

# NONLINEAR STANDING WAVE EXCITATION BY SERIES-RESONANCE ENHANCED HARMONICS IN LOW PRESSURE CAPACITIVE DISCHARGES

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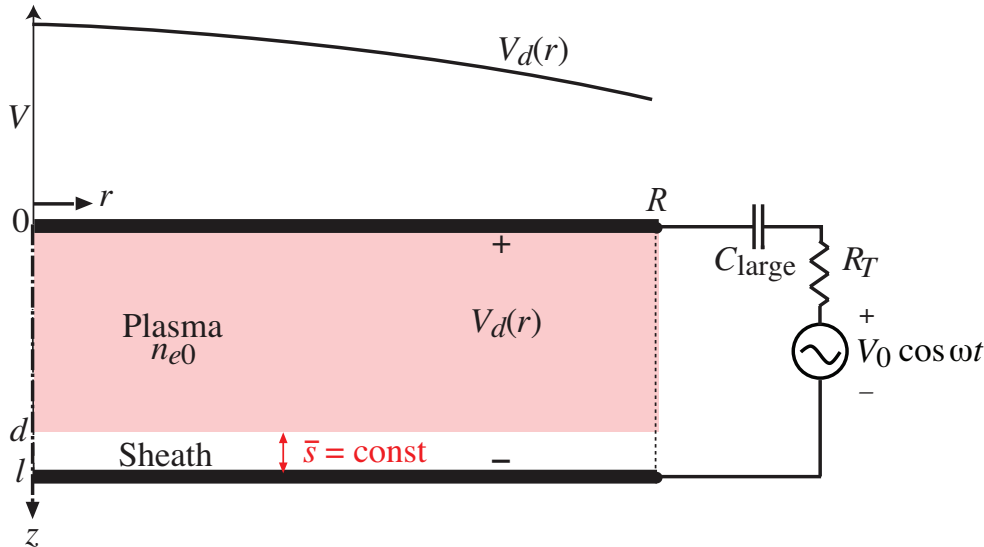
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# INTRODUCTION — STANDING WAVES

(Lieberman et al, PSST, 2002)

- Cylindrical discharge driven at outer radius
- **Linear** sheath model (constant sheath width  $\bar{s}$ )
- **Electromagnetic** fields



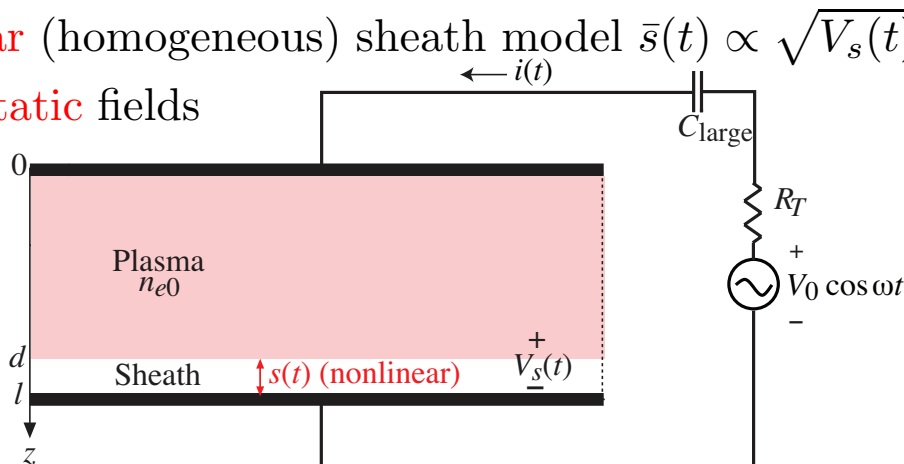
- Spatial (quarter-wave) resonance

$$\omega_{\text{SW}} = \left( \frac{\bar{s}}{l} \right)^{1/2} \frac{2.405 c}{R}$$

# INTRODUCTION — NONLINEAR SERIES RESONANCE

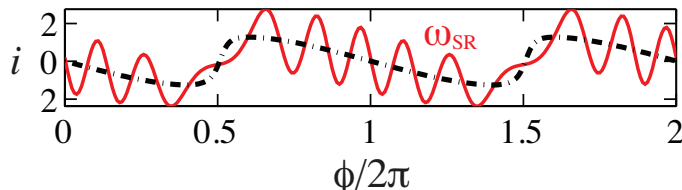
(Mussenbrock and Brinkmann, APL, 2006; Lieberman et al, PoP, 2008)

- Voltage-driven, asymmetric (single sheath) discharge
- **Nonlinear** (homogeneous) sheath model  $\bar{s}(t) \propto \sqrt{V_s(t)}$
- **Electrostatic** fields



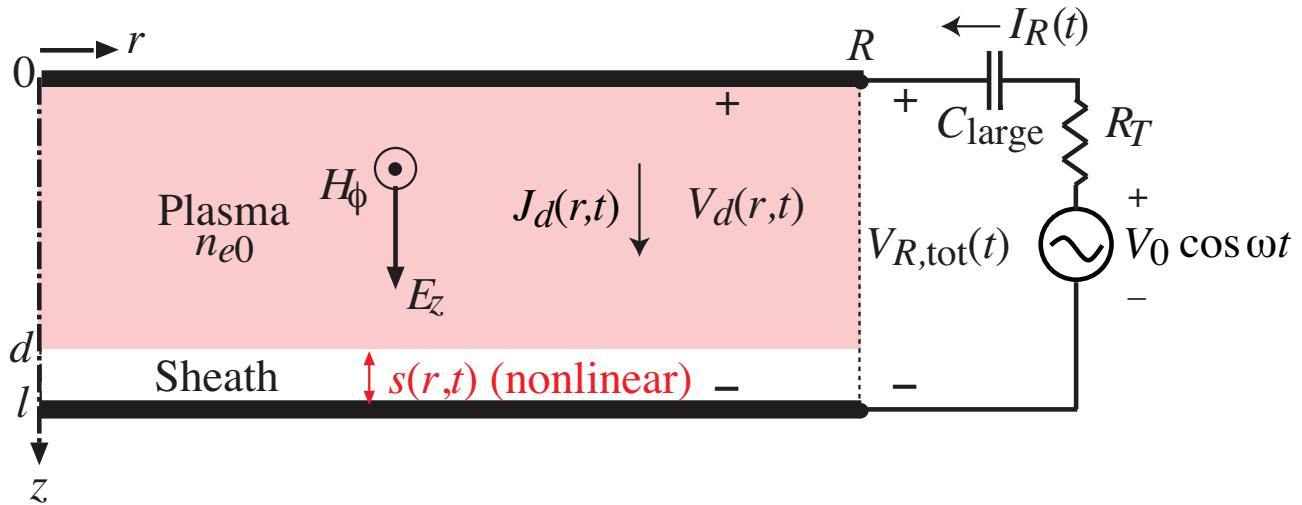
- Series resonance (capacitive sheath + inductive plasma)

$$\omega_{\text{SR}} = \left( \frac{\bar{s}}{l} \right)^{1/2} \omega_p \approx N\omega$$



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# SERIES RESONANCE ENHANCED STANDING WAVES



- Nonlinear radially-varying sheath + electromagnetic fields
- Low density regime ( $E_z \gg E_r$ ) with ordering

$$s \ll l \ll \delta_p, R$$

with  $\delta_p = c/\omega_p$  the collisionless skin depth

# MODEL EQUATIONS AND BASE CASE

$$\frac{\partial \Sigma}{\partial t} = J_d - J_{i0} + J_{e0} e^{-\Sigma^2 / 2en_e \epsilon_0 T_e}, \quad \Sigma > 0, \quad (\text{sheath charge})$$

$$\frac{\partial J_d}{\partial t} = \frac{e^2 n_e}{m d} (V_d - V_{dc}) - \frac{e}{2\epsilon_0 m d} \Sigma^2 - \nu J_d, \quad (\text{axial current density})$$

$$\frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial V_d}{\partial r} \right) = \mu_0 l \frac{\partial J_d}{\partial t}, \quad (\text{radial transmission line voltage})$$

$\Sigma = en_e s(r, t)$ ,  $\nu =$  collision frequency,  $V_{dc} =$  bias voltage

- Solve for  $V_d(r, t)$ ,  $J_d(r, t)$ ,  $s(r, t)$ , and  $V_{dc}$

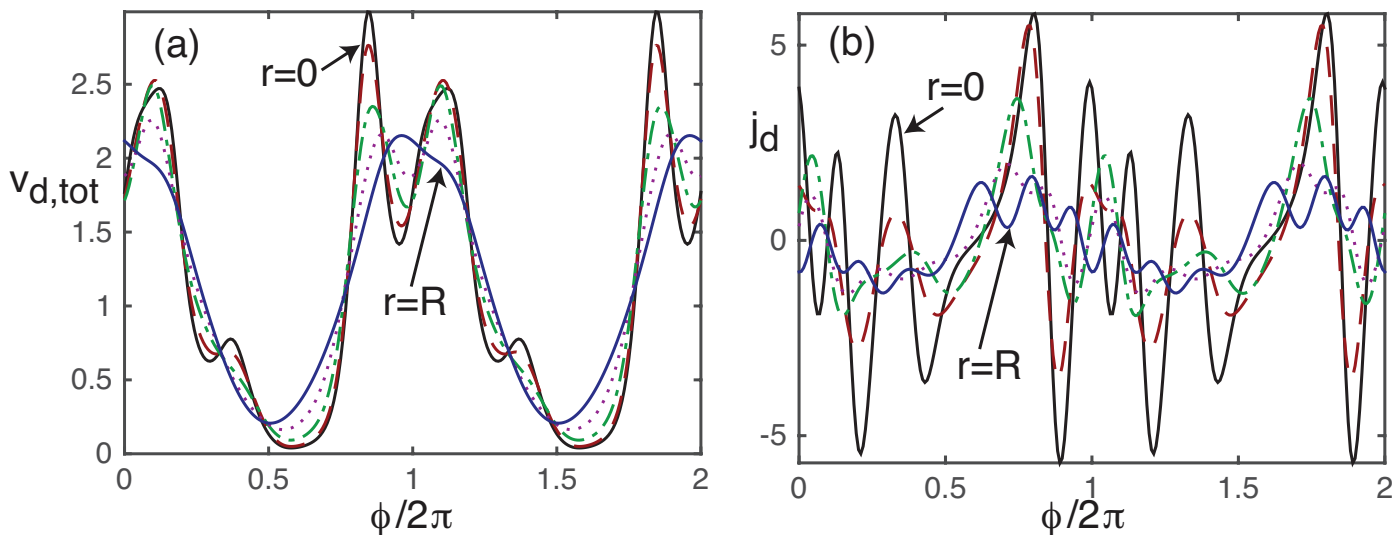
- **BASE CASE:**

$l = 2$  cm,  $R = 15$  cm conducting electrodes

10 mT argon,  $n_e = 2 \times 10^{16} \text{ m}^{-3}$ ,  $T_e = 3$  V

$V_0 = 500$  V,  $f = 60$  MHz,  $R_T = 0.5 \Omega$

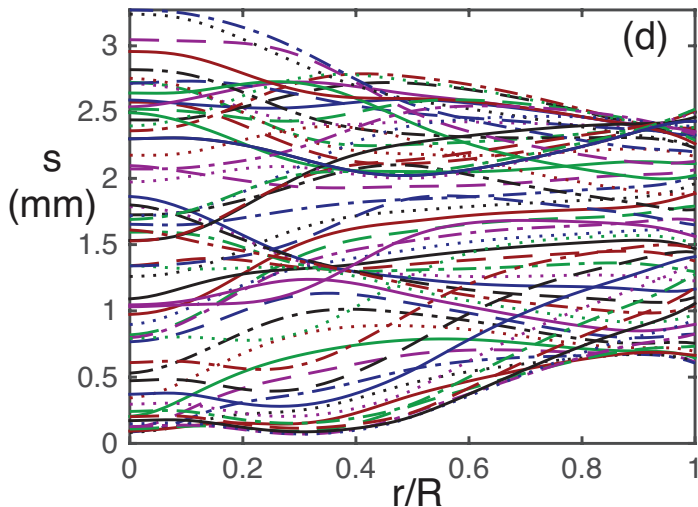
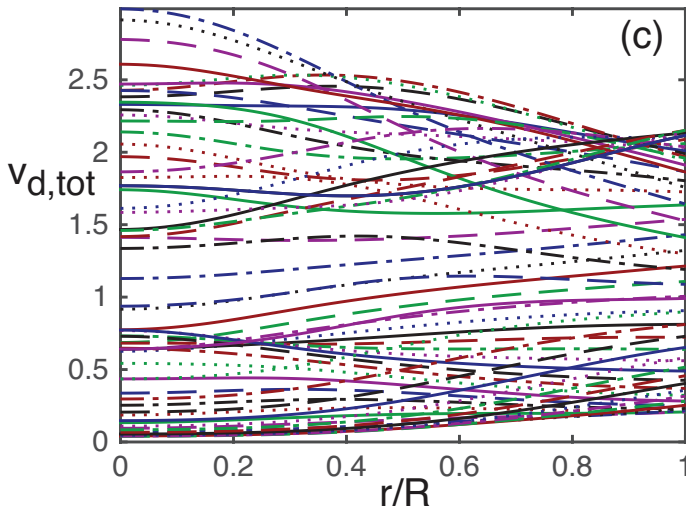
# BASE CASE DISCHARGE VOLTAGE AND CURRENT



- Normalized discharge voltage has weak harmonic content at  $r = R$ ; stronger at  $r = 0$
- Voltage at  $r = R$  can be greater than at  $r = 0$
- Normalized discharge current density shows strong harmonics; series resonance oscillations at  $r = R$ ; strong at  $r = 0$

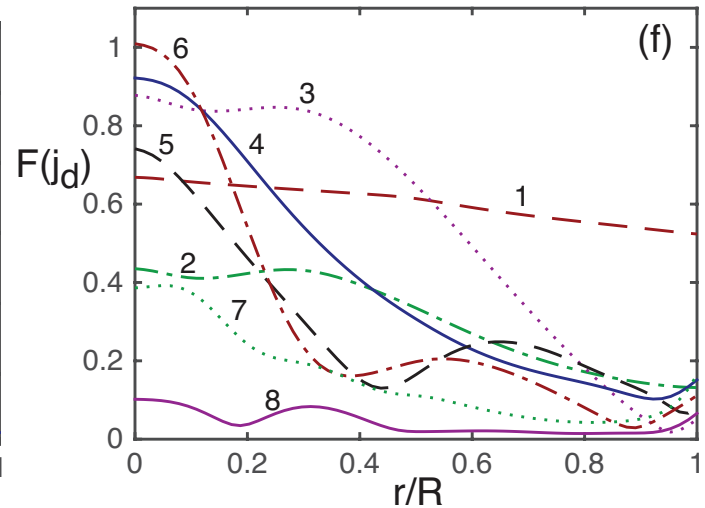
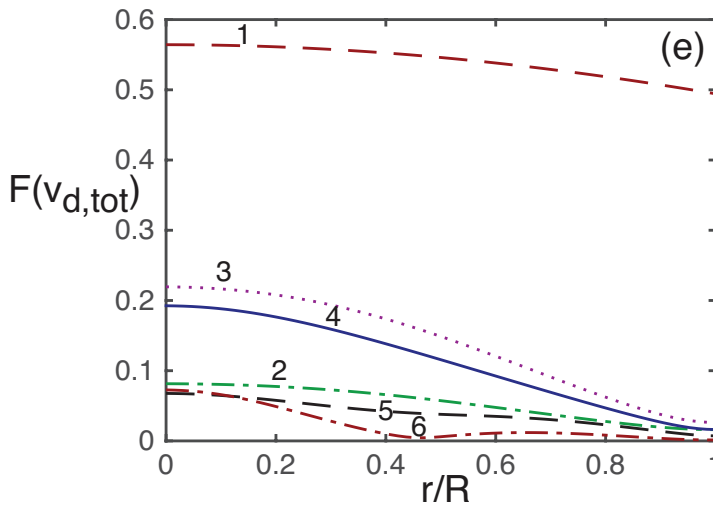
# BASE CASE VOLTAGE AND SHEATH MOTION

(65 times within an rf cycle)



- Maximum discharge voltage is higher at  $r = 0$  than at  $r = R$
- Minimum sheath width at  $r = 0$  is smaller than at  $r = R$   
⇒ electrons collected near  $r = 0$ , ions collected near  $r = R$
- Maximum sheath width at  $r = 0$  is larger than at  $r = R$
- Sheath motion shows series resonance oscillations; strong at  $r = 0$

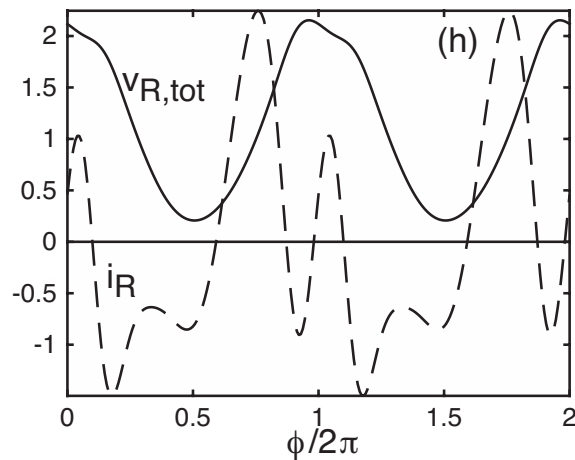
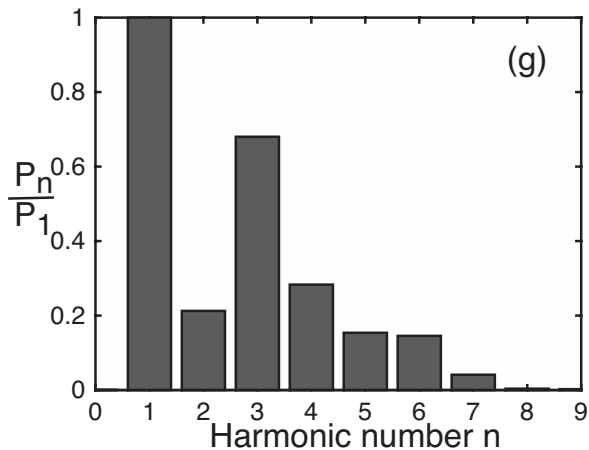
# BASE CASE FOURIER TRANSFORMS OF V AND J



- Fundamental voltage and current show a weak standing wave
- Voltage shows significant 3rd and 4th harmonics
- Discharge current shows strong central ( $r = 0$ ) 3–6 harmonics
  - $J \propto \omega CV$  (capacitive sheath)
  - Series resonance enhancement (sheath resonates with plasma)

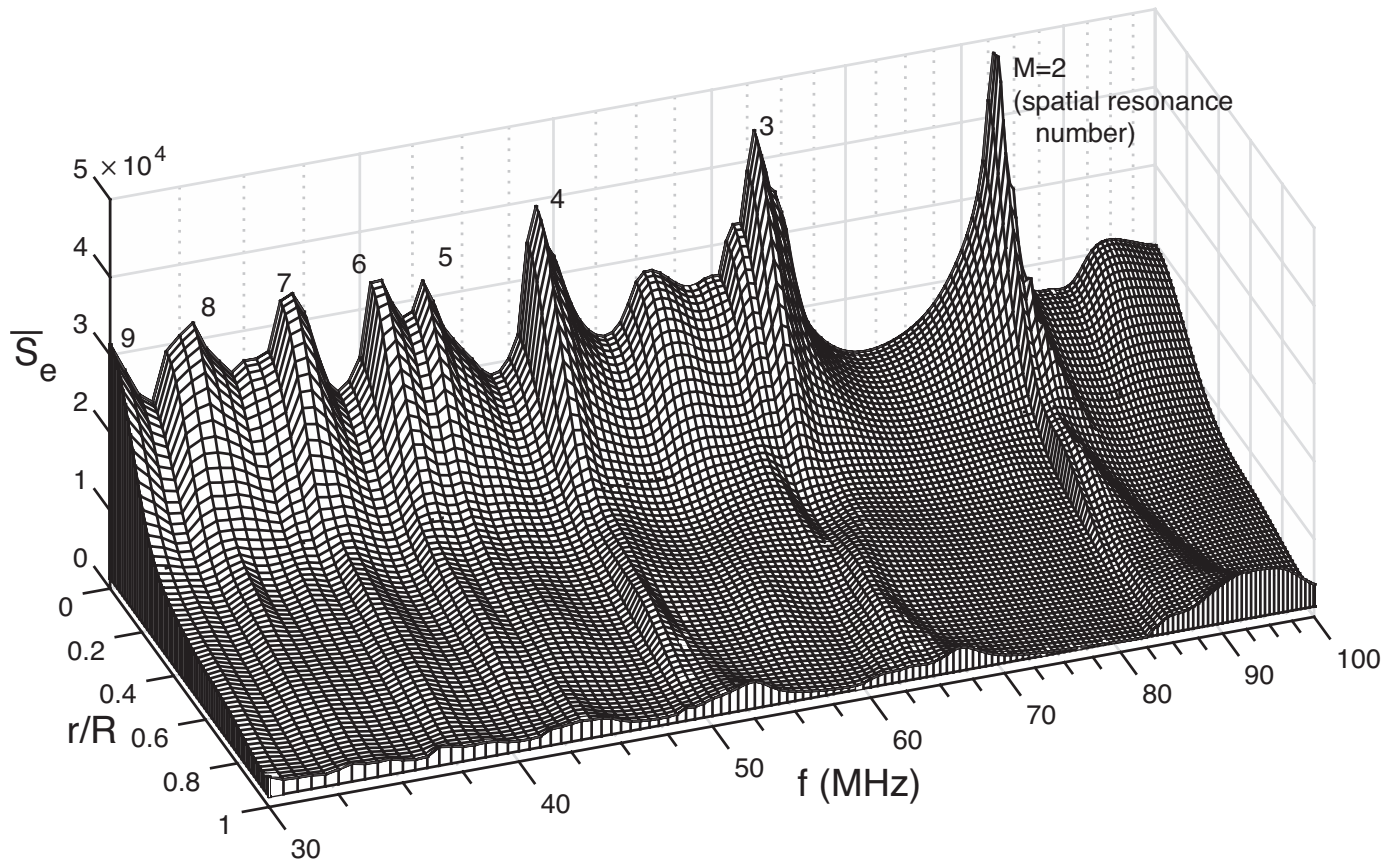


# BASE CASE TOTAL POWER AND EXCITATION V-I



- Total electron power has strong 3rd and 4th harmonics
- Excitation voltage is nearly sinusoidal with a dc bias
- Excitation current has strong harmonic content

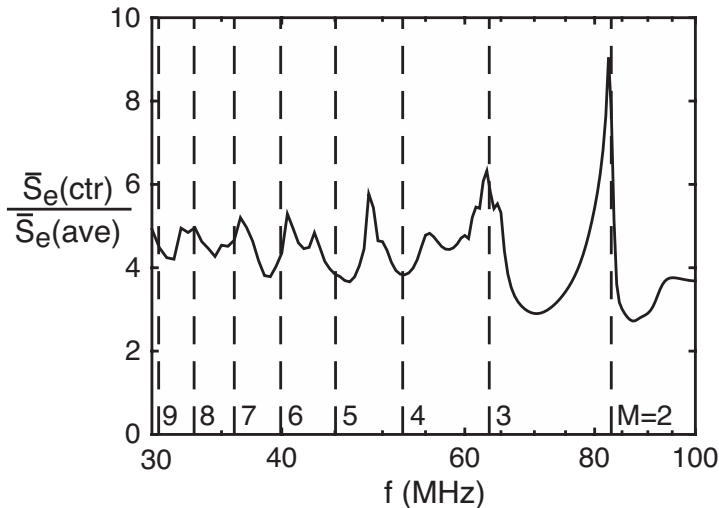
# POWER/AREA VS FREQUENCY AND RADIUS



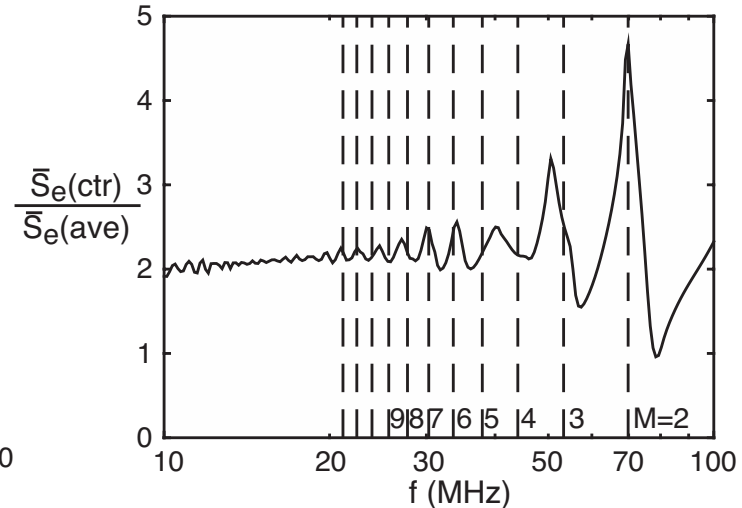
- Strong spatial resonance effects seen near  $M\omega = \omega_{SW}$

# CENTER-TO-AVERAGE POWER/AREA

$$n_e = 2 \times 10^{16} \text{ m}^{-3}$$



$$n_e = 5 \times 10^{15} \text{ m}^{-3}$$



- Dashed vertical lines are the spatial resonances
- Even at lower frequencies there is a significant center-peaking of the electron power/area

# CONCLUSIONS

- We developed and numerically solved a nonlinear radial transmission line model of an asymmetrically driven rf capacitive discharge.
- We found that the series resonance-enhanced harmonics of the driving frequency coupled strongly to the standing wave spatial resonances.
- We found significant center-peaking of the electron power/area, even at low excitation frequencies.
- These phenomena may be responsible for the center-peaked plasma density seen experimentally in high frequency capacitive discharges (e.g., Sawada et al, JJAP, 2014).

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