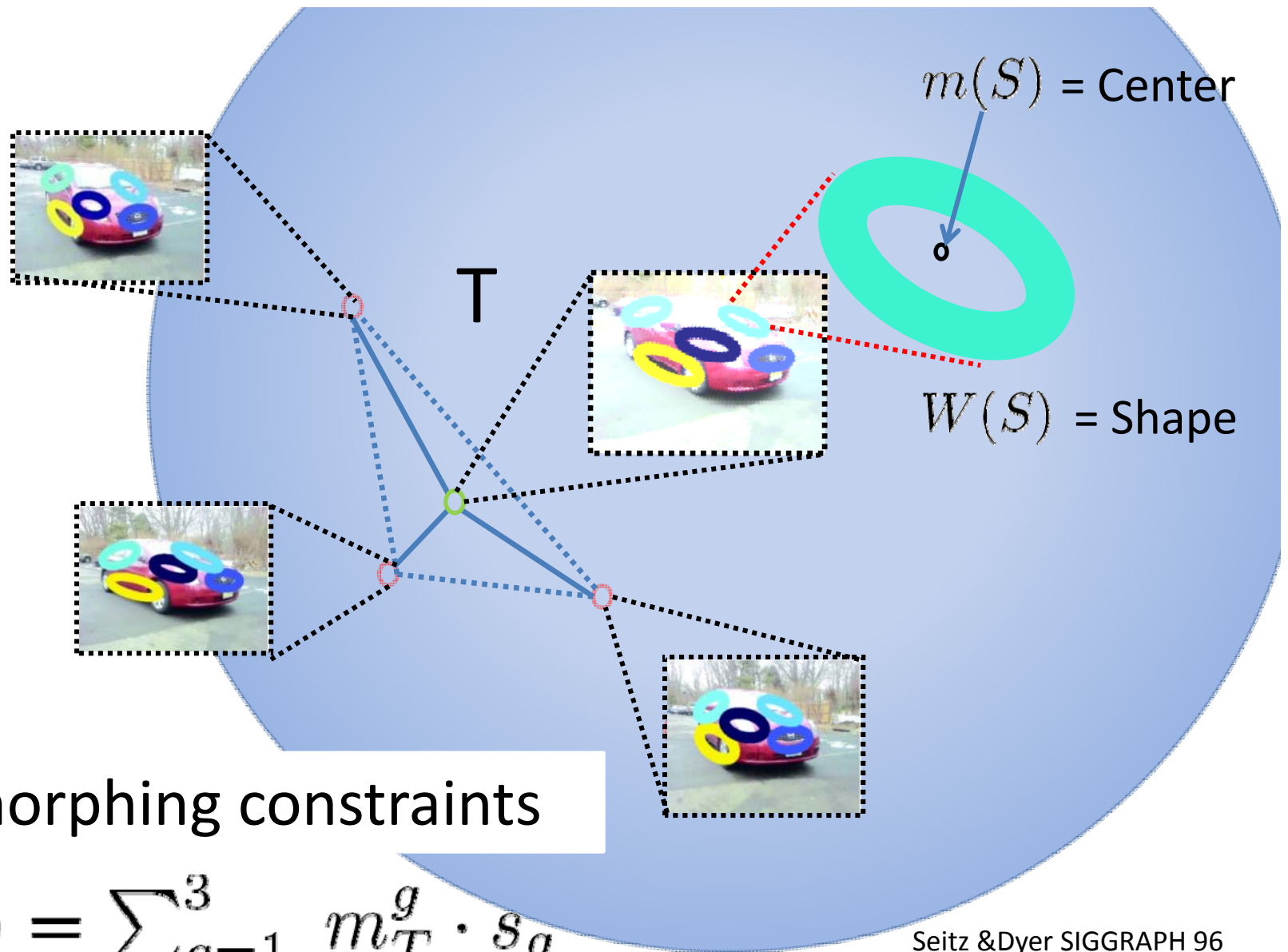
- Training images can be provided sequentially

# Dense representation on view-sphere



- Triangle T
- Morphing parameter S





## View morphing constraints

$$m(S) = \sum_{g=1}^3 m_T^g \cdot s_g$$

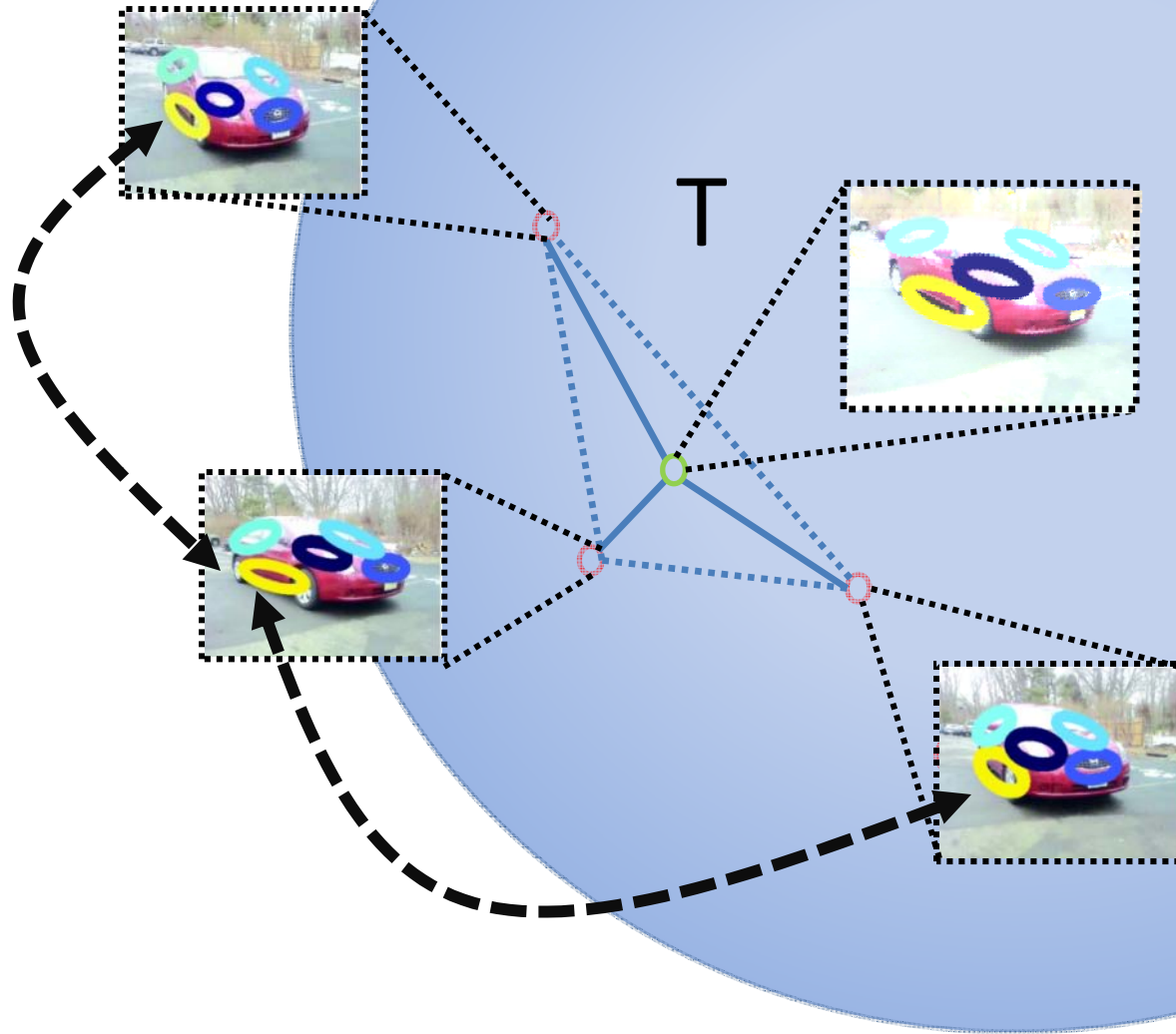
$$W(S) = \sum_{g=1}^3 W_T^g \cdot s_g$$

Seitz & Dyer SIGGRAPH 96  
Xiao & Shah CVIU '04

For first time used for  
modeling object categories!

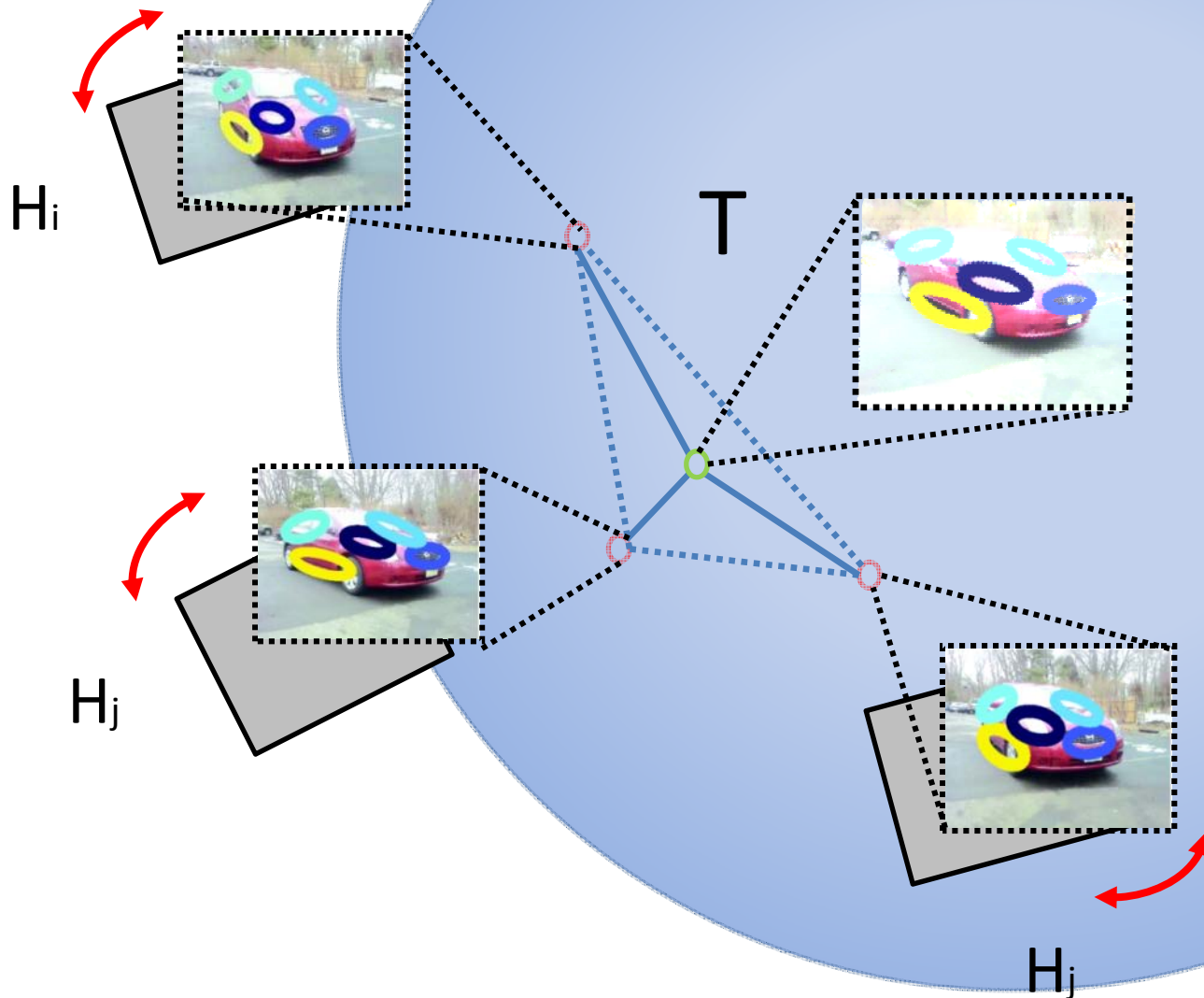


# Conditions for geometrically consistent morphing



1. Correct correspondence between parts must be established

# Conditions geometrically consistent morphing



2. Key views are rectified by a pre-warping transformations  $H$

# Key contributions

## •Representation:

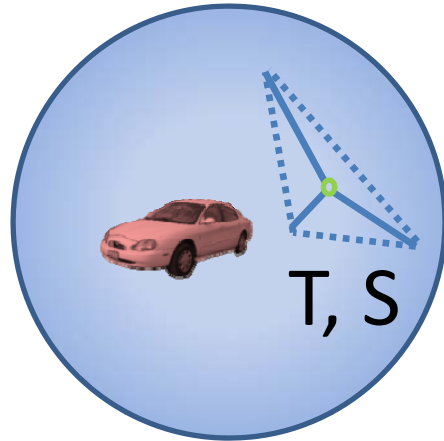
- Dense representation on the viewing sphere:
  - Model object appearance and shape from any position on the viewing sphere
  - Enable view synthesis

- **Multi-view generative part-based model** [Sun et al cvpr 09]
  - Object is represented by collections of parts
  - Parts are linked across views
  - Parts and relationships are probabilistic

## •Learning:

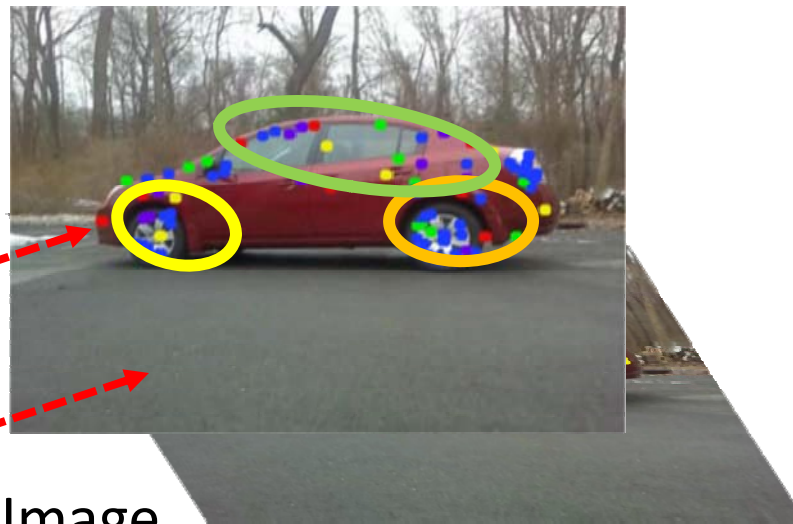
- Semi-supervised learning
  - no part or pose labels are required
- Incremental:
  - Training images can be provided sequentially

# Multi-view generative part-based model



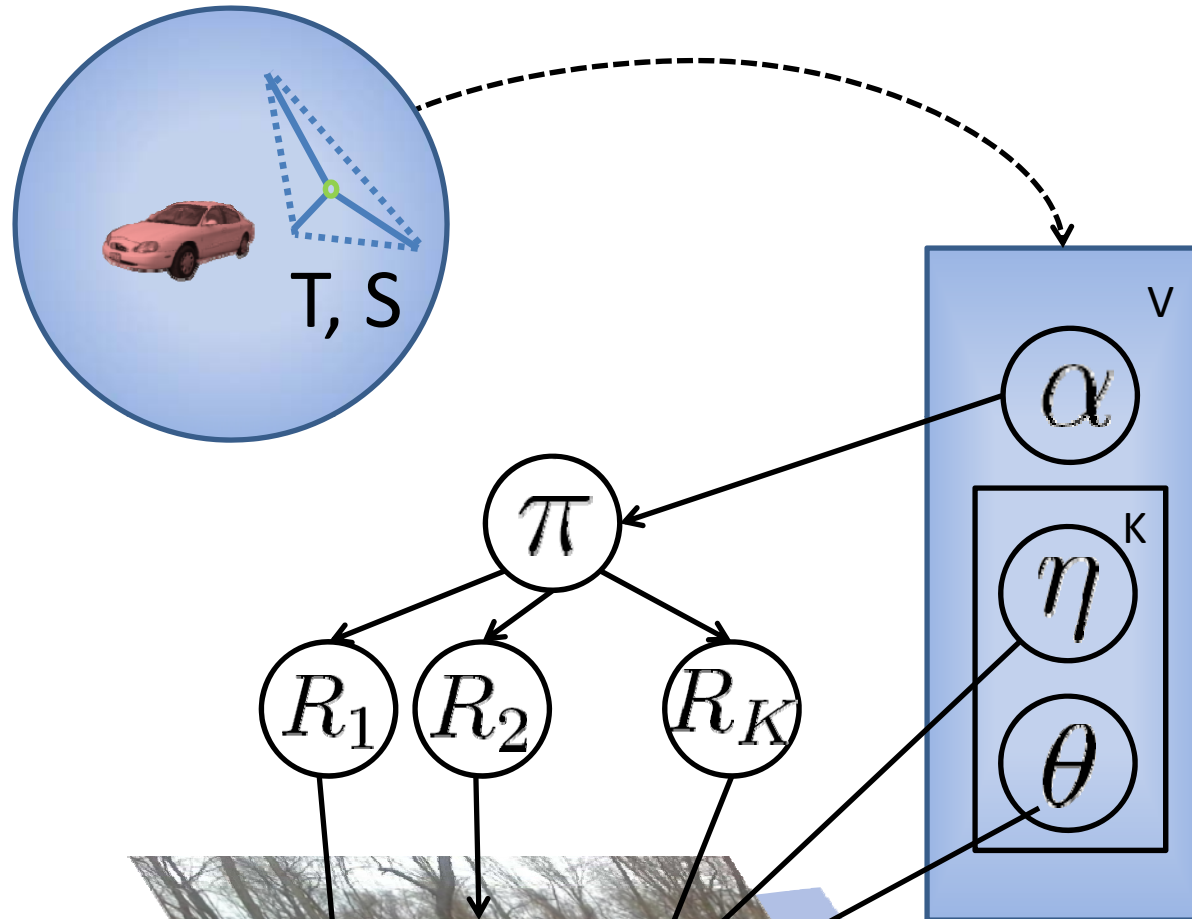
$Y_n = \text{Codeword}$   
 $X_n = \text{Location}$

$Y_n = \text{Codeword}$   
 $X_n = \text{Location}$



Image

# Multi-view generative part-based model



$\alpha$  = Part Prop. Prior

$$\pi \sim \text{Dir}(\alpha)$$

$$R \sim \text{Mult}(\pi)$$

$$Y_n \sim \text{Mult}(\eta)$$

$$X_n \sim N(\theta)$$

$\eta$  = Part Appearance

$\theta$  = Part Location/shape

$Y_n$ =Codeword

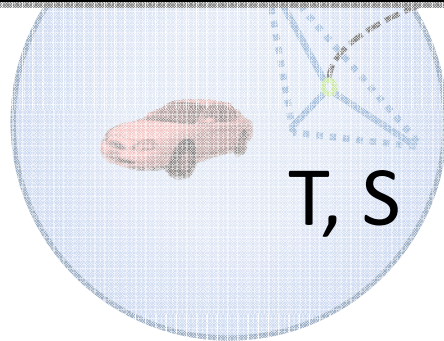
$X_n$ =Location

Image

$$X_n \leftarrow A \cdot X$$

$$P(X, Y, T, S, R, \pi) \propto P(\pi | \alpha_T)$$

$$\prod_n \{ P(X_n | \theta_{TR_n}(S), A) P(Y_n | \eta_{TR_n}(S)) P(R_n | \pi) \}$$



$\alpha$  = Part Prop. Prior

$$\pi \sim \text{Dir}(\alpha)$$

$$R \sim \text{Mult}(\pi)$$

$$Y_n \sim \text{Mult}(\eta)$$

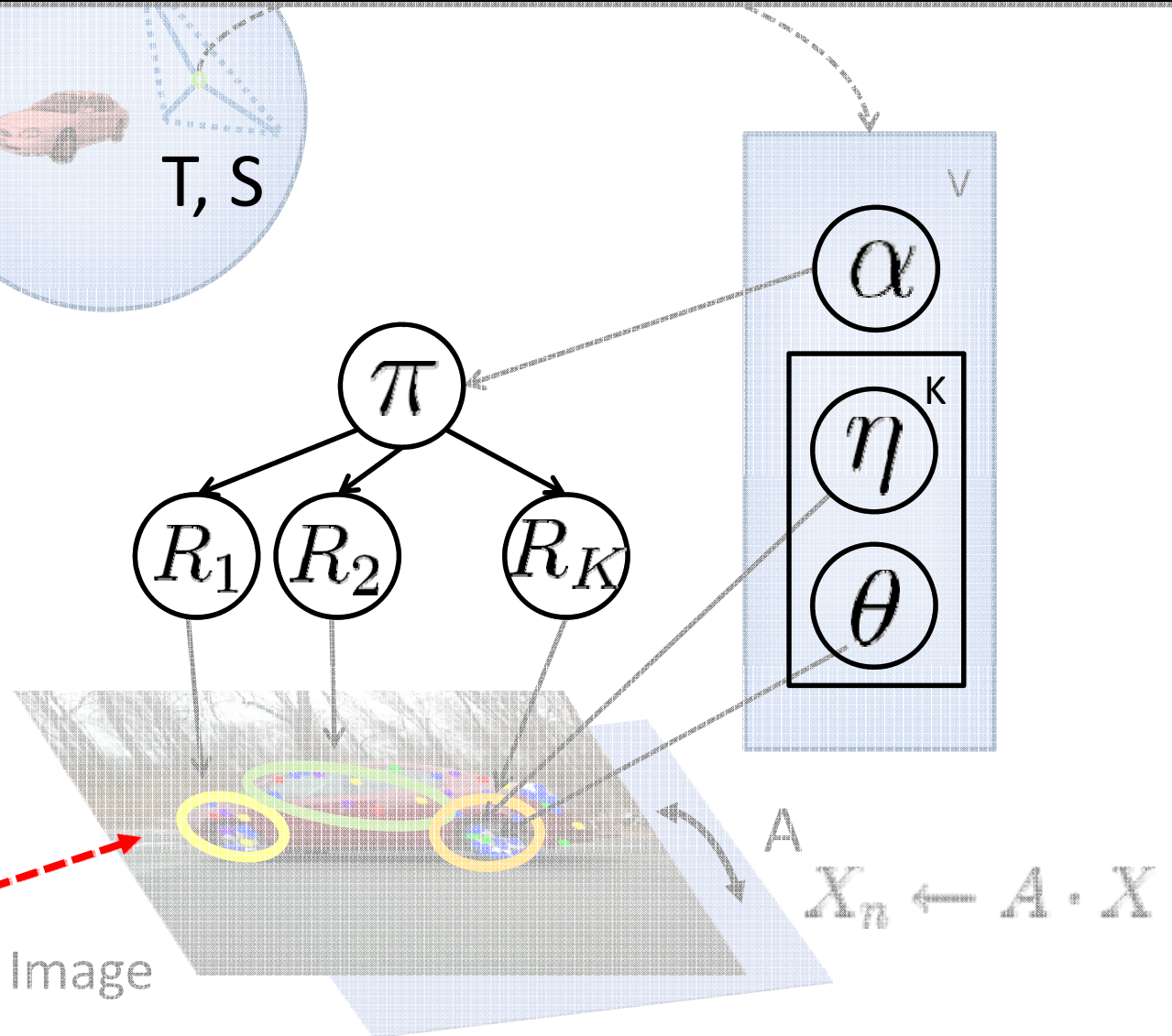
$$X_n \sim N(\theta)$$

$\eta$  = Part Appearance

$\theta$  = Part Location/shape

$Y_n$  = Codeword

$X_n$  = Location



$$P(X, Y, T, S, R, \pi) \propto P(\pi | \alpha_T)$$

$$\prod_n \{ P(X_n | \theta_{TR_n}(S), A) P(Y_n | \eta_{TR_n}(S)) P(R_n | \pi) \}$$

Exact Inference is intractable!

We use Variational EM

$\alpha$  = Part Prop. Prior

$$\pi \sim \text{Dir}(\alpha)$$

$$R \sim \text{Mult}(\pi)$$

$$Y_n \sim \text{Mult}(\eta)$$

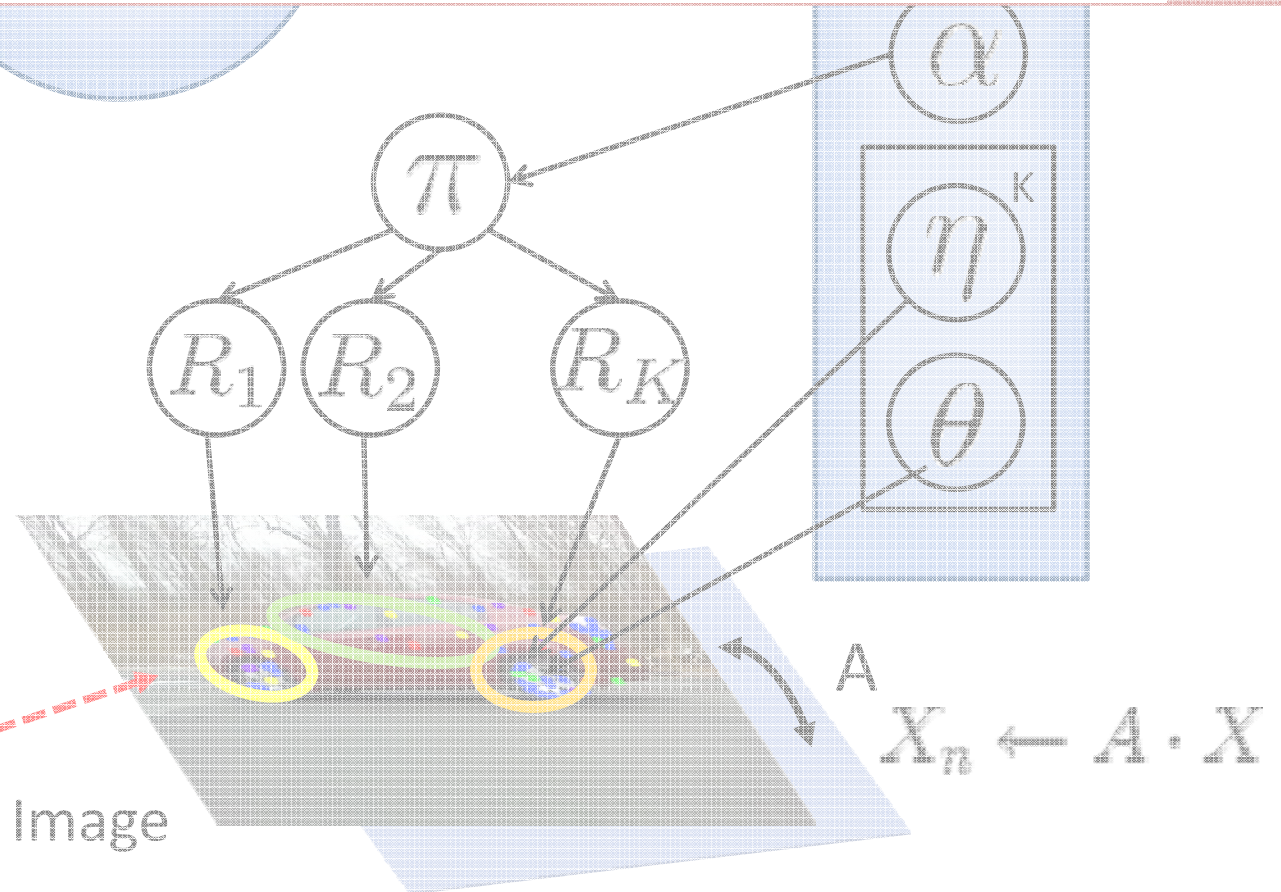
$$X_n \sim N(\theta)$$

$\eta$  = Part Appearance

$\theta$  = Part Location/shape

$Y_n$  = Codeword

$X_n$  = Location



# Key contributions

## •Representation:

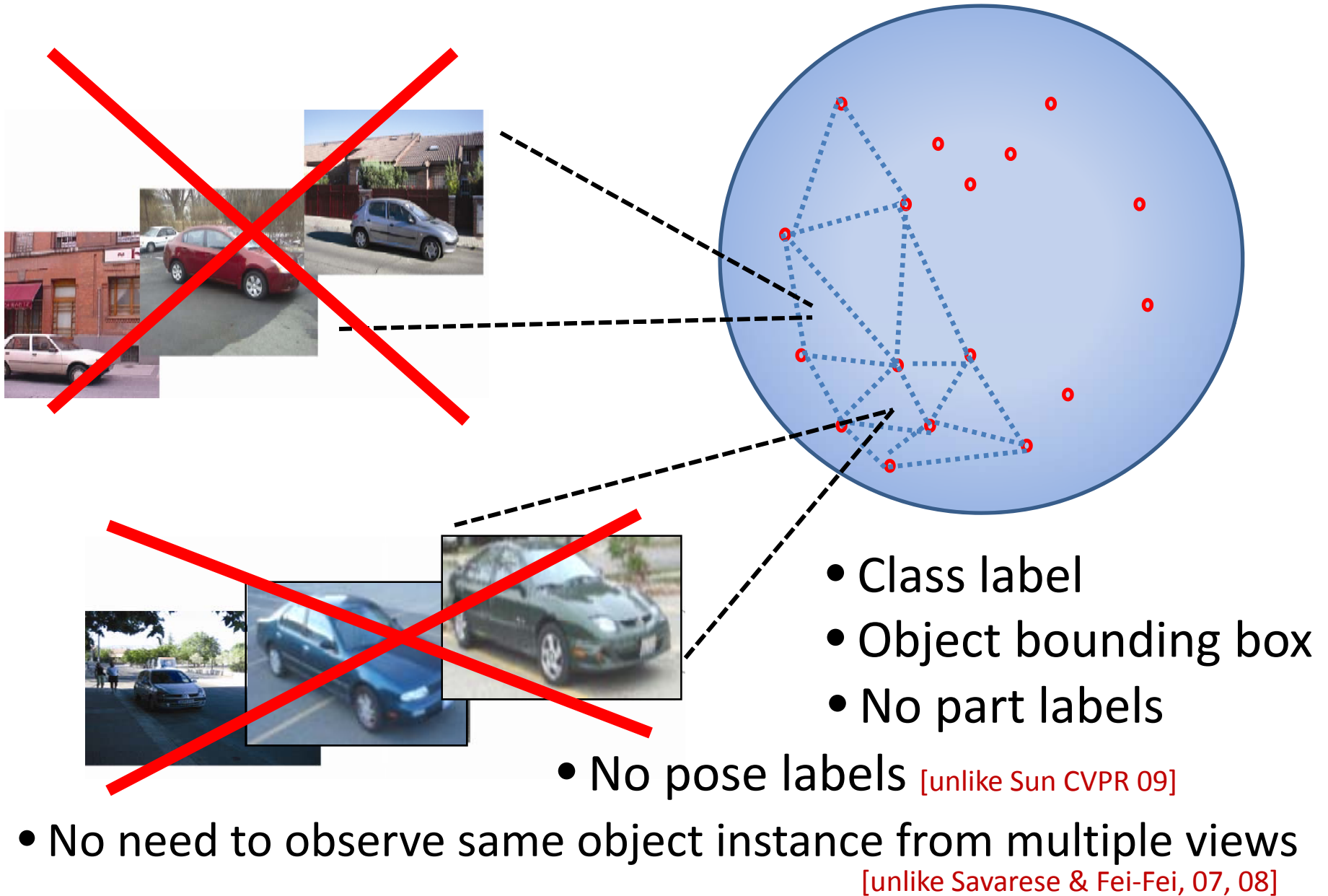
- Dense representation on the viewing sphere:
  - Model object appearance and shape from any position on the viewing sphere
  - Enable view synthesis
- Multi-view generative part-based model [Sun et al cvpr 09]
  - Object is represented by collections of parts
  - Parts are linked across views
  - Parts and relationships are probabilistic

## •Learning:

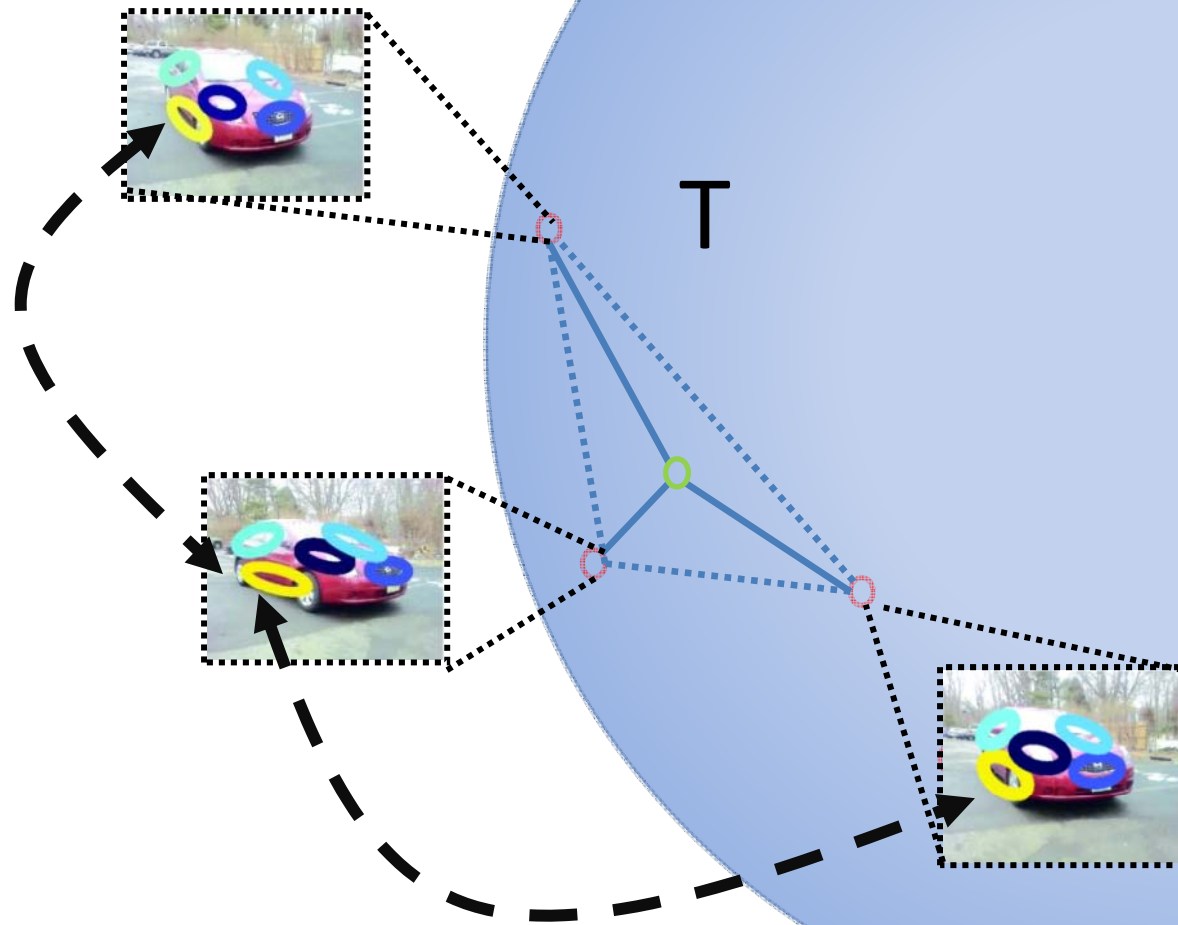
- Semi-supervised learning
  - no part or pose labels are required
- Incremental:
  - Training images can be provided sequentially



# Semi-supervised

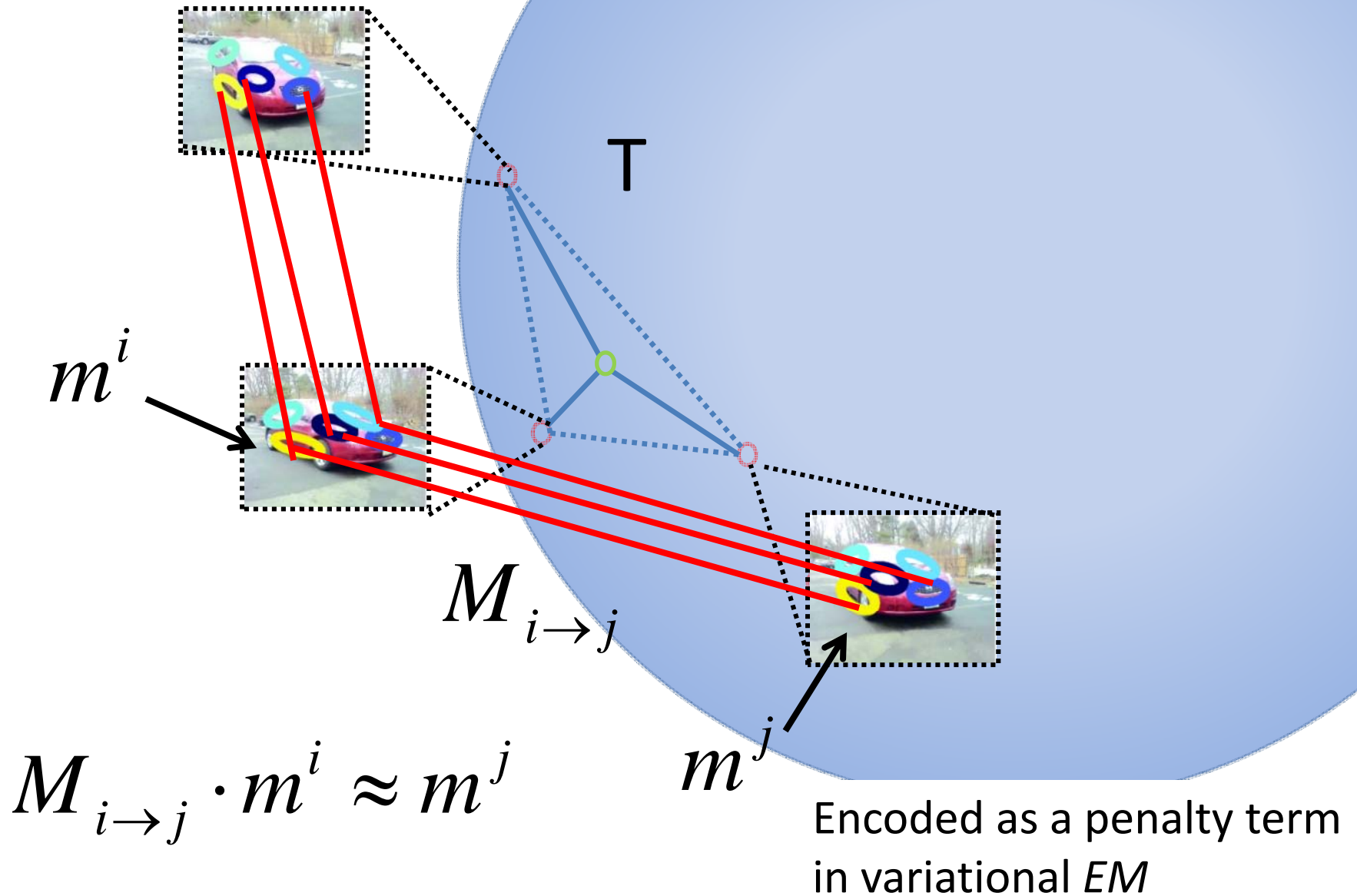


# Incorporating geometrical constraints

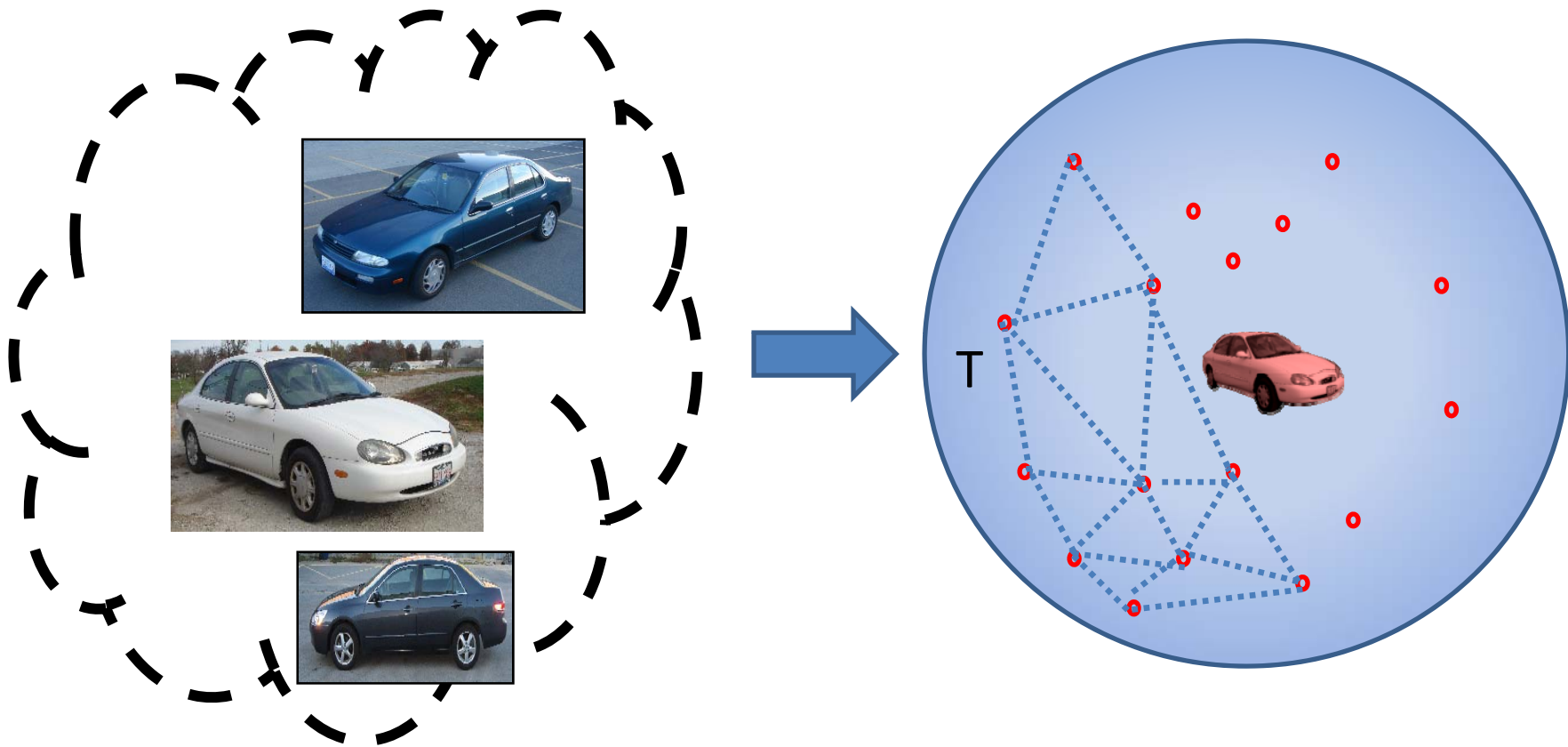


- Parts are linked across views
- Part topology is preserved under morphing transformation

# Within-triangle constraints

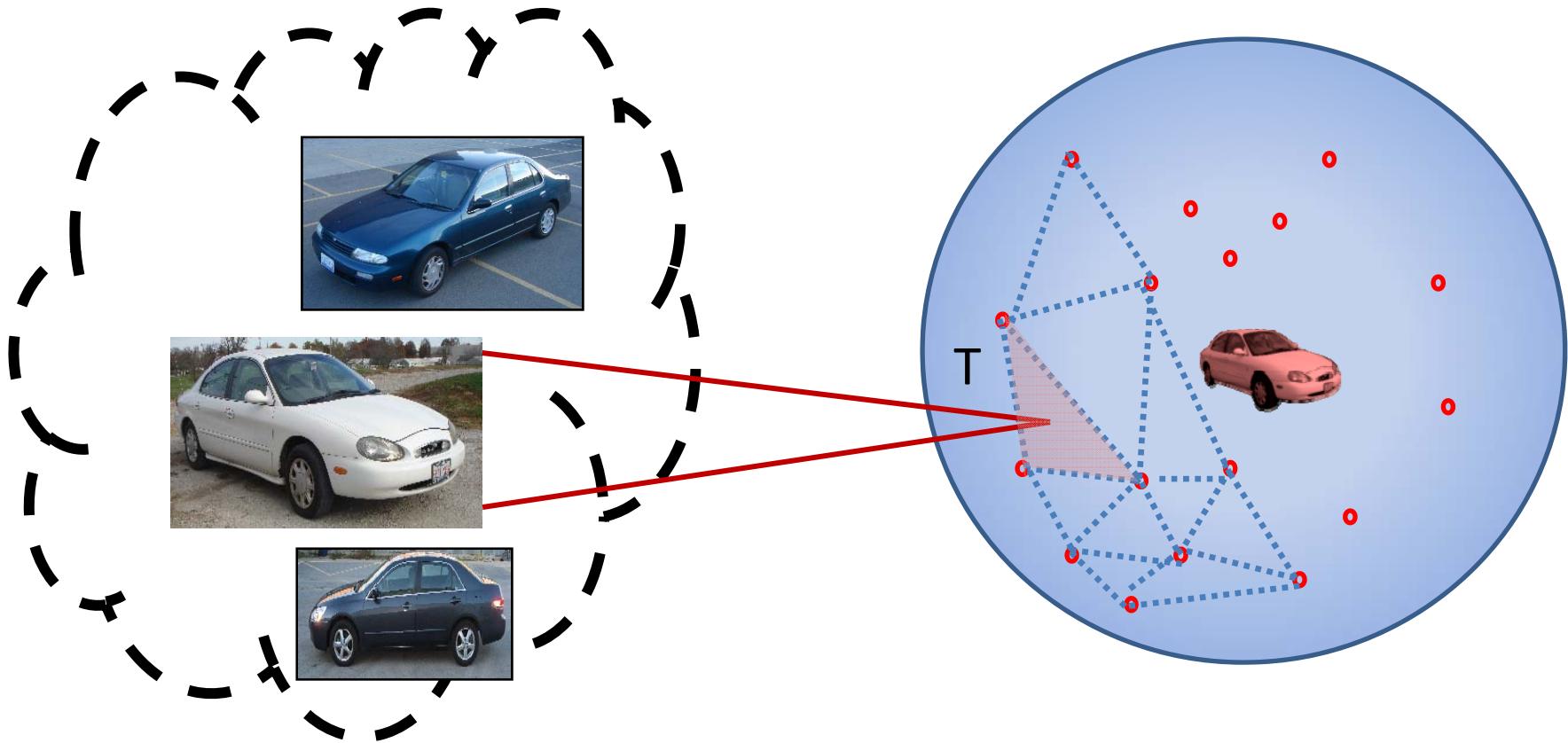


# Incremental learning



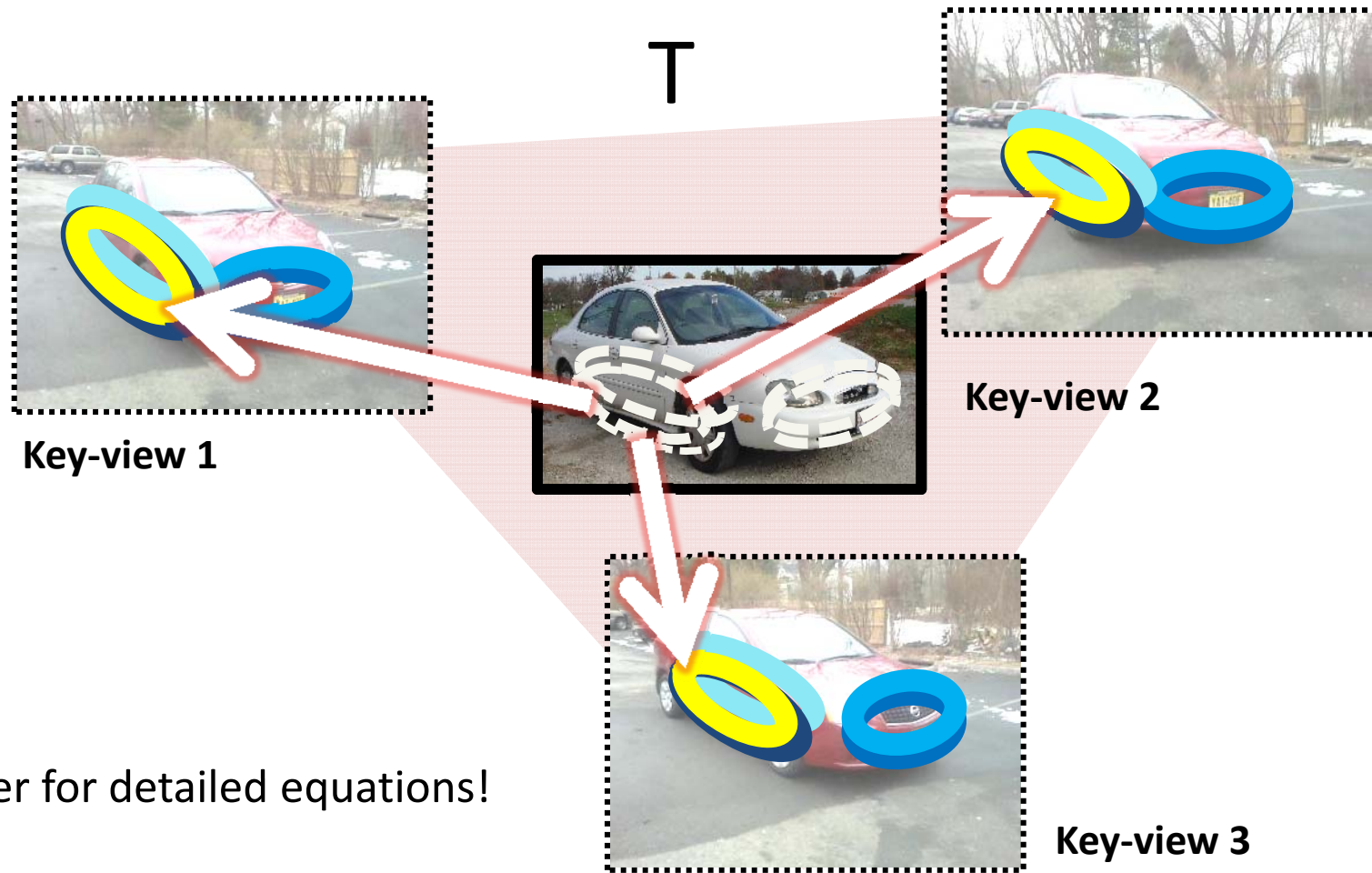
- Enable unorganized and on-line collection training images
- Increase efficiency in learning (no need large storage space)

# Incremental learning



- Sequentially assign new training images to triangles on view sphere

# Incremental learning



See paper for detailed equations!

- Sequentially assign new training images to triangles on view sphere
- Evidence of training image used to update model parameters

# Initializing the model

- Estimating key views and triangles
- Defining initial parts



$$\pi : I^h \rightarrow \{P_1^h, P_2^h, P_3^h, O^h\}$$

$$\tau : I^k \rightarrow \{P_1^k, P_2^k, P_3^k, O^k\}$$

Sequential ransac

J-linkage



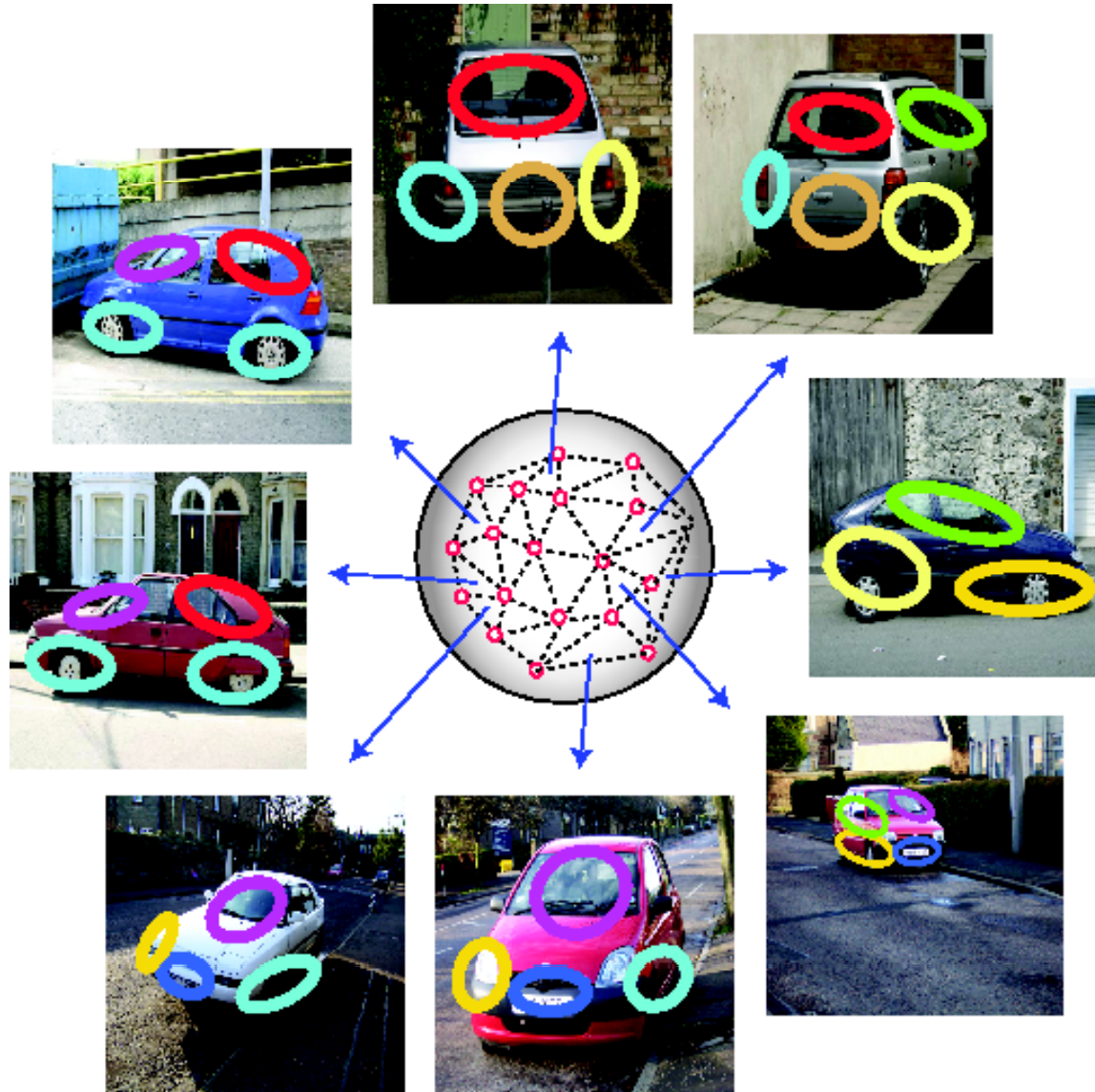
# Example of part learning





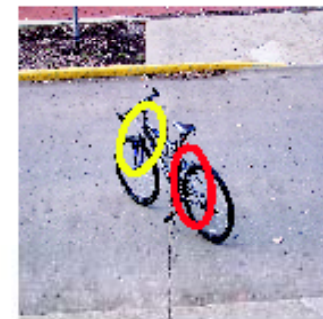
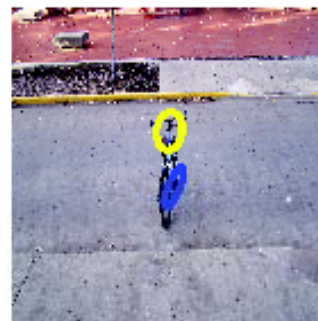
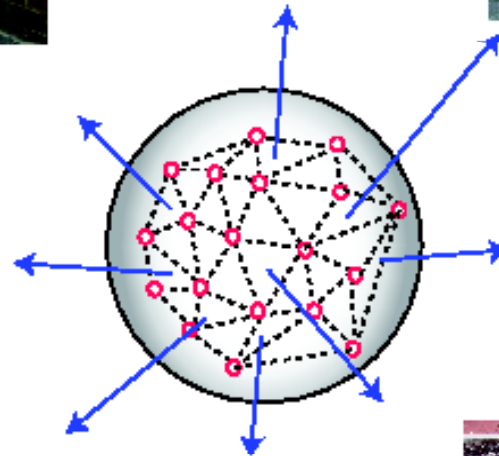
# Examples of learnt part-based models

Car



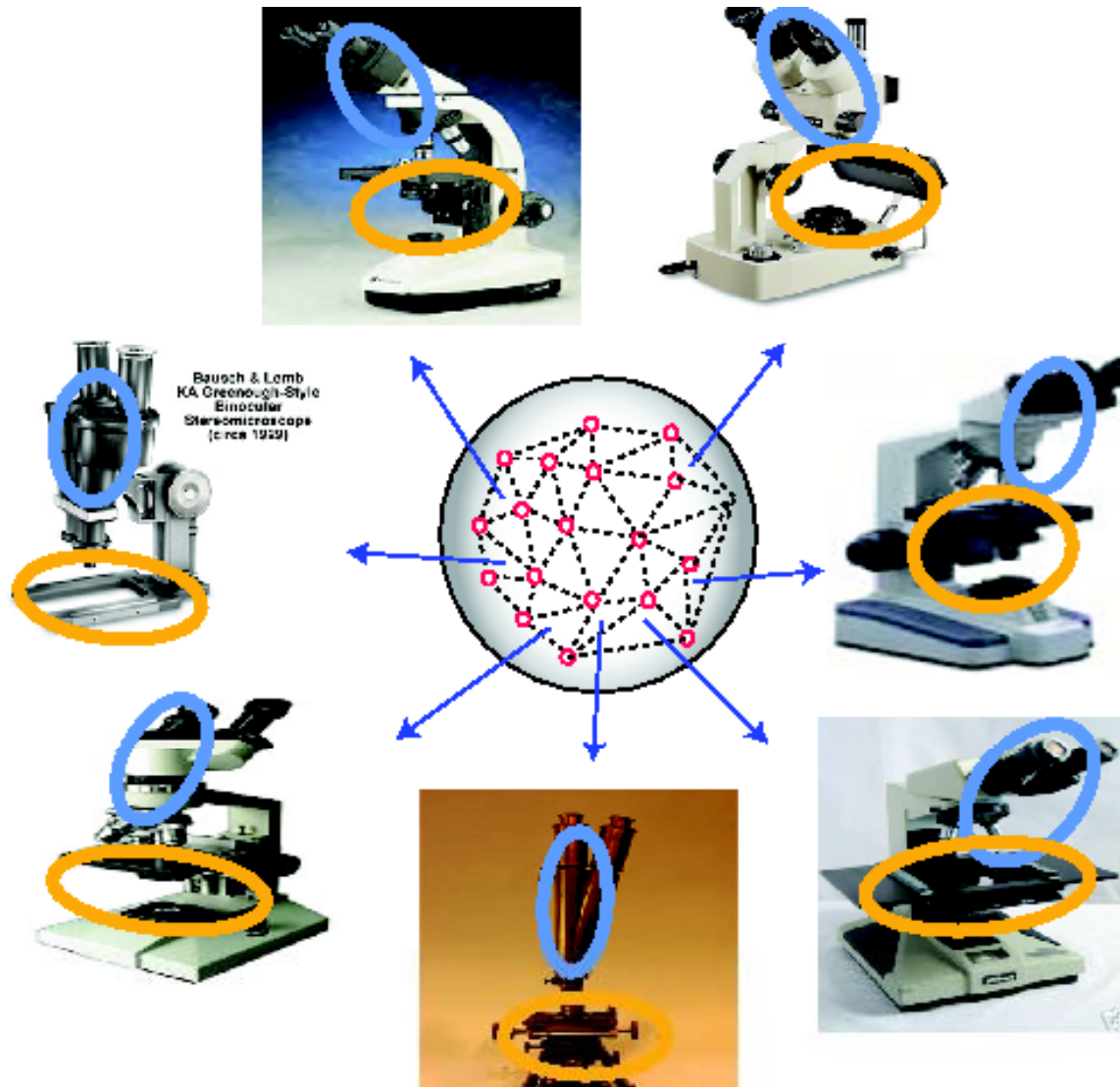
# Examples of learnt part-based models

**Bicycle**



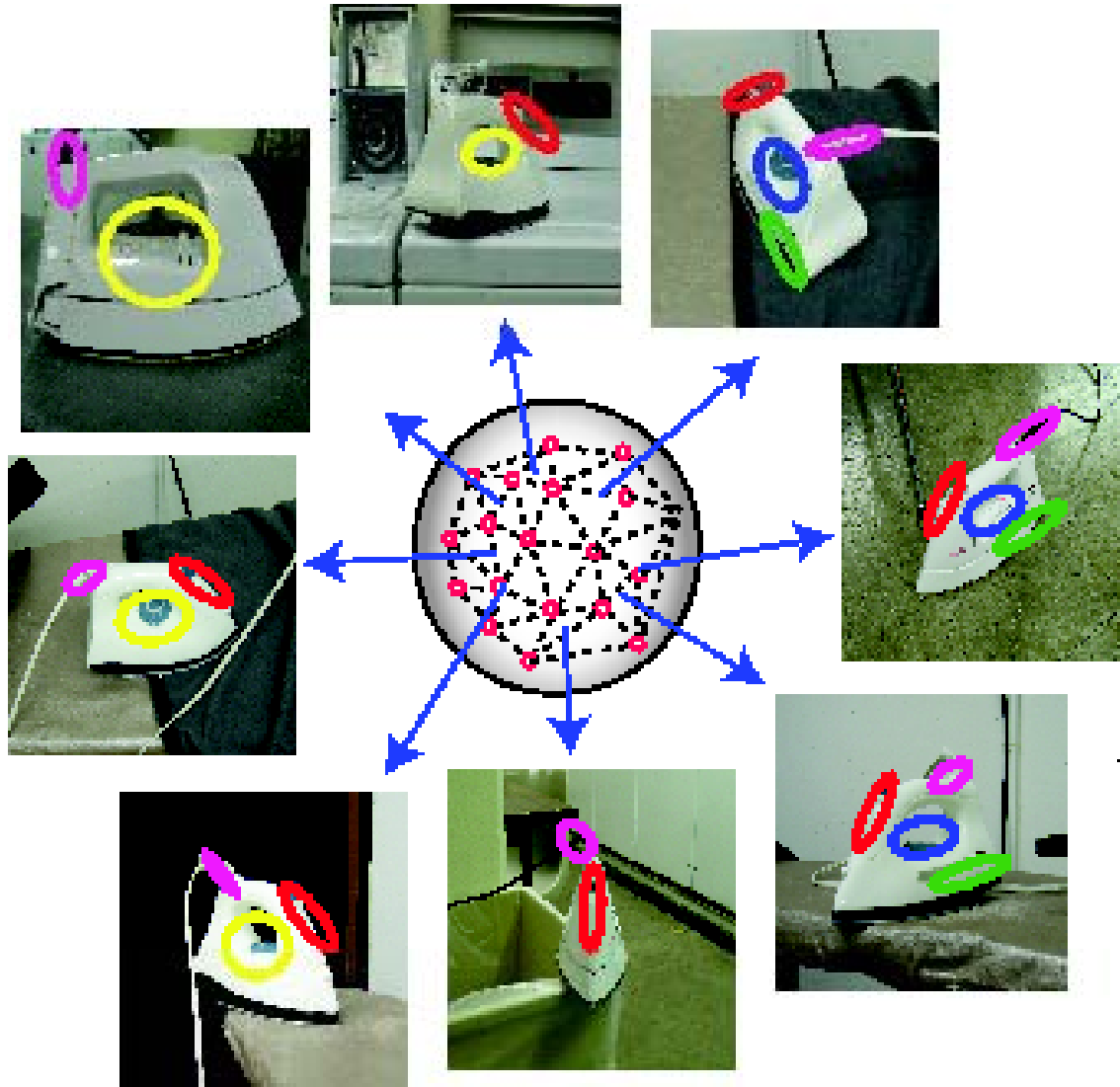
# Examples of learnt part-based models

**Binocular  
micro-  
scope**



# Examples of learnt part-based models

**Travel  
iron**



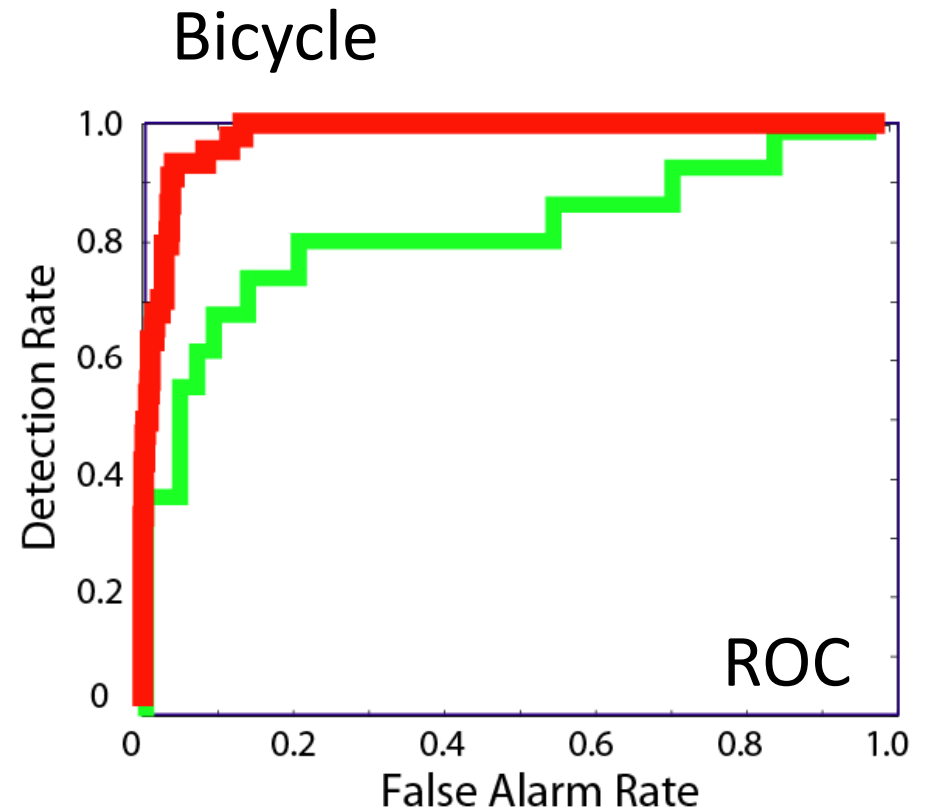
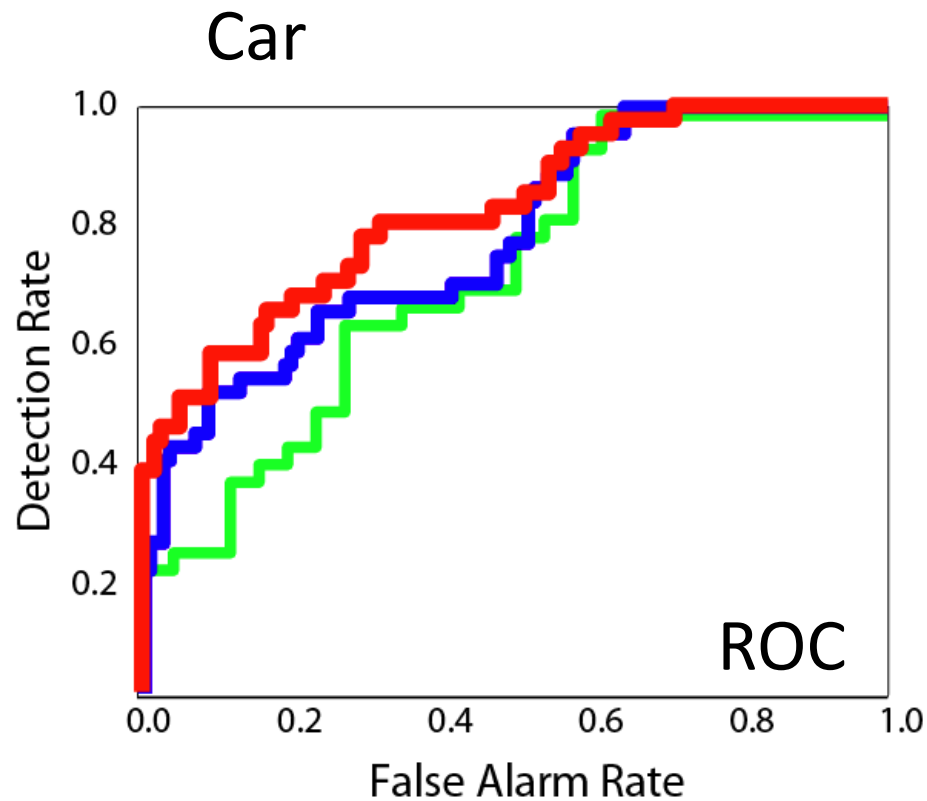
# Let's use our model!

- **Detect** objects from any viewing angles
- Accurate **pose estimation**
- **Synthesize** object shape and appearance from novel views

# Detection – UIUC 3D dataset [Savarese & Fei-Fei 07]



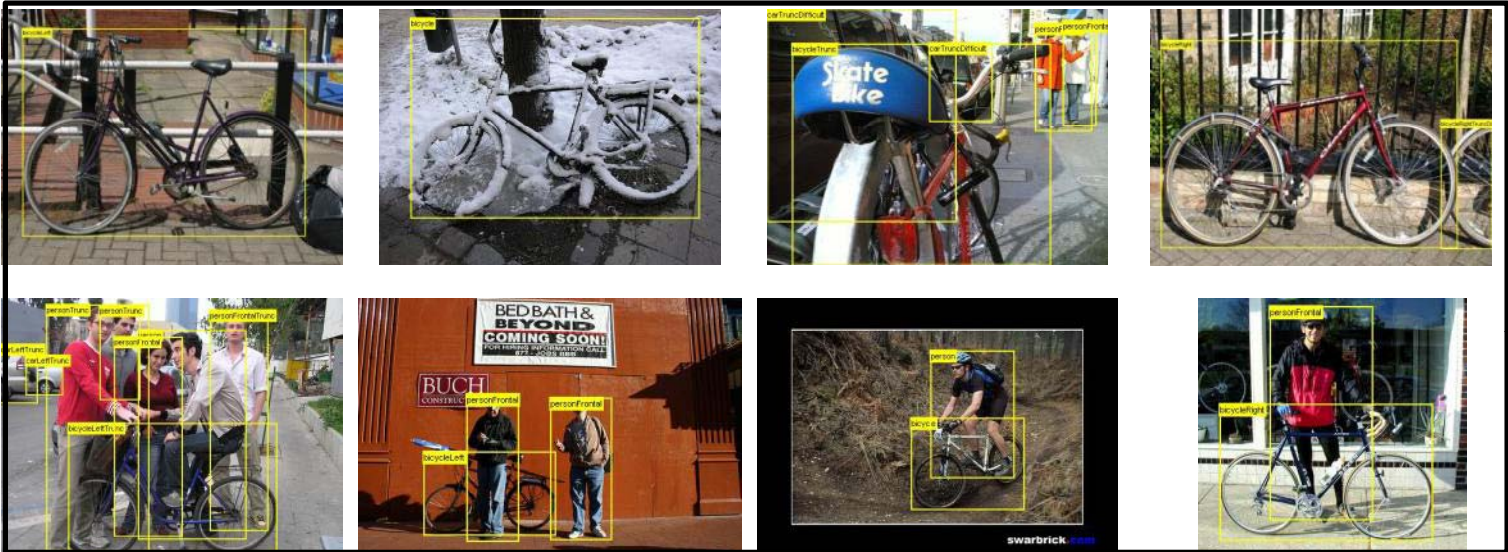
# Detection - UIUC 3D dataset



- Our model
- Min et al, CVPR 09
- Savarese & Fei-Fei ICCV '07

# Detection - Pascal 2006 dataset

Bicycle



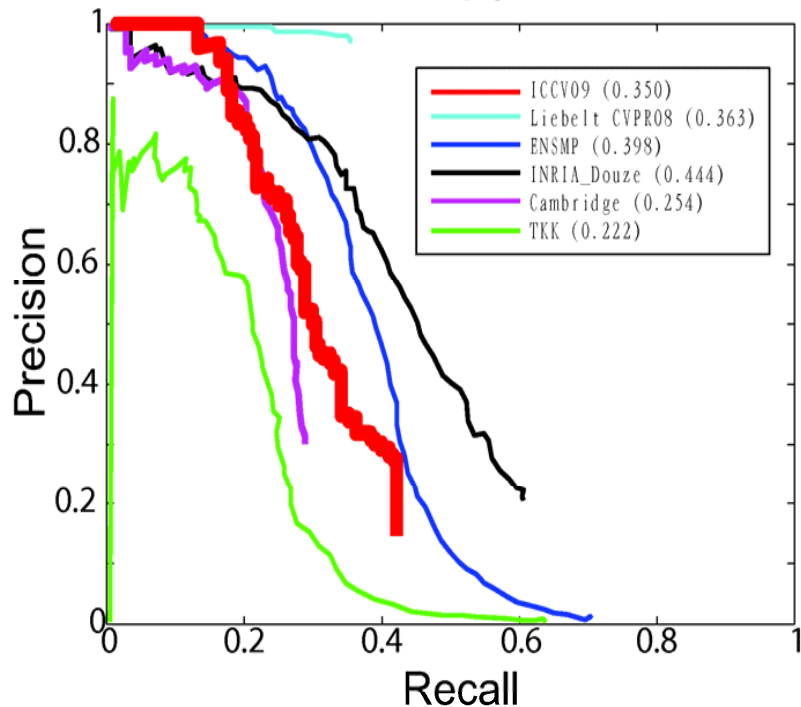
Car





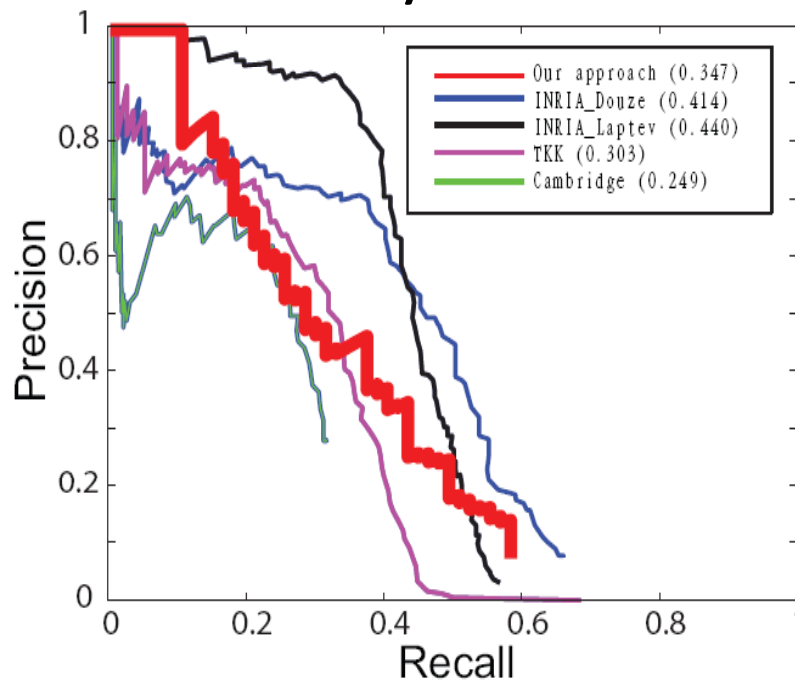
# Detection - Pascal 2006 dataset

## Car



0.35(average p)

## Bicycle



0.347(average p)

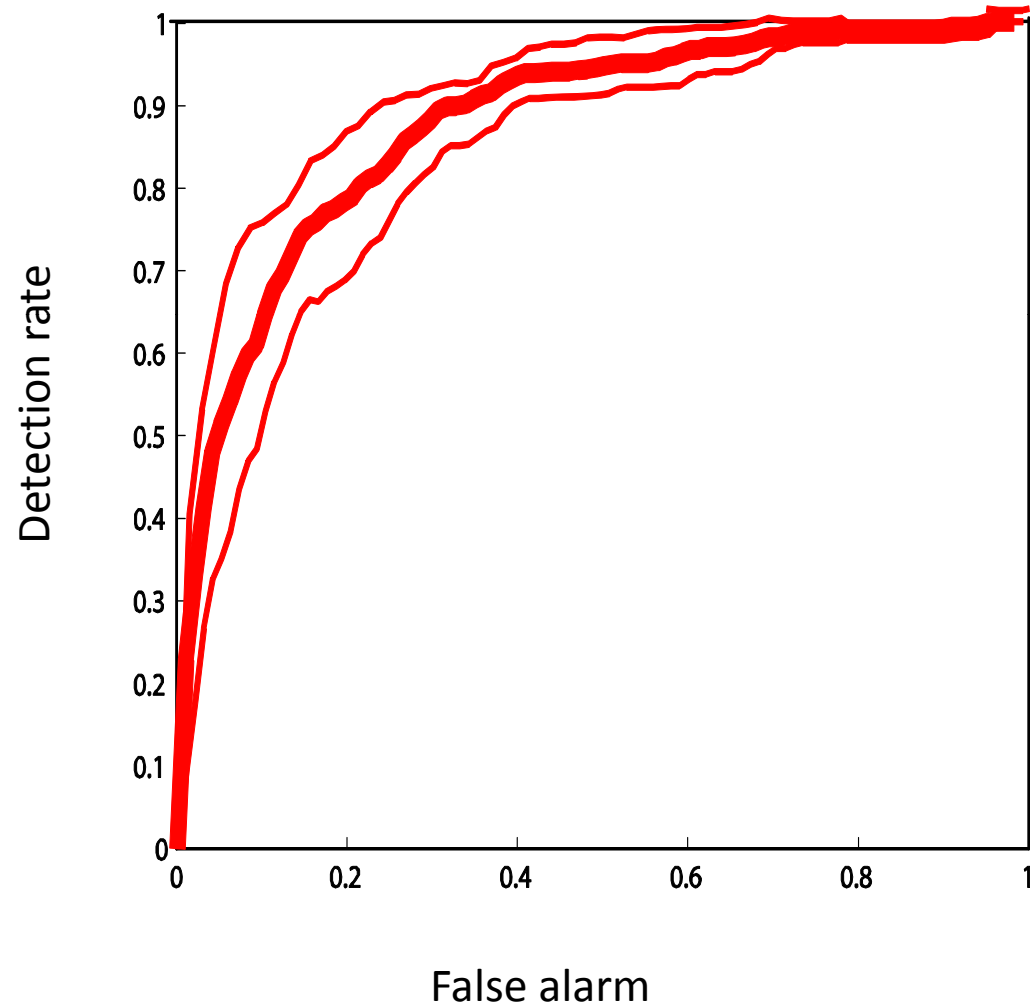
— Our model

# Detection - Household Item Dataset

Watch Light Teapot Calculat Chair Iron Microscope Sewing M

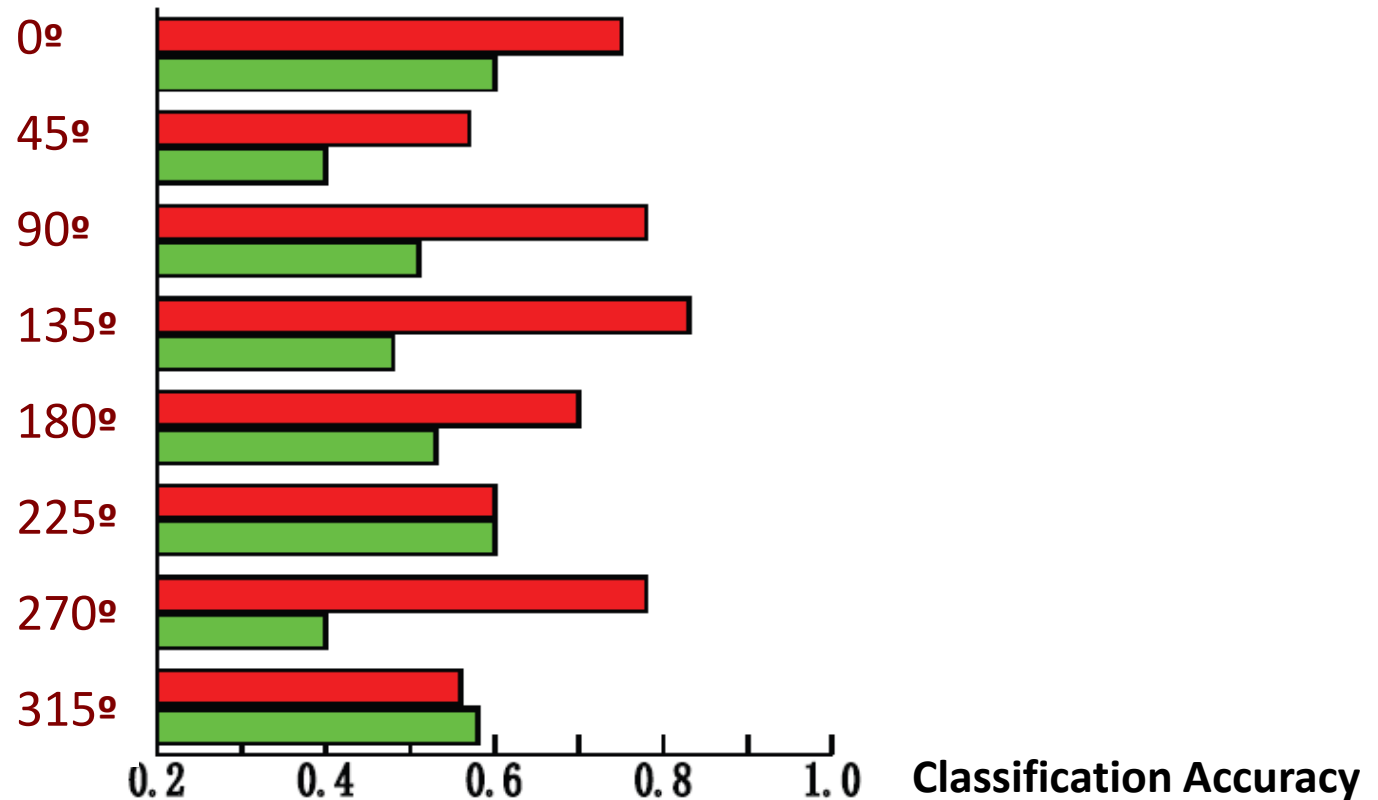


# Detection - Household Item Dataset



# Viewpoint Classification

Car from UIUC 3D Dataset



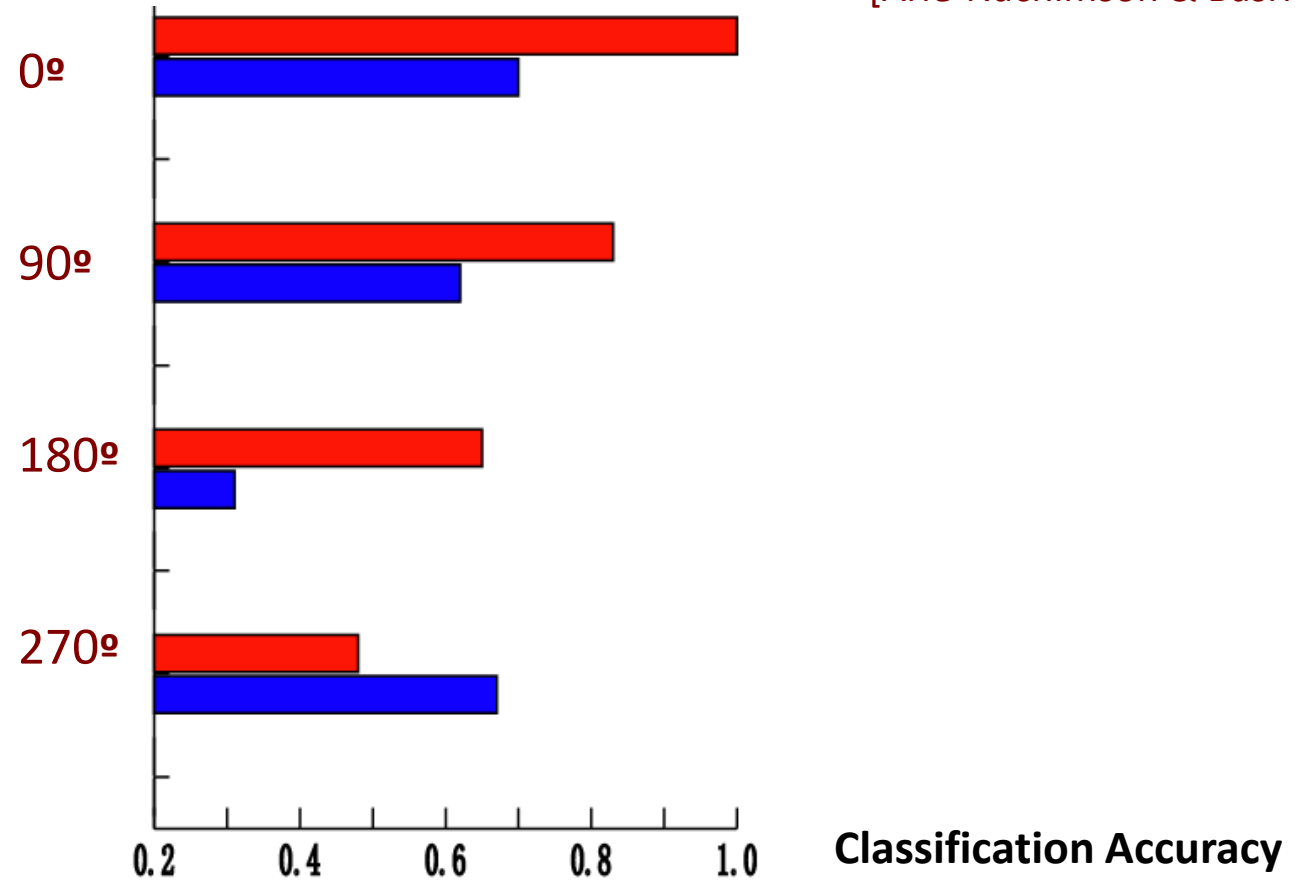
- Our model
- Savarese & Fei-Fei ICCV '07

# Viewpoint Classification

Car- Pascal 2006 dataset

First the time!

[Arie-Nachimson & Basri '09]

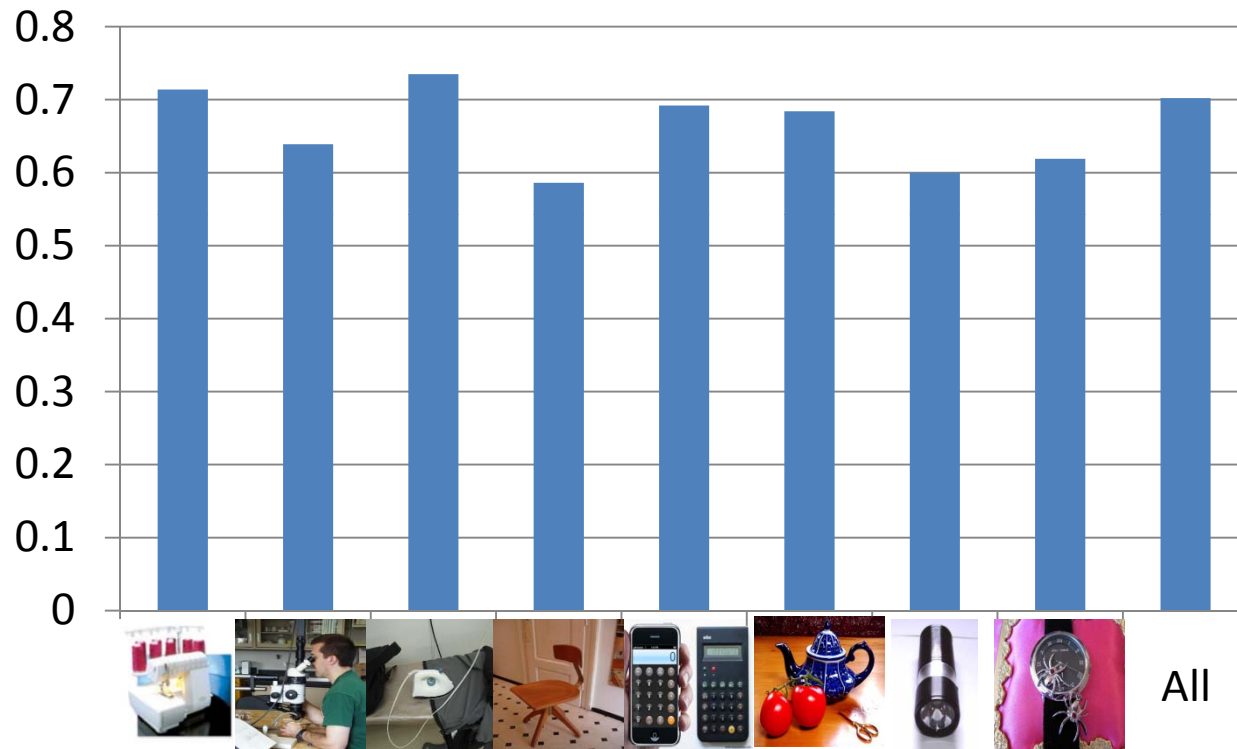


- Our model
- Min et al, CVPR 09

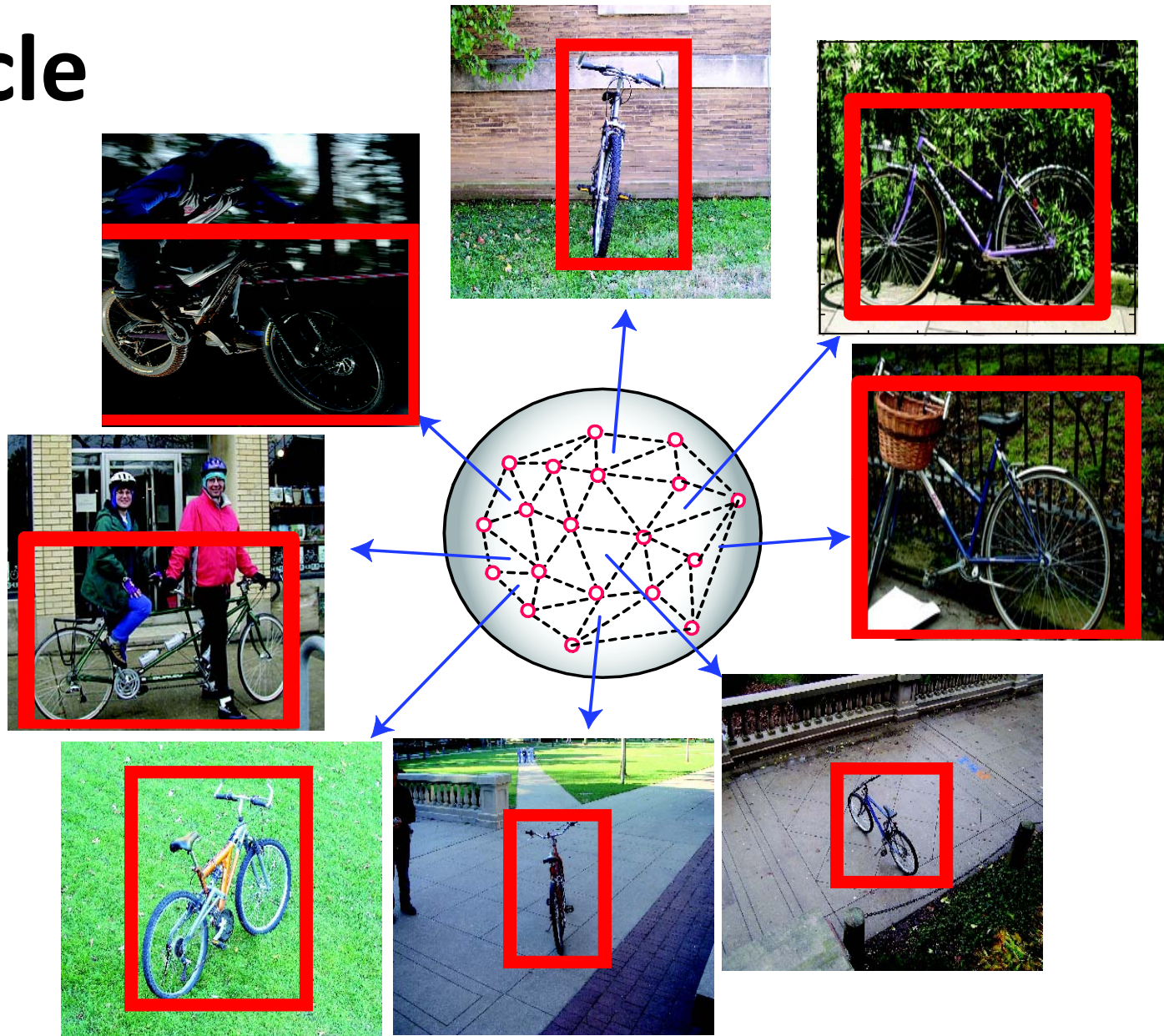
# Viewpoint Classification

## Household Item Dataset

Avg. Accuracy

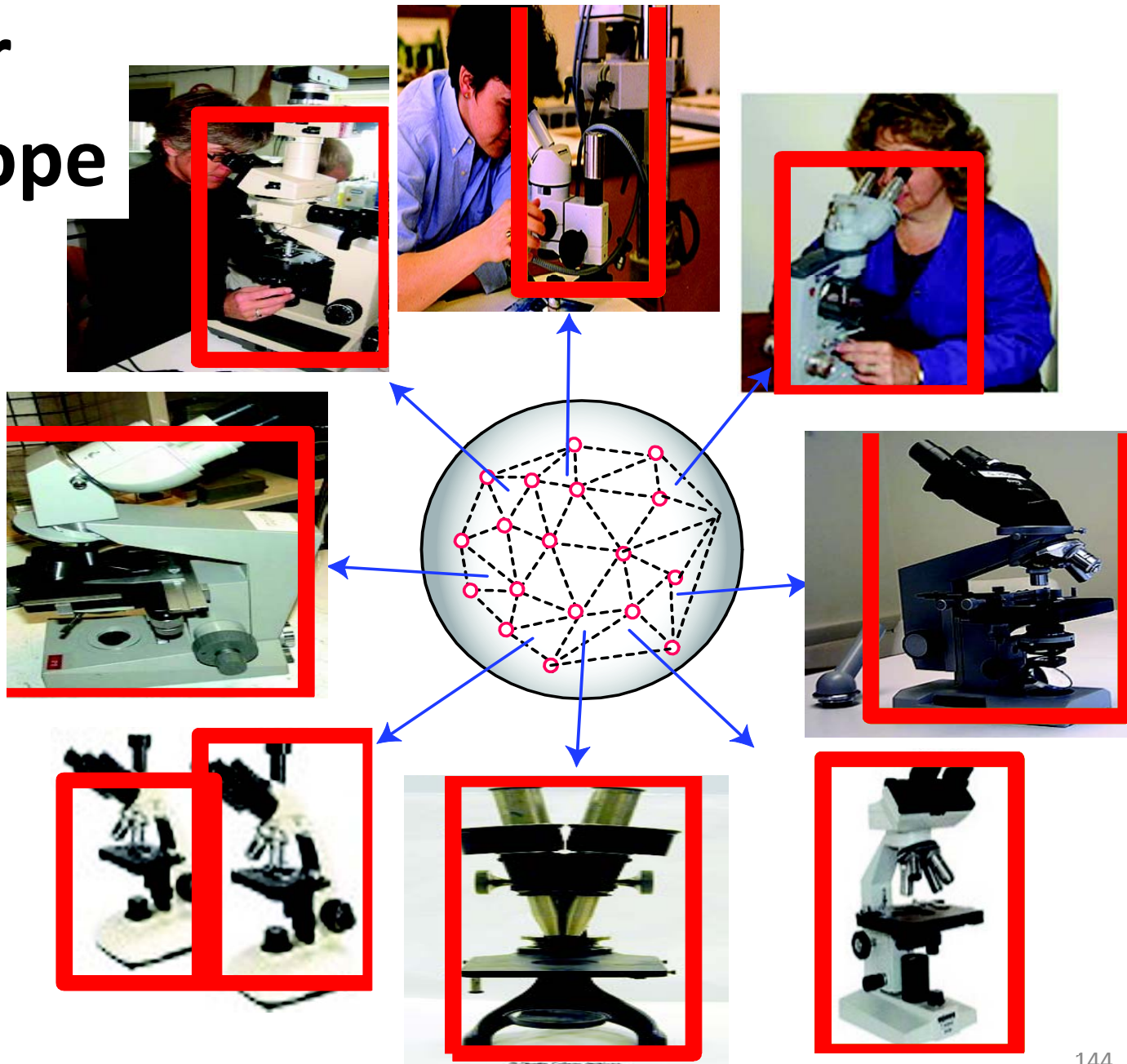


# Bicycle



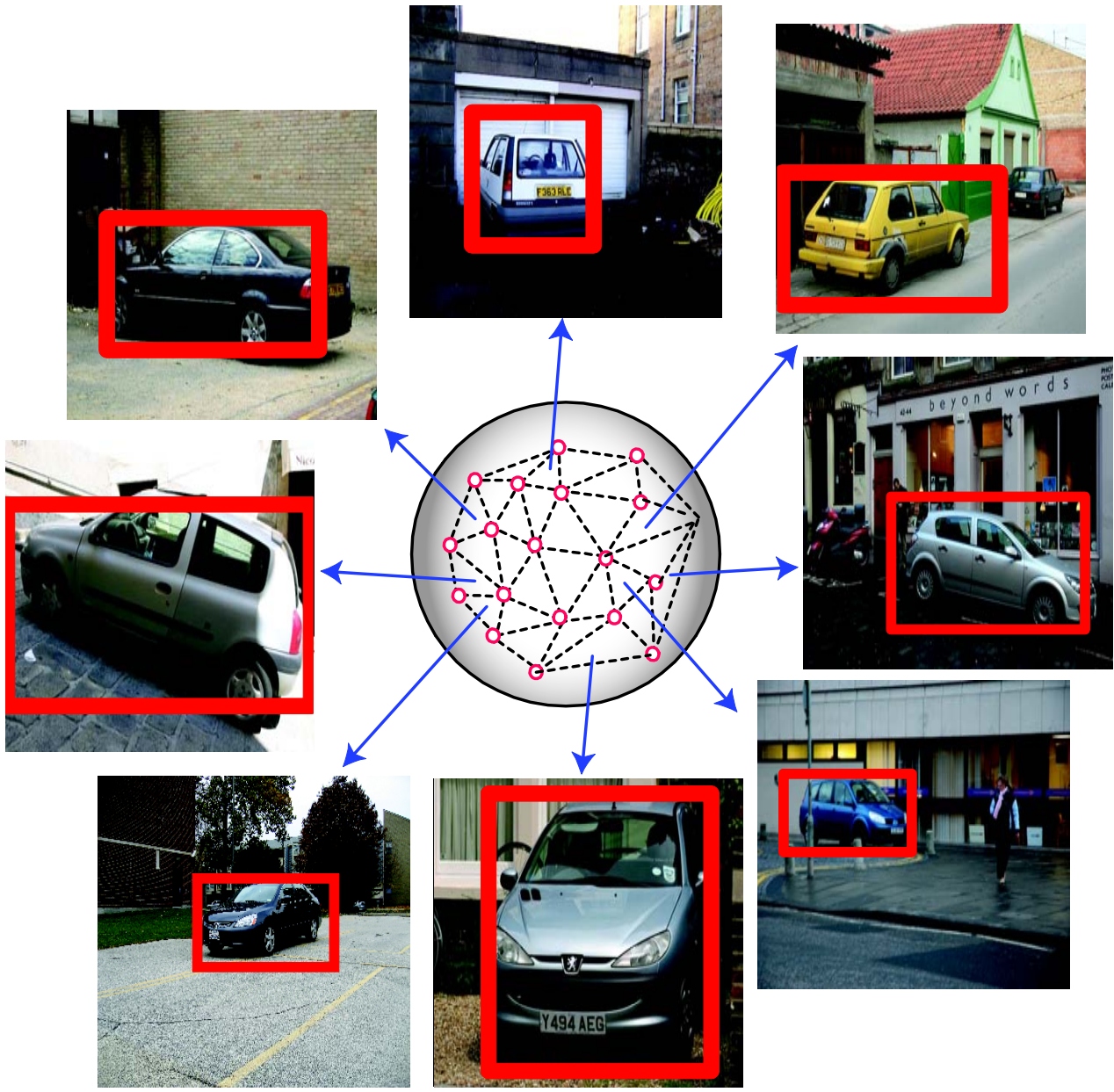
Notice the viewpoint variability in the dataset!

# Binocular Microscope

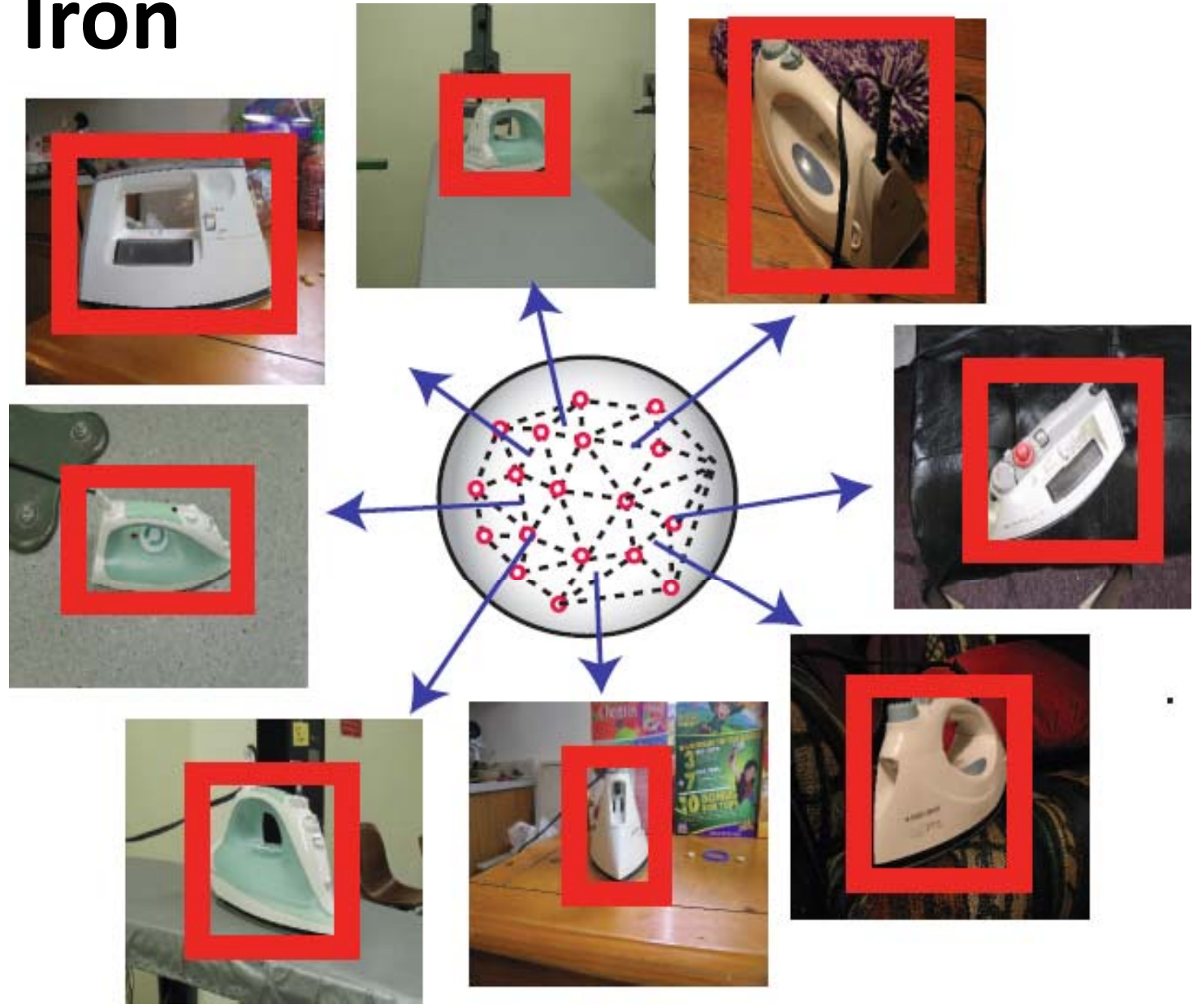




# Car



# Travel Iron



# Novel view object synthesis from a single image

For the first time!

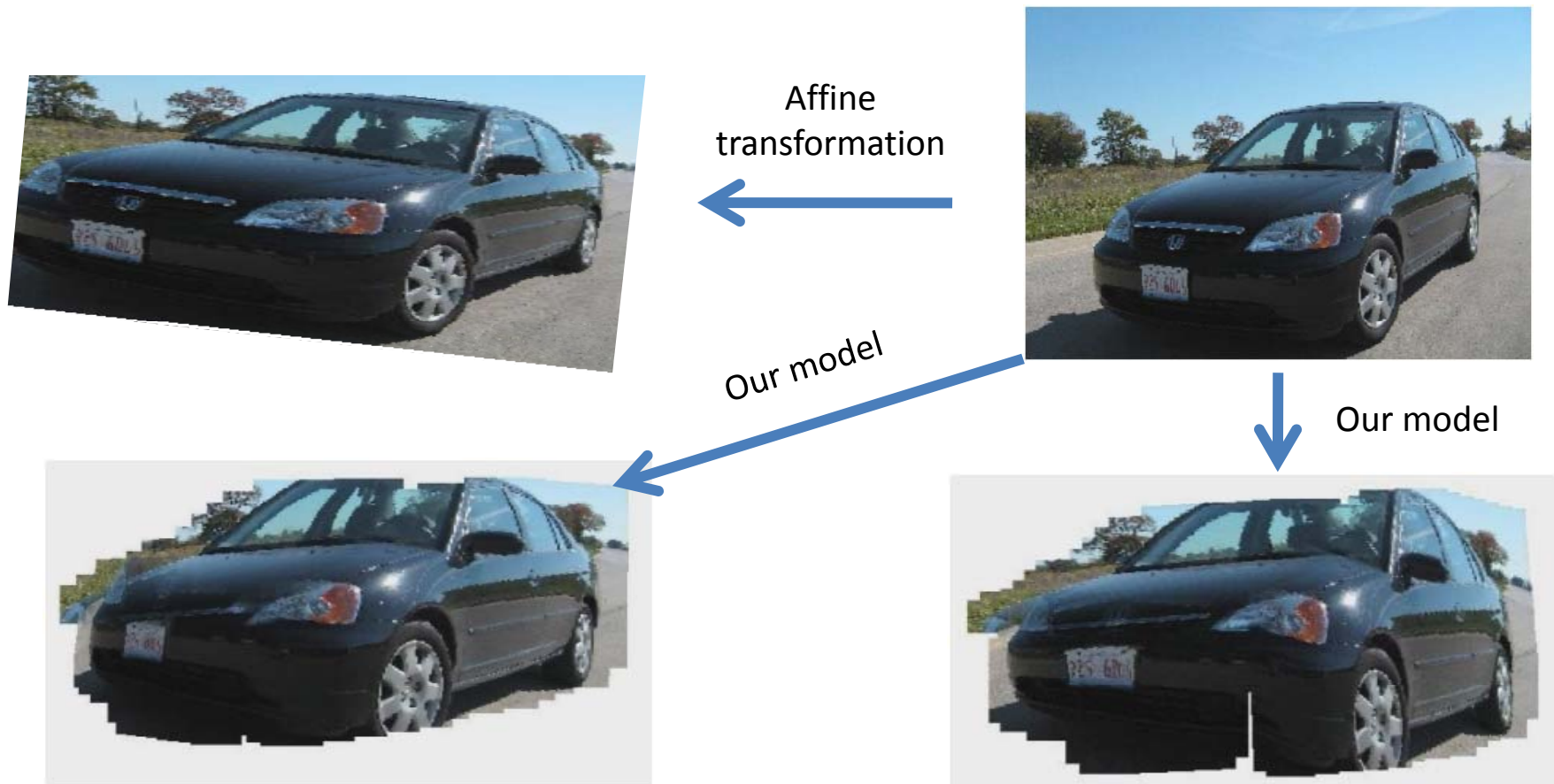
[For natural scenes, see Hoiem et al 07;  
Saxena et al 07]



# Novel view object synthesis from a single image

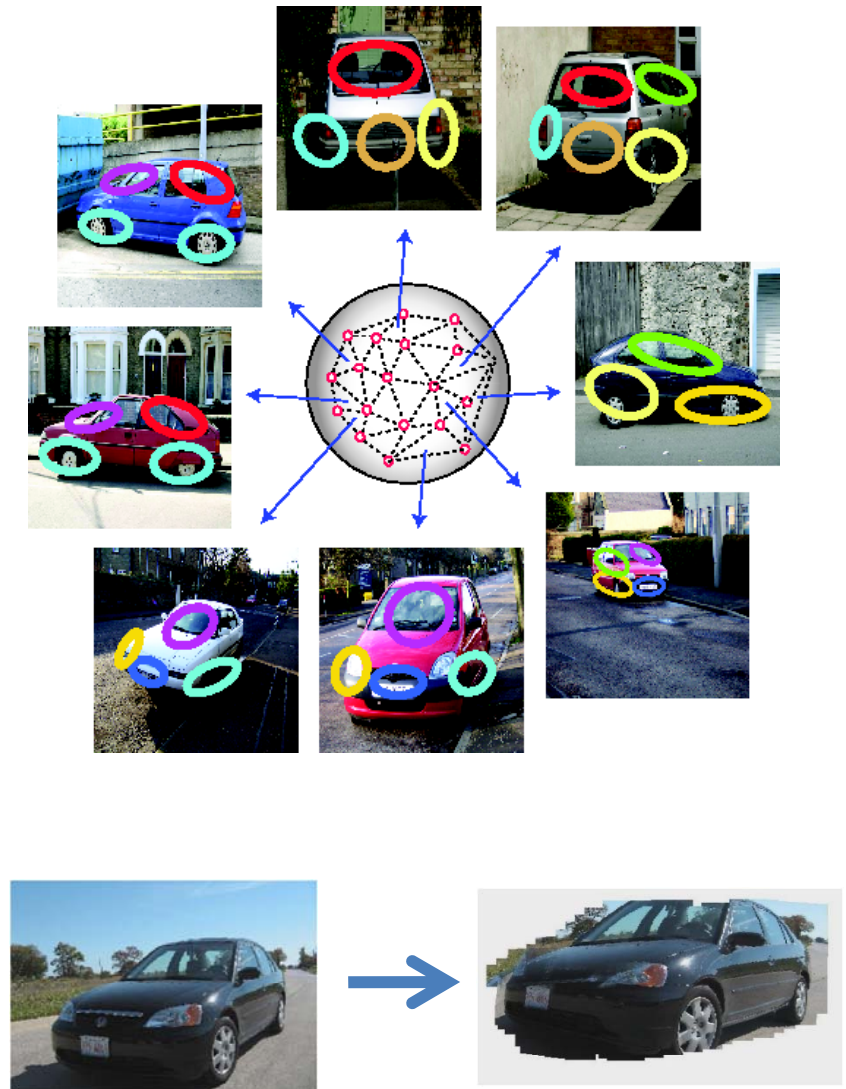
For the first time!

[For natural scenes, see Hoiem et al 07;  
Saxena et al 07]



# Saravese Conclusions

- A **new part-based multi-view** representation for object categories
- **Incremental learning** scheme with **little supervision**
- Achieve **accurate pose estimation** tested on up to **16 categories**
- **Image based rendering** from just **one single image!**





# Today

- Naïve-Bayes Nearest Neighbor (Irani)
- ISM (Liebe)
- Constellation Models (Fergus)
- Transformed LDA Models (Sudderth)
- 3-D view models (Saravese)